

PREDICTIVE MONTE CARLO TOOLS FOR COLLIDERS

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LECTURE I

TASI 2013, Boulder CO

TEST: HOW MUCH DO I KNOW ABOUT MC's?

Statements		TRUE	FALSE	IT DEPENDS	l have no clue
0	MC's are black boxes, I don't need to know the details as long as there are no bugs.				
Ι	A MC generator produces ''unweighted'' events, i.e., events distributed as in Nature.				
2	MC's are based on a classical approximation (Markov Chain), QM effects are not included.				
3	The "Sudakov form factor" directly quantifies how likely it is for a parton to undergo branching.				
4	A calculation/code at NLO for a process provides NLO predictions for any IR safe observable.				
5	Tree-level based MC's are less accurate than those at NLO.				

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TEST: HOW MUCH DO I KNOW ABOUT MC's?

Score	Result	Comment	
≥5	Addict	Always keep in mind that there are also other interesting activities in the field.	
4	Excellent	No problem in following these lectures.	
3	Fair	Check out carefully the missed topics.	
≤2	Room for improvement	Enroll in a MC crash course at your home institution.	
6 x no clue	No clue	It's Time to Call 9111 I a a A b c P a o # We to do no ENERCLICY	







Background directly measured from data. TH needed only for parameter extraction (Normalization, acceptance,...)

shape









"easy"

Background directly measured from data. TH needed only for parameter extraction (Normalization, acceptance,...)

hard

Background shapes needed. Flexible MC for both signal and background tuned and validated with data.

shape

peak









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hard

Background shapes needed. Flexible MC for both signal and background tuned and validated with data.

discriminant

$pp \rightarrow H \rightarrow W^+W^-$



very hard

Background normalization and shapes known very well. Interplay with the best theoretical predictions (via MC) and data.



NO SIGN OF NEW PHYSICS (SO FAR)!

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MC developer



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• Accuracy: accurate simulations for both SM and BSM are a must.

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- Confidence on possible excesses, evidences and eventually discoveries builds upon an intense (and often non-linear) process of description/ prediction of data via MC's.
- Both **measurements** and **exclusions** rely on accurate predictions.



Even this plot actually needs theory input (and the total quoted uncertainty in the measurements does have a contribution from theory)!!!

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NEW GENERATION (LHC) OF MC TOOLS

Theory

Lagrangian Gauge invariance QCD Partons NLO Resummation

...

Detector simulation Pions, Kaons, ... Reconstruction B-tagging efficiency Boosted decision tree Neural network



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<image>

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AIMS FOR THESE LECTURES

- Recall the basics of the necessary QCD concepts to understand what is going on in a pp event at the TeV scale.
- Critically revisit the "old" ways of making predictions for hadron colliders: either via fixed-order predictions or parton showers.
- Present the new *predictive* techniques which allow to:
 - Merge tree-level calculations with parton showers (CKKW/MLM).
 - Match NLO calculations with parton showers (MC@NLO and POWHEG) automatically.

<u>WIKI</u>

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- Basics : LO predictions and event generation
- Fixed-order calculations : from NLO to NNLO
- Exclusive predictions : Parton Shower
- Merging ME+PS
- Matching NLO with PS



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Today

MASTER FORMULA FOR THE LHC



MASTER FORMULA FOR THE LHC

$\sum_{a,b} \int dx_1 dx_2 d\Phi_{\rm FS} f_a(x_1,\mu_F) f_b(x_2,\mu_F) \hat{\sigma}_{ab\to X}(\hat{s},\mu_F,\mu_R)$ Phase-space Parton density Parton-level cross

integral

functions

section

Two ingredients necessary:

I. Parton distribution functions : non perturbative (fit from experiments, but evolution from theory)

2. Parton-level cross section: short distance coefficients as an expansion in $\alpha_{\rm S}$ (from theory)

$\hat{\sigma}_{ab \to X}(\hat{s}, \mu_F, \mu_R)$ Parton-level cross section

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• Including higher corrections improves predictions and reduces theoretical uncertainties

How do we calculate a LO cross section for 3 jets at the LHC?

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I. Identify all subprocesses ($gg \rightarrow ggg$, $qg \rightarrow qgg...$) in:

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III. Square the amplitude, sum over spins & color, integrate over the phase space $(D \sim 3n)$

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PHASE-SPACE INTEGRAL

• Calculations of cross section or decay widths involve integrations over phase space of very complex functions



PHASE-SPACE INTEGRAL

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$$\sigma = \frac{1}{2s} \int |\mathcal{M}|^2 d\Phi(n)$$



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General and flexible method is needed: Numerical (Monte Carlo) integration



PHASE-SPACE

$$d\Phi_n = \left[\prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 (2E_i)}\right] (2\pi)^4 \delta^{(4)} (p_0 - \sum_{i=1}^n p_i)$$

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PHASE-SPACE

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$$d\Phi_{n} = \left[\Pi_{i=1}^{n} \frac{d^{3}p_{i}}{(2\pi)^{3}(2E_{i})}\right] (2\pi)^{4} \delta^{(4)}(p_{0} - \sum_{i=1}^{n} p_{i})$$

$$d\Phi_{2}(M) = \frac{1}{8\pi} \frac{2p}{M} \frac{d\Omega}{4\pi}$$

$$(n - \sum_{i=1}^{n} e^{i})$$

$$d\Phi_{n}(M) = \frac{1}{2\pi} \int_{0}^{(M-\mu)^{2}} d\mu^{2} d\Phi_{2}(M) d\Phi_{n-1}(\mu)$$

INTEGRALS AS AVERAGES

$$I = \int_{x_1}^{x_2} f(x) dx \quad \longrightarrow \quad I_N = (x_2 - x_1) \frac{1}{N} \sum_{i=1}^N f(x)$$

$$V = (x_2 - x_1) \int_{x_1}^{x_2} [f(x)]^2 dx - I^2 \quad \longrightarrow \quad V_N = (x_2 - x_1)^2 \frac{1}{N} \sum_{i=1}^N [f(x)]^2 - I_N^2$$

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$$I = I_N \pm \sqrt{V_N/N}$$

INTEGRALS AS AVERAGES

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$$I = I_N \pm \sqrt{V_N}/N$$

INTEGRALS AS AVERAGES

Convergence is slow but it can be estimated easily
 Error does not depend on # of dimensions!
 Improvement by minimizing V_N
 Optimal/Ideal case: f(x) = Constant ⇒ V_N = 0



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MG101



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more bins where f(x) is large

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Idea: learn during the run and build a step-function approximation p(x) of $f(x) \longrightarrow VEGAS$



more bins where f(x) is large

$$p(x) = \frac{1}{N_b \Delta x_i}, \quad x_i - \Delta x_i < x < x_i$$

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can be generalized to n dimensions:

$$p(\mathbf{x}) = p(\mathbf{x}) \bullet p(\mathbf{y}) \bullet p(\mathbf{z}) \dots$$

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but the peaks of f(x) need to be "aligned" to the axis!

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This is ok...
IMPORTANCE SAMPLING

can be generalized to n dimensions:

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This is not ok...

IMPORTANCE SAMPLING

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but it is sufficient to make a change of variables!



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In this case there is no unique tranformation: Vegas is bound to fail!



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Solution: use different transformations = channels

$$p(x) = \sum_{i=1}^{n} \alpha_i p_i(x) \qquad \text{with} \qquad \sum_{i=1}^{n} \alpha_i = 1$$

with each $p_i(x)$ taking care of one "peak" at the time



In this case there is no unique tranformation: Vegas is bound to fail! P

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In this case there is no unique tranformation: Vegas is bound to fail!

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But if you know where the peaks are (=in which variables) we can use different transformations= channels:

$$p(x) = \sum_{i=1}^{n} \alpha_i p_i(x) \quad \text{with} \quad \sum_{i=1}^{n} \alpha_i = 1$$
$$I = \int f(x) dx = \sum_{i=1}^{n} \alpha_i \int \frac{f(x)}{p(x)} p_i(x) dx$$

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- Advantages
 - The integral does not depend on the α_i but the variance does and can be minimised by a careful choice
- Drawbacks
 - Need to calculate all gi values for each point
 - Each phase space channel must be invertible
 - N coupled equations for α_i so it might only work for small number of channels

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 - Need to calculate all gi values for each point
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Very popular method!

MULTI-CHANNEL BASED ON SINGLE DIAGRAMS

Consider the integration of an amplitude |M|^2 at treel level which lots of diagrams contribute to. If there were a basis of functions,

$$f = \sum_{i=1}^{n} f_i$$
 with $f_i \ge 0$, $\forall i$,

such that:

I. we know how to integrate each one of them,

2. they describe all possible peaks,

then the problem would be solved:

$$I = \int d\vec{\Phi} f(\vec{\Phi}) = \sum_{i=1}^{n} \int d\vec{\Phi} g_i(\vec{\Phi}) \frac{f_i(\vec{\Phi})}{g_i(\vec{\Phi})} = \sum_{i=1}^{n} I_i,$$

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Does such a basis exist?

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bes such a basis exist? YES! $f_i = \frac{|A_i|^2}{\sum_i |A_i|^2} |A_{\text{tot}}|^2$

MULTI-CHANNEL : MADGRAPH

- Key Idea
 - Any single diagram is "easy" to integrate
 - Divide integration into pieces, based on diagrams
- Get N independent integrals
 - Errors add in quadrature so no extra cost
 - No need to calculate "weight" function from other channels.
 - Can optimize # of points for each one independently
 - Parallel in nature
- What about interference?
 - Never creates "new" peaks, so we're OK!

EXERCISE: TOP DECAY



Easy but non-trivial

• Breit-Wigner peak
$$rac{1}{(q^2-m_W^2)^2+\Gamma_W^2m_W^2}$$
 to be ''flattened'':

• Choose the right "channel" for the phase space:



EXERCISE: TOP DECAY





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- Every phase-space point computed in this way, can be seen as an event (=collision) in a detector
- However, they still carry the "weight" of the matrix elements:
 events with large weights where the cross section is large
 events with small weights where the cross section is small
- In nature, the events don't carry a weight:
 more events where the cross section is large
 less events where the cross section is small
- How to go from weighted events to unweighted events?



Alternative way

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Alternative way

I. (randomly) pick x

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Par



Alternative way

I. (randomly) pick x2. calculate f(x)

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Alternative way

I. (randomly) pick x
2. calculate f(x)
3. (randomly) pick 0<y<fmax

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Alternative way

- I. (randomly) pick x
- 2. calculate f(x)
- 3. (randomly) pick 0<y<fmax

4. Compare: if f(x)>y accept event,



Alternative way

- I. (randomly) pick x
- 2. calculate f(x)
- 3. (randomly) pick 0<y<fmax
- 4. Compare: if f(x)>y accept event,else reject it.



Alternative way

- I. (randomly) pick x
- 2. calculate f(x)
- 3. (randomly) pick 0<y<fmax
- 4. Compare: if f(x)>y accept event,
 - else reject it.
 - = efficiency



What's the difference?

before:

Same # of events in areas of phase space with very different probabilities:

Events must have different weights:

$$w_i = p(x_i)$$



What's the difference? after:

events is proportional to the probability of areas of phase space:

Events have all the same weight (''unweighted'')

Events distributed as in Nature



Improved

I. pick x distributed as p(x)

2. calculate f(x) and p(x)

3. pick 0<y<1

Compare:
 if f(x)>y p(x) accept event,

else reject it.

much better efficiency!!!



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MC integrator

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MC EVENT GENERATOR: DEFINITION

At the most basic level a Monte Carlo event generator is a program which produces particle physics events with the same probability as they occur in nature (virtual collider).

In practice it performs (a possibly large) number of (sometimes very difficult) integrals and then unweights to give the four momenta of the particles that interact with the detector (simulation).

Note that, at least among theorists, the definition of a "Monte Carlo program" also includes codes which don't provide a fully exclusive information on the final state but only cross sections or distributions at the parton level, even when no unweighting can be performed (typically at NLO).

I will refer to these kind of codes as "MC integrators".



GENERAL STRUCTURE

Includes all possible subprocess leading to a given multi-jet final state automatically or manually (done once for all)

d~ d -> a d d~ u u~ g d~ d -> a d d~ c c~ g s~ s -> a d d~ u u~ g s~ s -> a d d~ c c~ g

...

"Automatically" generates a code to 2 calculate |M|2 for arbitrary processes with many partons in the final state. Use Feynman diagrams with tricks to reduce the factorial growth, others have recursive relations to reduce the 1complexity to exponential. ☺


GENERAL STRUCTURE



Integrate the matrix element over the phase space using a multichannel technique and using parton-level cuts.

Events are obtained by unweighting. These are at the parton-level. Information on particle id, momenta, spin, color is given in the Les Houches format.





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CODES

- Example of tree-level Monte Carlo codes:
 - Alpgen: fast matrix elements due to use of recursion relations. SM only.
 - Comix (Sherpa): fast matrix elements due to use of recursion relations. Some BSM models implemented (however, e.g. no Majorana particles).
 - MadGraph: Feynman diagrams to generate matrix elements which results in high unweighting efficiency. Virtually all BSM models are (or can be) implemented.
- and more: CalcHEP/CompHEP, Whizard...

Skip FeynRules



- FeynRules is a Mathematica package that allows to derive Feynman rules from a Lagrangian.
- Current public version: I.6.x.
- The only requirements on the Lagrangian are:
 - → All indices need to be contracted (i.e. Lorentz and gauge invariance)
 - ➡ Locality
 - ➡ Supported field types:

spin 0, 1/2, 1, 2 & ghosts (3/2 are coming)

- FeynRules comes with a set of interfaces, that allow to export the Feynman rules to various matrix element generators.
- Interfaces coming with current public version
 - CalcHep / CompHep
 - FeynArts / FormCalc
 - ➡ MadGraph
 - ➡ Sherpa
 - ➡ Whizard / Omega
 - Universal FeynRules
 Output



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 Output



• The input requested form the user is twofold.

 The Model File: Definitions of particles and parameters (e.g., a quark)

F[1] ==	
{ClassName	-> q,
SelfConjugate	-> False,
Indices	-> {Index[Colour]},
Mass	-> {MQ, 200},
Width	-> {WQ, 5} }

• The Lagrangian:

$$\mathcal{L} = -\frac{1}{4} G^a_{\mu\nu} \, G^{\mu\nu}_a + i\bar{q} \, \gamma^\mu \, D_\mu q - M_q \, \bar{q} \, q$$

L =

- -1/4 FS[G,mu,nu,a] FS[G,mu,nu,a] + I qbar.Ga[mu].del[q,mu]
- MQ qbar.q

• Once this information has been provided, FeynRules can be used to compute the Feynman rules for the model:

FeynmanRules[L]

• Once this information has been provided, FeynRules can be used to compute the Feynman rules for the model:

FeynmanRules[L]

Vertex 1

```
Particle 1 : Vector, G
```

```
Particle 2 : Dirac , q^{\dagger}
```

```
Particle 3 : Dirac , q
```

Vertex:

$$i gs \gamma^{\mu_1}{}_{s_2,s_3} \delta_{f_2,f_3} T^{a_1}{}_{i_2,i_3}$$

 Once we have the Feynman rules, we can export them to a MC event generator via the UFO:

WriteUFOutput[L]

• This produces a set of files that can be directly used in the matrix element generator (''plug 'n' play'').

interactions.dat

GGGG MGVX2 OCD OCD	q q G G G G	GG QCD MGVX1 QCD	
	GGGG	MGVX2 QCD (QD

q	q~	F	S	ZERO	ZERO	Τ	d	1
G	G	V	С	ZERO	ZERO	0	G 2	;1

couplings.dat	
GG(1) = -G GG(1) = -G MGVX1 = G $MGVX2 = G^{2}$	



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- Already available models:
 - Standard Model
 - Simple extensions of the SM (4th generation, 2HDM, ...)
 - SUSY models ((N)MSSM, RPV-MSSM, ...)
 - Extra-dimensional models (minimal UED, Large Extra Dimensions, ...)
 - Strongly coupled and effective field theories (Minimal Walking Technicolor, Chiral Perturbation theory, ...)
- Straight-forward to start from a given model and to add extra particles/ interactions
- All available models, restrictions, syntax and more information can be found on the FeynRules website:

http://feynrules.phys.ucl.ac.be

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LO PREDICTIONS : REMARKS

$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \to X}(x_1, x_2, \alpha_S(\mu_R^2), \frac{Q^2}{\mu_F^2}, \frac{Q^2}{\mu_R^2})$$

• By calculating the short distance coefficient at tree-level we obtain the first estimate of rates for inclusive final states.

• Even at LO extra radiation is included: it is described by the PDF's in the initial state and by the definition of a final state parton, which at LO represents all possible final state evolutions.

• Due to the above approximations a cross section at LO can strongly depend on the factorization and renormalization scales.

• Predictions can be systematically improved, at NLO and NNLO, by including higher order corrections in the short distance and in the evolution of the PDF's.



- Having accurate and flexible simulations tools available for the LHC is a necessity (even more now!!)
- At LO event generation is technically challenging, yet conceptually straightforward.



To organize this presentation I have benefited from lectures (and actual slides), talks and discussions with many people. In particular:

- Mike Seymour (MC basics)
- Claude Duhr (FeynRules)
- Johan Alwall (ME+PS merging)
- Rikkert Frederix, Paolo Torrielli (NLO+PS)
- Stefano Frixione, Michelangelo Mangano, Paolo Nason (for QCD, PS, LO, NLO, and more...)

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Whom I all warmly thank!!