

# BSM II

## AUTOMATION@NLO

HUA-SHENG SHAO  
CERN, PH-TH

LECTURE BSM I GIVEN BY BENJAMIN FUKS ON MONDAY

MadGraph School Shanghai 2015

MadGraph School on Collider Phenomenology

November 23-27, Shanghai Jiao Tong University



26 Nov 2015

# PREDICTION CHAIN



slide stealing from Valentin Hirschi

SU(3) x SU(2) x U(1) • **Symmetries**

$$G^{\mu\nu}G_{\mu\nu} + i\bar{q}(i)D_\mu\gamma^\mu q(i) + \dots$$

Standard Model • **Model**

$$= i\gamma^\mu t_{ij}^a, \dots$$

p p > j j QCD=2 • **Matrix Element**

$$\mathcal{M}_{gg \rightarrow d\bar{d}}^2, \dots$$

matrix.f • **Partonic Events**

```
<event>
5 16 0.35019064E-07 0.51353448E-03 1.79577472E-01 0.11721981+00
-1 -1 0 0 0 341 1.00000000E-10 0.00000000E-00 0.00000000E-00 0.00000000E-00
1 -1 0 0 501 0 1.00000000E-10 0.00000000E-00 0.00000000E-00 0.00000000E-00
20 1 1 2 0 0 1.35462641E+02 0.298420561E+02 0.462820
24 1 1 2 0 0 -1.39056110E+02 -2.45781831E+01 -2.09800
-24 1 1 2 0 0 1.37935445E+01 -2.73834381E+02 -5.06178
# 1 0 2 0 1.00000000E-00 0.100000001E-00 0 0 0 1.00000000E-01 0
</event>
<rngt>
0.41697537E+00 0.41697538E+00 } 1
0.41697538E+00 0.43335245E+00 0.199121501E+00
0.41697538E+00 0.43335245E+00 0.199121501E+00
0.41697538E+00 0.43335245E+00 0.199121501E+00
</rngt>
</event>
```

events.lhe • **Hadron Level**

$$\{\pi^0, K^+, e^+, p, \dots\}$$

events.hep • **Detector Level**



# BSM MODELS: READY FOR USE

## Available models

|   |  |
|---|--|
| <a href="#">Standard Model</a>                                | The SM implementation of FeynRules, included into the distribution of the FeynRules package.   |
| <a href="#">Simple extensions of the SM</a>                   | Several models based on the SM that include one or more additional particles, like a 4th generation, a second Higgs doublet or additional colored scalars. |
| <a href="#">Supersymmetric Models</a>                         | Various supersymmetric extensions of the SM, including the MSSM, the NMSSM and many more.  |
| <a href="#">Extra-dimensional Models</a>                      | Extensions of the SM including KK excitations of the SM particles.   |
| <a href="#">Strongly coupled and effective field theories</a> | Including Technicolor, Little Higgs, as well as SM higher-dimensional operators, vector-like quarks.   |
| <a href="#">Miscellaneous</a>                                 |  |
| <a href="#">NLO</a>   | Models ready for NLO computations  |



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| Model   | Short Description  | Contact   | Status    |
|---|--|---|-----------|
| <a href="#">Axigluon model</a>                  | The SM plus a scalar gluon field.  | S. Krastanov  | Available |
| <a href="#">DY SM extension</a>                 | The SM plus new spin-0, -1, and -2 bosons that contribute to Drell-Yan production of leptons at the LHC.   | N. Christensen  | Available |
| <a href="#">EFT mass basis</a>                  | The SM EFT Lagrangian in the mass basis  | B. Fuks, K. Mawatari                                    | Available |
| <a href="#">FCNC Higgs interactions</a>         | The SM plus higher-dimensional flavor changing Higgs interactions.   | S. Krastanov  | Available |
| <a href="#">Fourth generation model</a>         | A fourth generation model including a $t'$ and a $b'$  | C. Duhr   | Available |
| <a href="#">General 2HDM</a>                    | The most general 2HDM, including all flavor violation and mixing terms.  | C. Duhr, M. Herquet                                     | Available |
| <a href="#">Hidden Abelian Higgs Model</a>      | A $Z'$ model where the $Z'$ interacts with the SM through mixings, leading to very small non-SM like $Z'$ couplings.   | C. Duhr   | Available |
| <a href="#">HiggsCharacterisation</a>           | The model file for the spin/parity characterisation of a 125 GeV resonance.  | F. Demartin, K. Mawatari                                | Available |
| <a href="#">Higgs effective theory</a>          | An add-on for the SM implementation containing the dimension 5 gluon fusion operator.  | C. Duhr   | Available |
| <a href="#">Higgs Effective Lagrangian</a>      | Higgs effective Lagrangian including operators up-to dimension 6.  | A. Alloul, B. Fuks and V. Sanz                          | Available |
| <a href="#">Hill Model</a>                      | A model with an unusual extension of the SM Higgs sector.  | P. de Aquino, C. Duhr                                   | Available |
| <a href="#">Inert Doublet Model</a>             | A model with an additional complex scalar $SU(2)_L$ doublet and an unbroken $Z_2$ symmetry under which all SM particles are even while the extra doublet is odd. | A. Goudelis, B. Herrmann, O. Stal                       | Available |
| <a href="#">Minimal <math>Z_p</math> models</a> | The minimal $Z'$ extension of the SM.  | L. Basso  | Available |
| <a href="#">Monotops</a>                        | The SM plus monotop effective Lagrangian.  | B. Fuks   | Available |
| <a href="#">Sextet diquarks</a>                 | The SM plus sextet diquark scalars.  | J. Alwall, C. Duhr                                      | Available |
| <a href="#">Standard model + Scalars</a>        | The SM, together with a set of singlet scalar particles coupling only to the SM Higgs, and allowing it to decay invisibly into this new scalar sector.           | C. Duhr   | Available |
| <a href="#">TFCNC</a>                           | The SM, plus FCNC top interactions.  | M. Buchkremer, G. Cacciapaglia, A. Deandrea, L. Panizzi | Available |
| <a href="#">Triplet diquarks</a>                | The SM plus triplet diquark scalars.   | J. Alwall, C. Duhr                                      | Available |



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| <a href="#">Miscellaneous</a>                                 |  |
| <b>NLO</b>  | Models ready for NLO computations  |

## Available models

| Description  | Contact     | Reference  | FeynRules model files         | UFO libraries                      | Validation material   |
|--|-------------|--|-------------------------------|------------------------------------|---|
| Dark matter simplified models ( <a href="#">more details</a> ) | K. Mawatari | -  | -                             | <a href="#">DMsimp_UFO.2.zip</a>   | -   |
| Glino pair production (SUSY-QCD)                               | B. Fuks     | <a href="#">arXiv:1510.00391</a>                                     | -                             | <a href="#">susyqcd_ufo.tgz</a>    | All figures available from the arxiv  |
| Higgs characterisation ( <a href="#">more details</a> )        | K. Mawatari | <a href="#">arXiv:1311.1829</a> ,<br><a href="#">arXiv:1407.5089</a> | -                             | <a href="#">HC_NLO_X0_UFO.zip</a>  | -   |
| Inclusive sgluon pair production                               | B. Fuks     | <a href="#">arXiv:1412.5589</a>                                      | <a href="#">sgluons.fr</a>    | <a href="#">sgluons_ufo.tgz</a>    | <a href="#">sgluons_validation.pdf</a> ;<br><a href="#">sgluons_validation_root.tgz</a>       |
| Stop pair -> t tbar + missing energy                           | B. Fuks     | <a href="#">arXiv:1412.5589</a>                                      | <a href="#">stop_ttmet.fr</a> | <a href="#">stop_ttmet_ufo.tgz</a> | <a href="#">stop_ttmet_validation.pdf</a> ;<br><a href="#">stop_ttmet_validation_root.tgz</a> |
| Two-Higgs-Doublet Model ( <a href="#">more details</a> )       | C. Degrande | <a href="#">arXiv:1406.3030</a>                                      | -                             | <a href="#">2HDM_NLO</a>           | -   |

<https://feynrules.irmp.ucl.ac.be/wiki/NLOModels>

# AUTOMATED LO CALCULATIONS

slide stealing from Benjamin Fuks

## ◆ A comprehensive approach to Monte Carlo simulations

[ Example based on FEYNRULES and MADGRAPH5\_aMC@NLO ]



## ◆ Streamline the chain from the model Lagrangian to analyzed simulated collisions

### ❖ Works at the **leading order**

- ★ Implementation of the new physics Lagrangian into FEYNRULES
- ★ Generation of a UFO model file
- ★ Import of the model into MADGRAPH5\_aMC@NLO
- ★ Hard scattering process with MADGRAPH5\_aMC@NLO
- ★ Matching to parton showering, multiparton matrix element merging, hadronization, detector simulation, etc.

### ❖ Fully tested and validated in the context of large classes of new physics models

What about new physics event generation  
at the **next-to-leading order** in QCD?

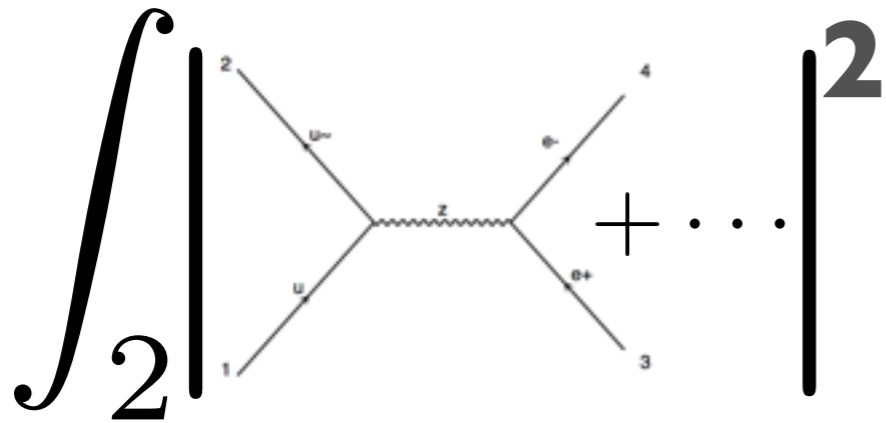
# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-} =$$



# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{LO}} =$$



# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{NLO}} =$$

$$\begin{aligned}
 & \int_2 \left| \begin{array}{c} \text{Diagram 1: } p \text{ (1) and } p \text{ (2) meet at a vertex, exchange a } Z \text{ boson, and produce } e^+ \text{ (3) and } e^- \text{ (4).} \\ \dots \end{array} \right|^2 + \int_3 \left| \begin{array}{c} \text{Diagram 2: } p \text{ (1) and } p \text{ (2) meet at a vertex, exchange a } Z \text{ boson, and produce } e^+ \text{ (3) and } e^- \text{ (4).} \\ \dots \end{array} \right|^2 \\
 & + \int_2 \left( \begin{array}{c} \text{Diagram 3: } p \text{ (1) and } p \text{ (2) meet at a vertex, exchange a } Z \text{ boson, and produce } e^+ \text{ (3) and } e^- \text{ (4).} \\ \dots \end{array} \right) \times \left( \begin{array}{c} \text{Diagram 4: } p \text{ (1) and } p \text{ (2) meet at a vertex, exchange a } Z \text{ boson, and produce } e^+ \text{ (3) and } e^- \text{ (4).} \\ \dots \end{array} \right) *
 \end{aligned}$$

# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{NLO}} =$$

$$\int_2 \left| \text{[Diagram 1]} + \dots \right|^2$$

Diagram 1: A tree-level process where two incoming quarks (1 and 2) annihilate into a virtual photon (Z), which then decays into an electron-positron pair (3 and 4).

$$+ \int_3 \left| \text{[Diagram 2]} + \dots \right|^2$$

Diagram 2: A tree-level process where an incoming quark (1) and an incoming gluon (5) interact via a top quark (2) loop to produce an electron-positron pair (3 and 4).

$$+ \int_2 \left( \text{[Diagram 3]} \right) \times \left( \text{[Diagram 1]} \right) *$$

Diagram 3: A tree-level process with a gluon loop on the quark line (1 and 2) before the annihilation into a virtual photon (Z) that decays into an electron-positron pair (3 and 4).

Infrared Div.  
 $\frac{c_{-2}}{\epsilon_{\text{IR}}^2} + \frac{c_{-1}}{\epsilon_{\text{IR}}}$



# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{NLO}} =$$

$$\int_2 \left| \text{[Diagram 1]} + \dots \right|^2 + \int_3 \left| \text{[Diagram 2]} + \dots \right|^2$$

Diagram 1: A tree-level process with two incoming quark lines (1, 2) and two outgoing lepton lines (3, 4). A gluon line (z) connects the quark and lepton vertices.

Diagram 2: A tree-level process with three incoming quark lines (1, 2, 3) and two outgoing lepton lines (4, 5). A gluon line (z) connects the quark and lepton vertices.

$$+ \int_2 \left( \text{[Diagram 1]} + \dots \right) \times \left( \text{[Diagram 1]} + \dots \right) *$$

Infrared Div.

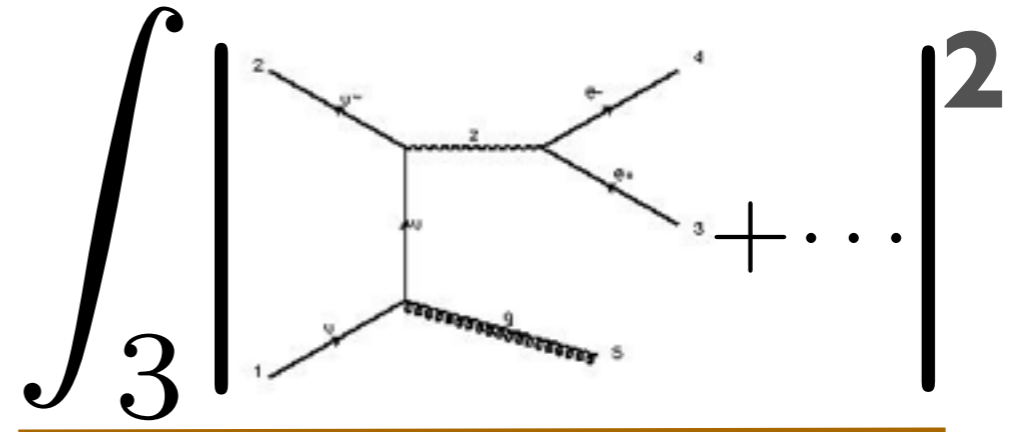
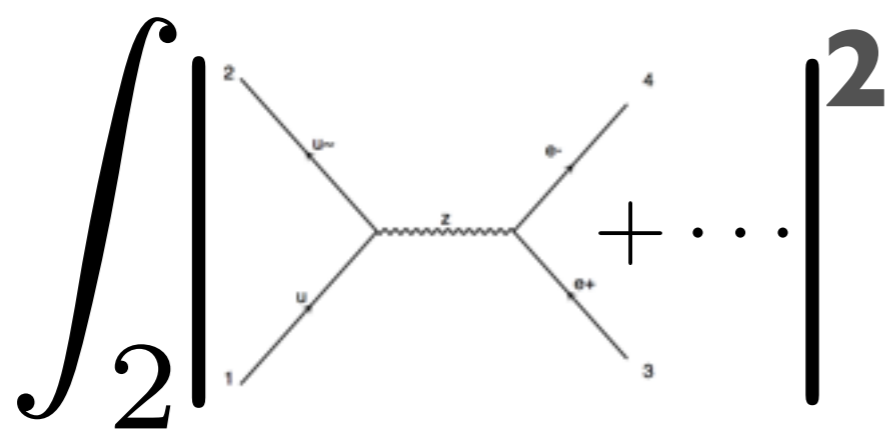
$$\frac{c_{-2}}{\epsilon_{\text{IR}}^2} + \frac{c_{-1}}{\epsilon_{\text{IR}}}$$

Ultraviolet Div.  $\frac{a}{\epsilon_{\text{UV}}}$

Infrared Div.  
 $-\frac{c_{-2}}{\epsilon_{\text{IR}}^2} - \frac{c_{-1}}{\epsilon_{\text{IR}}}$

# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{NLO}} =$$



$$+ \int_2 \left( \text{diagram with loop} + \dots \right) \times \left( \text{diagram with loop} + \dots \right) *$$

Infrared Div.

$$\frac{c_{-2}}{\epsilon_{\text{IR}}^2} + \frac{c_{-1}}{\epsilon_{\text{IR}}}$$

*Kinoshita-Lee-Nauenberg theorem*

Ultraviolet Div.  $\frac{a}{\epsilon_{\text{UV}}}$

Infrared Div

$$-\frac{c_{-2}}{\epsilon_{\text{IR}}^2} - \frac{c_{-1}}{\epsilon_{\text{IR}}}$$



# ANATOMY

$$\sigma_{pp \rightarrow e^+ e^-}^{\text{NLO}} =$$

$$\int_2 \left| \text{[Diagram 1]} + \dots \right|^2 + \int_3 \left| \text{[Diagram 2]} + \dots \right|^2$$

Diagram 1: A tree-level diagram for \$pp \to e^+e^-\$ via a \$Z\$ boson. Two incoming quark lines (1 and 2) meet at a vertex, exchange a \$Z\$ boson, and then split into two outgoing lepton lines (3 and 4). Diagram 2: A tree-level diagram for \$pp \to e^+e^- + g\$ via a \$Z\$ boson. Two incoming quark lines (1 and 2) meet at a vertex, exchange a \$Z\$ boson, and then split into two outgoing lepton lines (3 and 4) and one outgoing gluon line (5).

$$+ \int_2 \left( \text{[Diagram 1 with loop]} + \dots \right) \times \left( \text{[Diagram 1]} + \dots \right) *$$

Diagram 1 with loop: A tree-level diagram for \$pp \to e^+e^- + g\$ via a \$Z\$ boson, but with a loop of quarks (1 and 2) and a gluon (5) attached to the quark lines.

Infrared Div.  
 $\frac{c_{-2}}{\epsilon_{\text{IR}}^2} + \frac{c_{-1}}{\epsilon_{\text{IR}}}$

*Kinoshita-Lee-Nauenberg theorem*

Ultraviolet Div.  $\frac{a}{\epsilon_{\text{UV}}}$   
 Renormalization!

Infrared Div.  
 $-\frac{c_{-2}}{\epsilon_{\text{IR}}^2} - \frac{c_{-1}}{\epsilon_{\text{IR}}}$





# ISSUES TO BE ADDRESSED @ NLO

- Tree-level ME: **MadGraph**
- Resolved phase-space integration: **MadEvent**
- Unresolved phase-space integration: **MadFKS**
- Loop ME: **MadLoop**
  - Amplitude: **ALOHA+MadLoop**
  - Loop integration: **OPP+TIR**
- Renormalization: **FeynRules->UFO->MadLoop**

# ISSUES TO BE ADDRESSED @ NLO+PS

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**LO**

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**NLO**

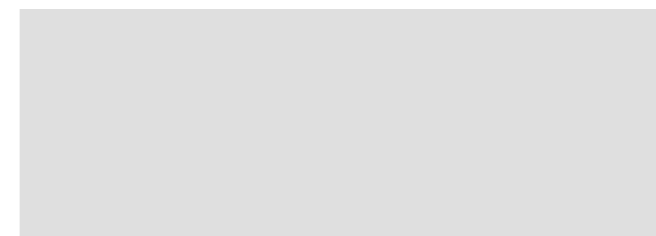
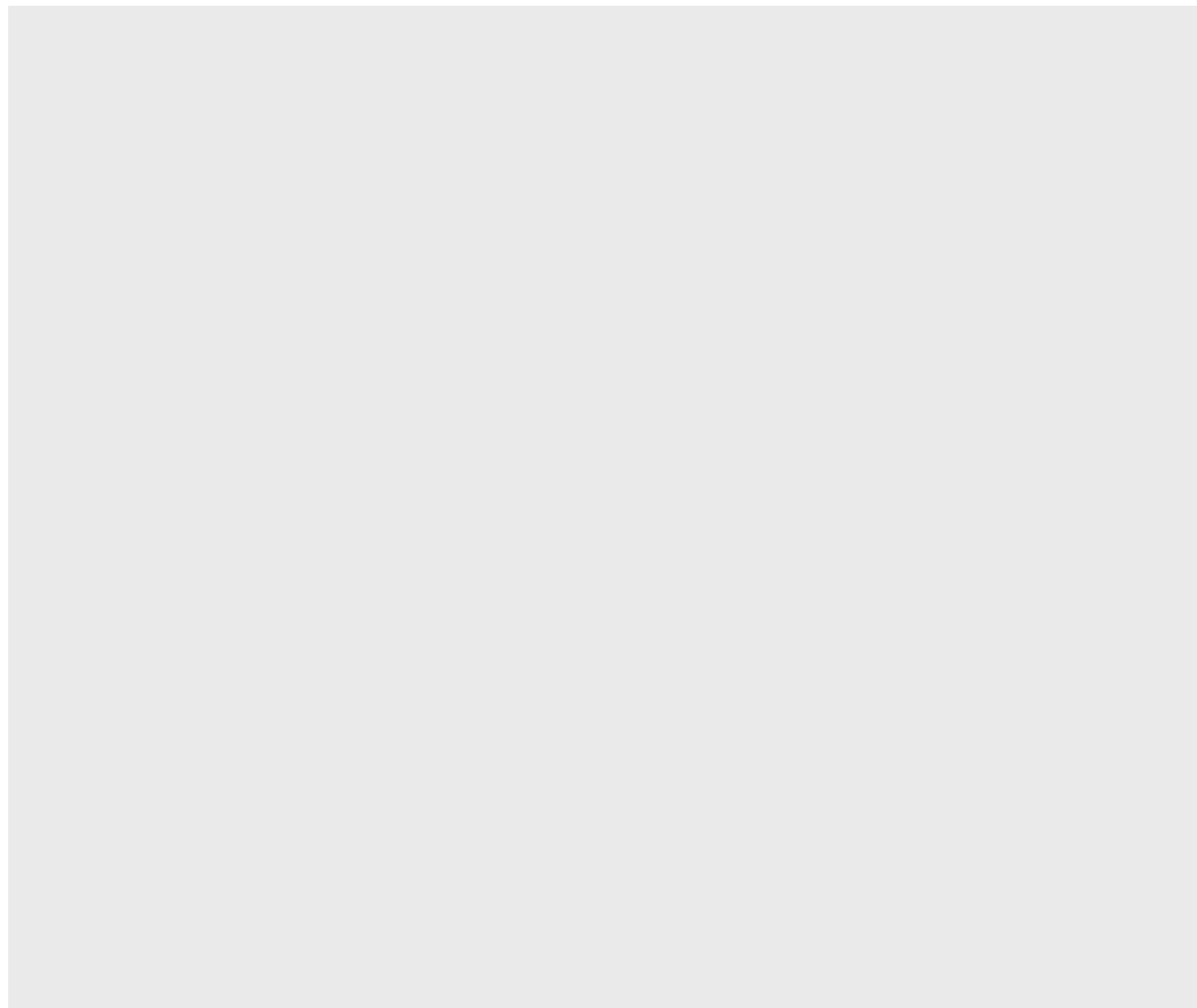
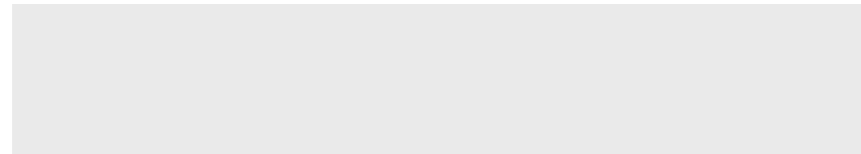
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**NLO+PS**

# JOINT EFFORTS FOR **AUTOMATION** AT NLO



Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, HSS, Stelzer, Torrielli, Zaro (JHEP'2014)





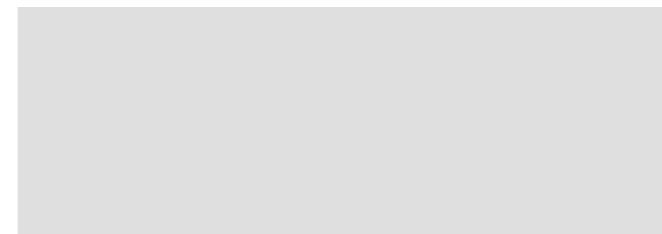
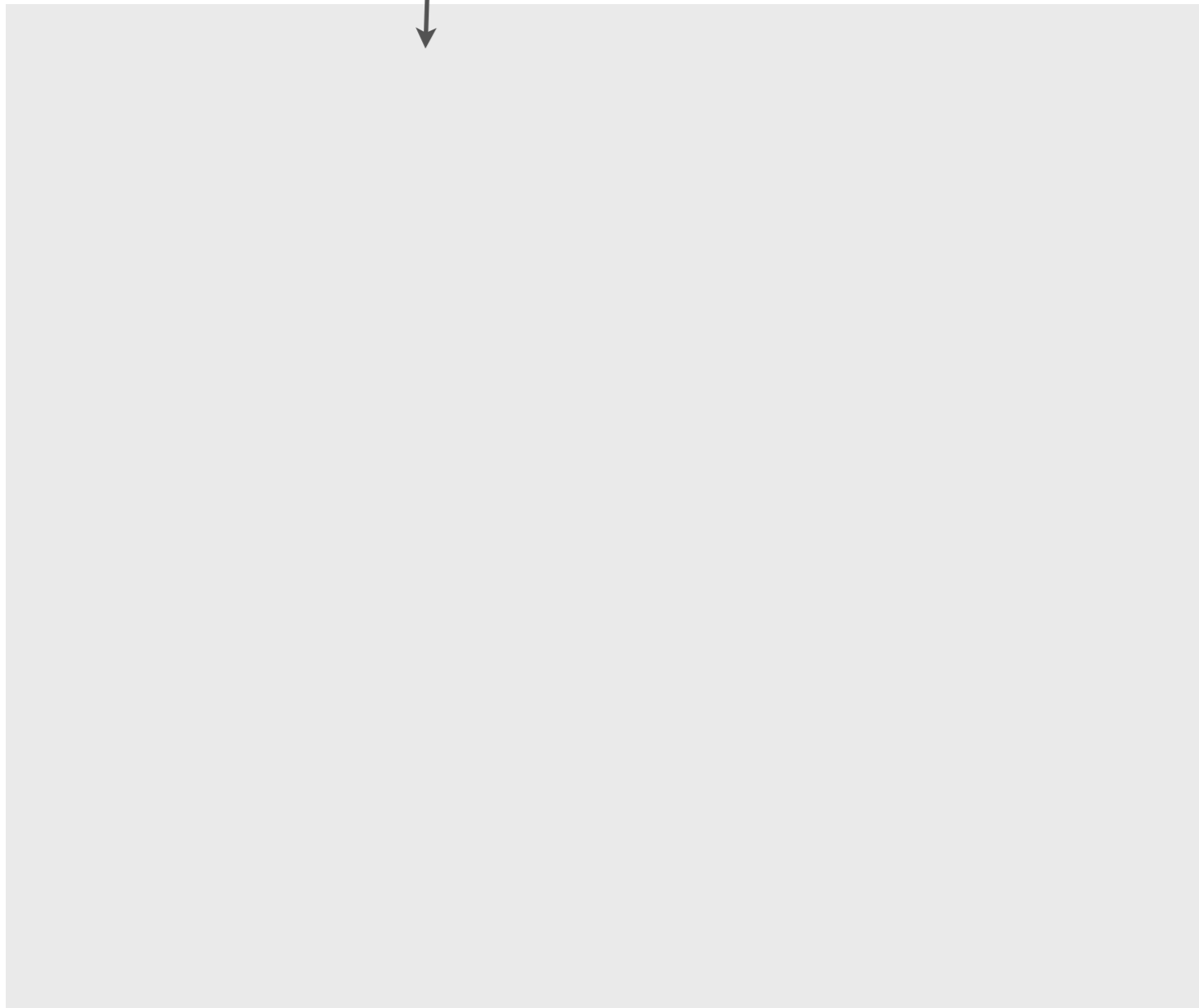
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FeynRules

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ALOHA

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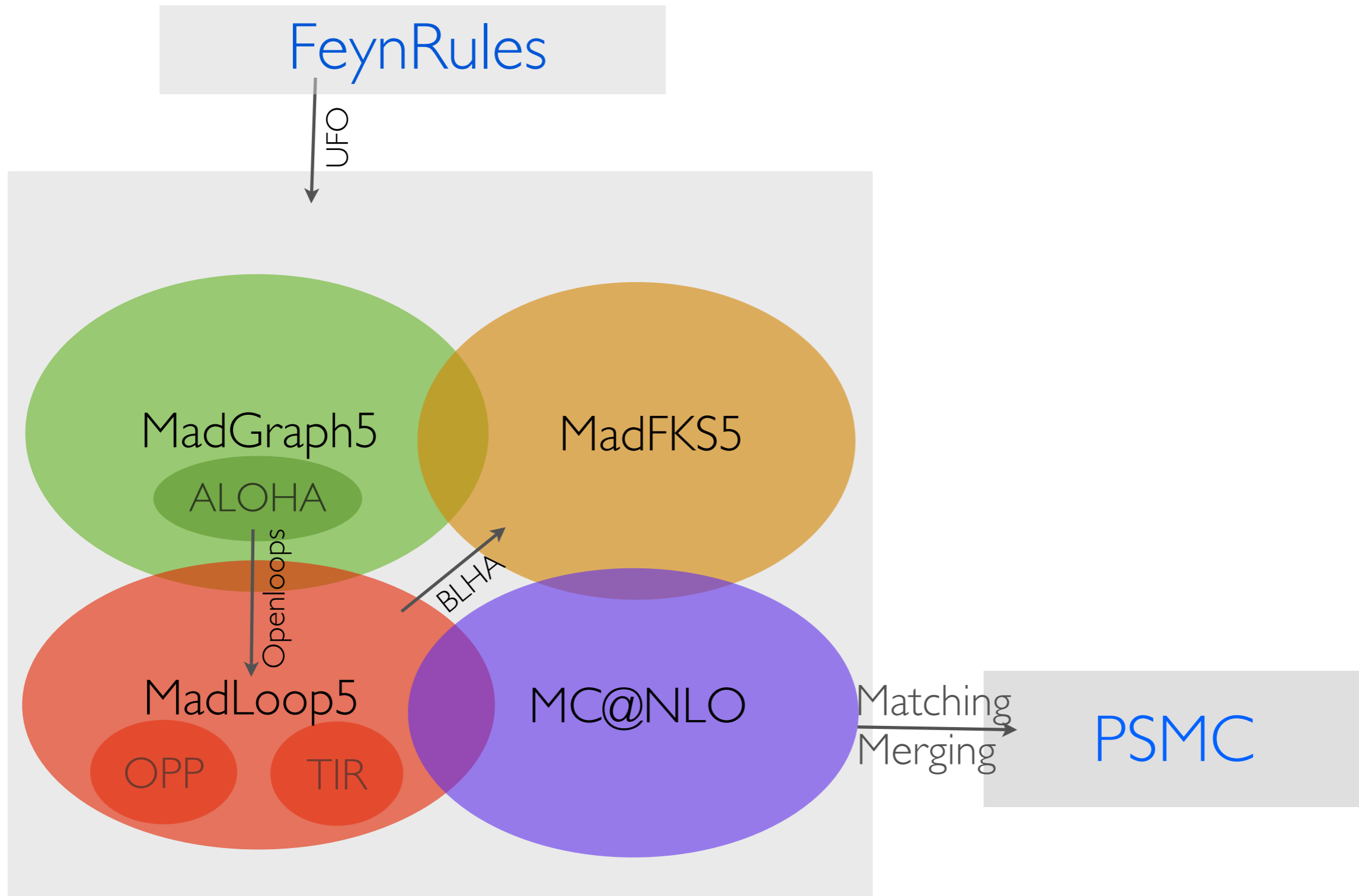
MadFKS5

BLHA

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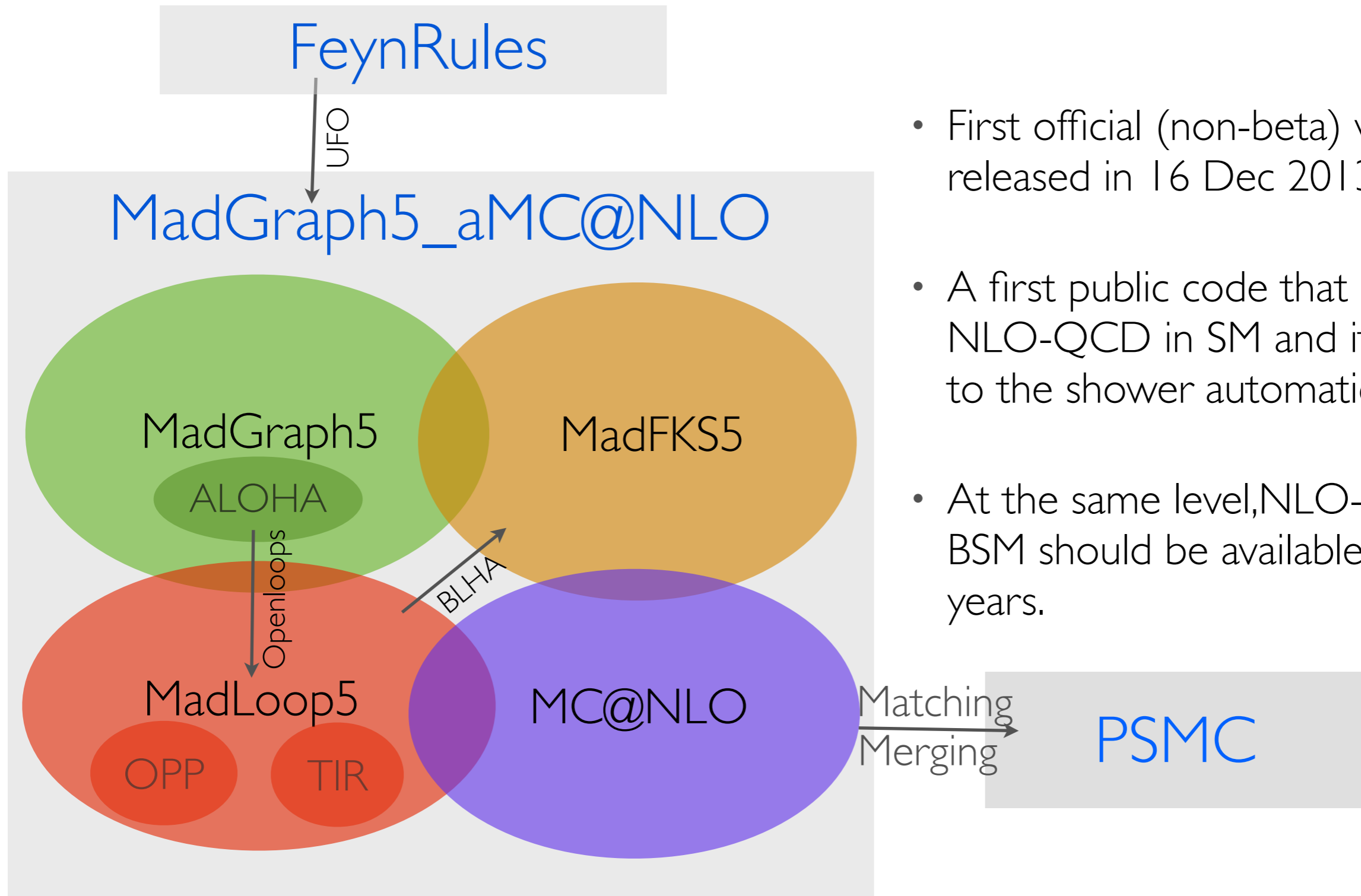
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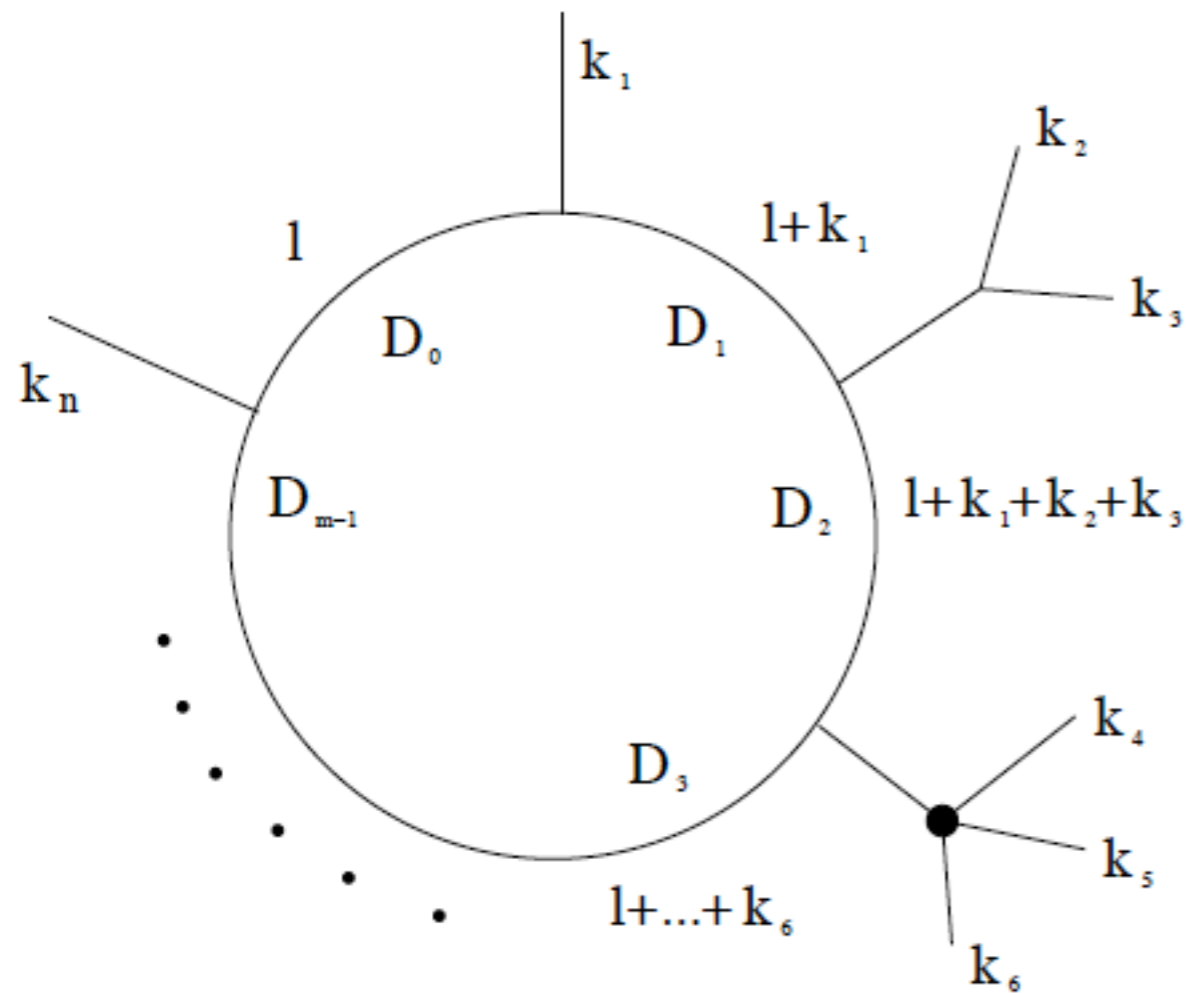
Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, HSS, Stelzer, Torrielli, Zaro (JHEP'2014)



- First official (non-beta) version was released in 16 Dec 2013.
- A first public code that provides NLO-QCD in SM and its interface to the shower automatically.
- At the same level, NLO-EW and BSM should be available in recent years.



# A GENERAL LOOP INTEGRAL



- Consider a  $m$ -point loop diagram with  $n$  external momenta.

- The integral is

$$\int d^{(4-2\epsilon)} l \frac{N(l)}{D_0 D_1 D_2 \cdots D_{m-1}}$$

$$D_i = (l + p_i)^2 - m_i^2$$

# A GENERAL LOOP INTEGRAL

$$\begin{aligned}
 & \int d^{(4-2\epsilon)} \frac{N(l)}{D_0 D_1 D_2 \cdots D_{m-1}} = \\
 & \sum_{0 \leq i_0 < i_1 < i_2 < i_3 \leq m-1} d_{i_0 i_1 i_2 i_3} \mathcal{I}_0(i_0 i_1 i_2 i_3) + \\
 & \sum_{0 \leq i_0 < i_1 < i_2 \leq m-1} c_{i_0 i_1 i_2} \mathcal{I}_0(i_0 i_1 i_2) + \\
 & \sum_{0 \leq i_0 < i_1 \leq m-1} b_{i_0 i_1} \mathcal{I}_0(i_0 i_1) + \\
 & \sum_{0 \leq i_0 \leq m-1} a_{i_0} \mathcal{I}_0(i_0) + \\
 & R,
 \end{aligned}$$

- Integral can be reduced to a minimal basis that was known.
- Rational term R is in general process dependent.

$$\mathcal{I}_0(i_0 i_1 i_2 i_3) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0} D_{i_1} D_{i_2} D_{i_3}},$$

$$\mathcal{I}_0(i_0 i_1 i_2) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0} D_{i_1} D_{i_2}},$$

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$$\mathcal{I}_0(i_0) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0}}.$$

# A GENERAL LOOP INTEGRAL

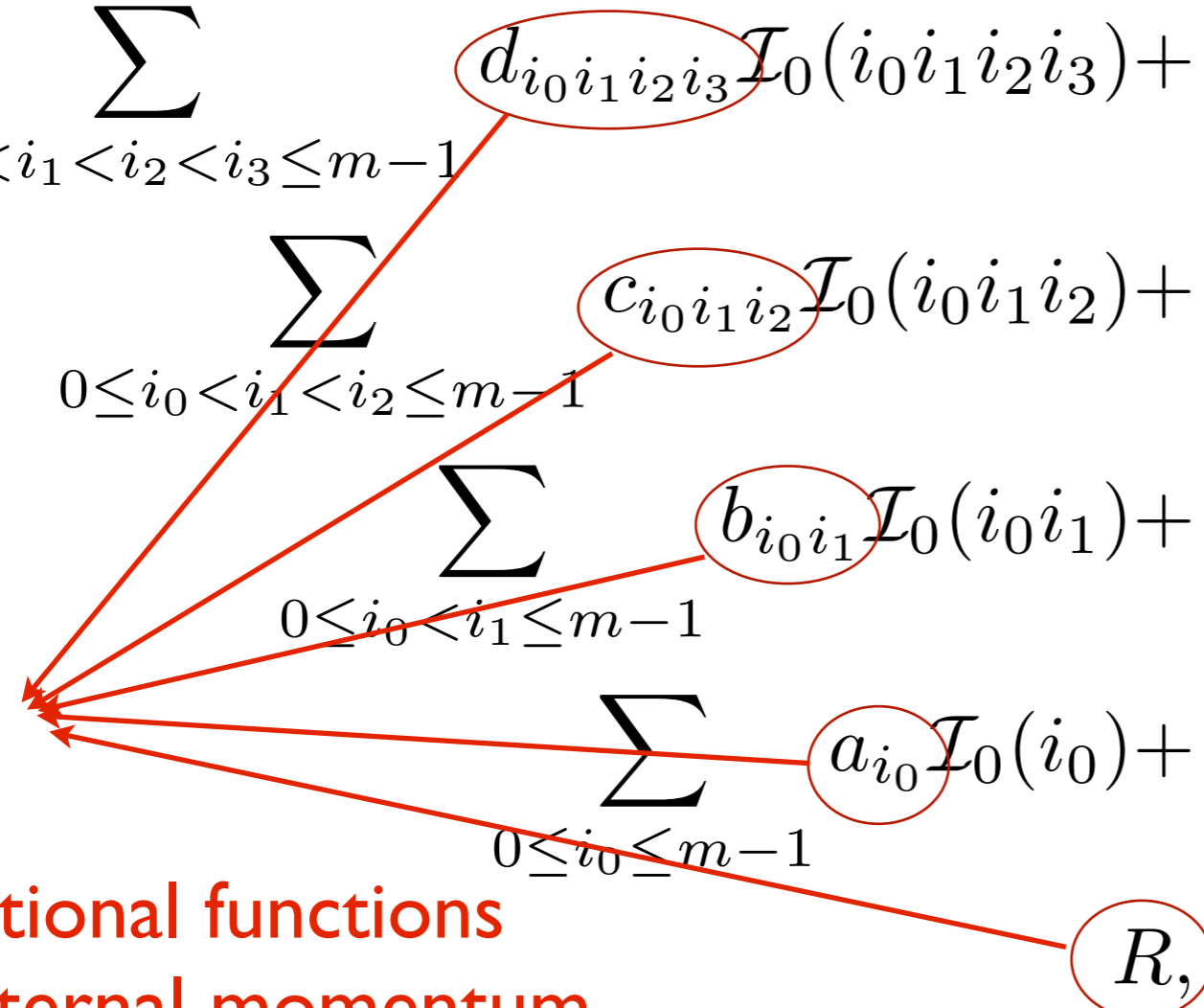
$$\int d^{(4-2\epsilon)} \frac{N(l)}{D_0 D_1 D_2 \cdots D_{m-1}} =$$

$$\sum_{0 \leq i_0 < i_1 < i_2 < i_3 \leq m-1} d_{i_0 i_1 i_2 i_3} \mathcal{I}_0(i_0 i_1 i_2 i_3) +$$

$$\sum_{0 \leq i_0 < i_1 < i_2 \leq m-1} c_{i_0 i_1 i_2} \mathcal{I}_0(i_0 i_1 i_2) +$$

$$\sum_{0 \leq i_0 < i_1 \leq m-1} b_{i_0 i_1} \mathcal{I}_0(i_0 i_1) +$$

$$\sum_{0 \leq i_0 \leq m-1} a_{i_0} \mathcal{I}_0(i_0) +$$

$$R,$$


**Rational functions  
of external momentum  
and masses**

- Integral can be reduced to a minimal basis that was known.
- Rational term R is in general process dependent.

$$\mathcal{I}_0(i_0 i_1 i_2 i_3) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0} D_{i_1} D_{i_2} D_{i_3}},$$

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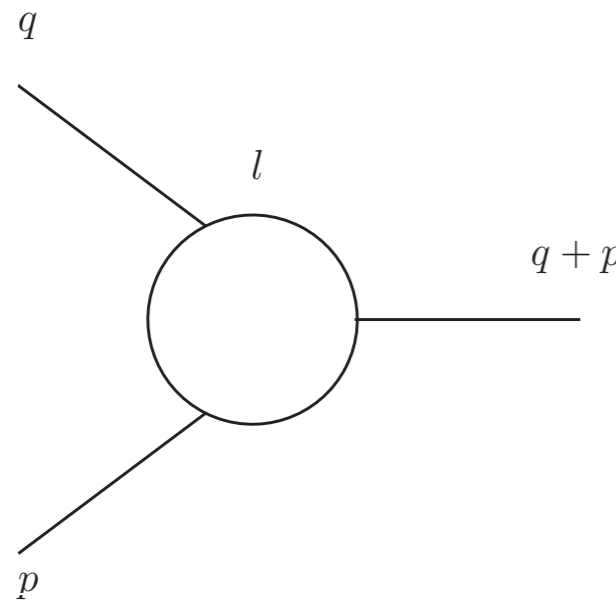
$$\mathcal{I}_0(i_0 i_1) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0} D_{i_1}},$$

$$\mathcal{I}_0(i_0) \equiv \int d^{(4-2\epsilon)} l \frac{1}{D_{i_0}}.$$

# EXAMPLE: A LOOP INTEGRAL

Passarino, Veltman (NPB'1979)

- Let us see an example:

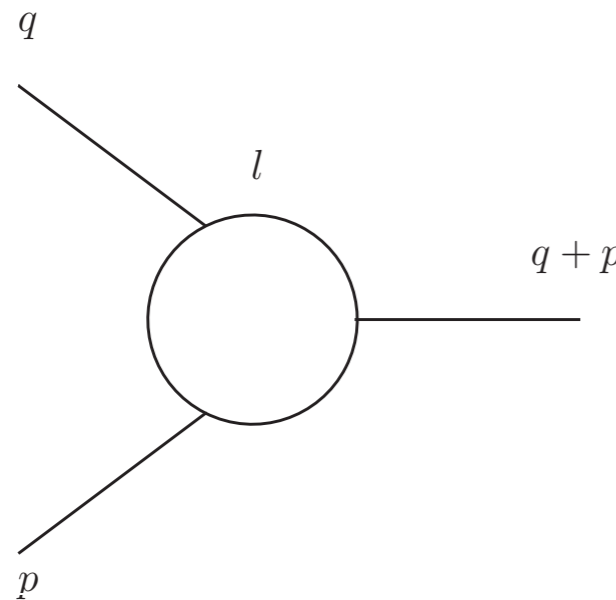


$$= \int d^{(4-2\epsilon)}l \frac{1}{(2\pi)^{(4-2\epsilon)}} \frac{l^\mu}{(l^2 - m_1^2) \left( (l+p)^2 - m_2^2 \right) \left( (l+q)^2 - m_3^2 \right)}$$

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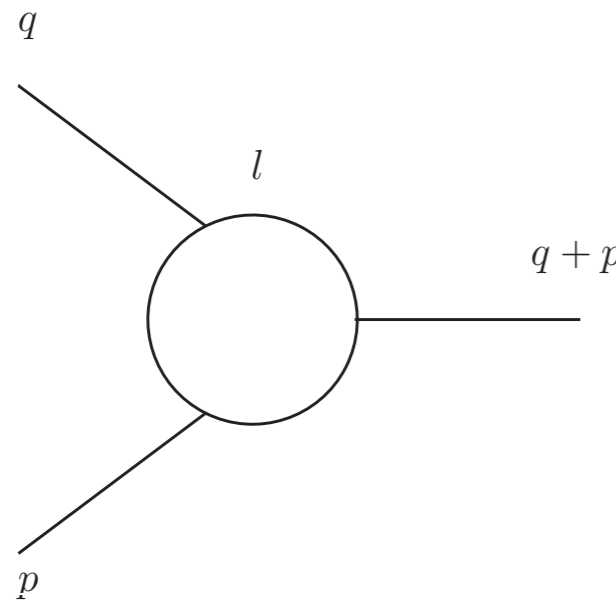
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- Try to solve the equation by contracting the external momenta

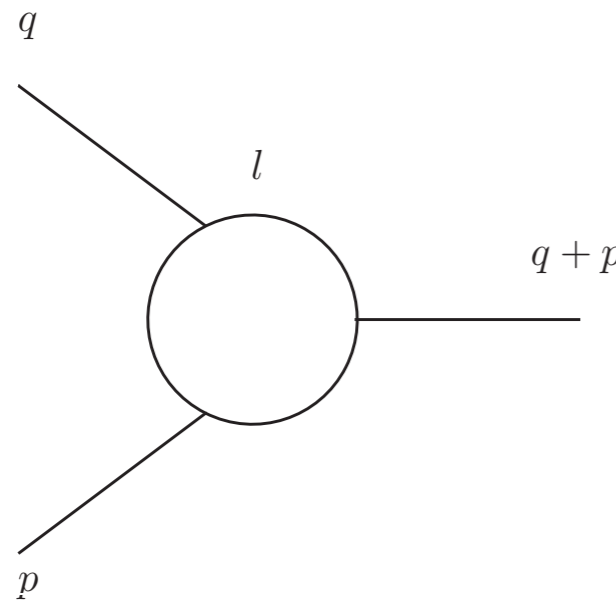
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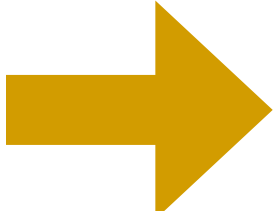
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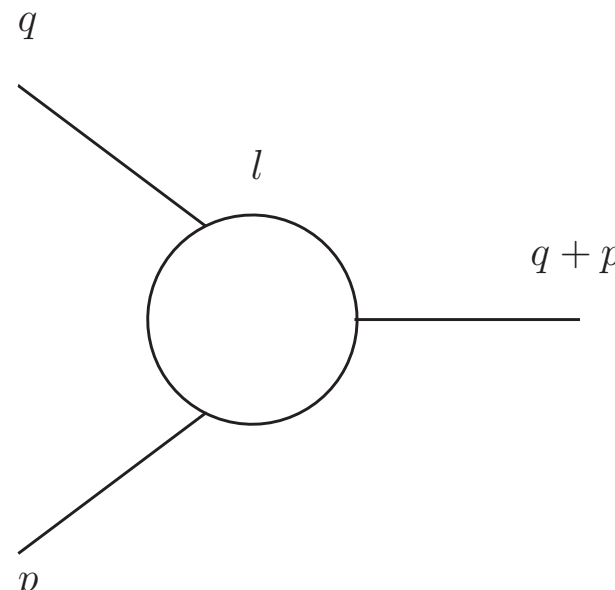


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## Gram Determination

- Due to the Lorentz invariant, integral must be proportional to

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Passarino, Veltman (NPB'1979)

- The numerator can be decomposed into denominators

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 &= \int d^{(4-2\epsilon)} l \frac{1}{(2\pi)^{(4-2\epsilon)}} \frac{[(l+p)^2 - m_2^2] - [l^2 - m_1^2] + [-m_1^2 + m_2^2 - p^2]}{(l^2 - m_1^2) ((l+p)^2 - m_2^2) ((l+q)^2 - m_3^2)}
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 &= \frac{1}{(2\pi)^{(4-2\epsilon)}} [\mathcal{I}_0(13) - \mathcal{I}_0(23) + (-m_1^2 + m_2^2 - p^2) \mathcal{I}_0(123)]
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- Similarly
- The scalar integrals are known: **QCDLoop** [Ellis, Zanderighi (JHEP'2008)],  
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 &= \frac{1}{(2\pi)^{(4-2\epsilon)}} \left[ \mathcal{I}_0(12) - \mathcal{I}_0(23) + (-m_2^2 + m_1^2 - q^2) \mathcal{I}_0(123) \right]
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- The scalar integrals are known: **QCDLoop** [Ellis, Zanderighi (JHEP'2008)], **OneLoop** [Hameren (CPC'2011)]
- An example (an exercise for interested student):

$$\begin{aligned}
 \mathcal{I}_0(12) &\equiv \int d^{(4-2\epsilon)}l \frac{1}{(l^2 - m_1^2) \left( (l+p)^2 - m_2^2 \right)} \\
 &= \frac{i\pi^2}{(2\pi\mu_R)^{2\epsilon}} \left( \frac{1}{\epsilon} - \gamma_E + 2 - \log \frac{p^2}{4\pi\mu_R^2} + \sum_{i=1}^2 \gamma_i \log \frac{\gamma_i - 1}{\gamma_i} - \log \gamma_i - 1 \right) \\
 \gamma_{1,2} &\equiv \frac{p^2 - m_2^2 + m_1^2 \pm \sqrt{(p^2 - m_2^2 + m_1^2)^2 - 4p^2 m_1^2}}{2p^2}
 \end{aligned}$$

# EXAMPLE: A LOOP INTEGRAL

Passarino, Veltman (NPB'1979)

- Solve the equation

=

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- Two disadvantages:

- It requires the determination of Gram matrix is not zero (need to improve **stability**)
- The expression of the coefficients can be complicated (need to improve **speed**)

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- Three solutions:

- improved tensor integral reduction (e.g. Denner, Dittmaier (NPB'2006))
- integrand reduction (OPP reduction refer to Marco's talk on Wednesday)
- generalized unitarity reduction (I will not talk about it, which is not used in MG5)

**known**



# ONE SLIDE ON INTEGRAND REDUCTION

Ossola, Papadopoulos, Pittau (NPB'2006)

- The numerator (before integration) can be decomposed into:

$$\begin{aligned}
 N(l) = & \sum_{i_0 < i_1 < i_2 < i_3}^{m-1} \left[ d_{i_0 i_1 i_2 i_3} + \tilde{d}_{i_0 i_1 i_2 i_3}(l) \right] \prod_{i \neq i_0, i_1, i_2, i_3}^{m-1} D_i \\
 & + \sum_{i_0 < i_1 < i_2}^{m-1} \left[ c_{i_0 i_1 i_2} + \tilde{c}_{i_0 i_1 i_2}(l) \right] \prod_{i \neq i_0, i_1, i_2}^{m-1} D_i \\
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To solve the OPP reduction, choosing special values for the loop momenta helps a lot

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For example, choosing  $l$  such that

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sets all the terms in this equation to zero except the **first** line

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**Recently, we have CutTools, Samurai, Ninja working in MadGraph5\_aMC@NLO**

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# ONE SLIDE ON TENSOR INTEGRAL REDUCTION REDUCTION

- Instead, one can also write the numerator into

$$N(l) = \sum_{r=0}^{r_{\max}} c_{\mu_1 \dots \mu_r} l^{\mu_1} \dots l^{\mu_r}$$

- Tensor integral reduction tries to work in

$$\int d^{(4-2\epsilon)} l \frac{N(l)}{D_0 D_1 D_2 \dots D_{m-1}} = \sum_{r=0}^{r_{\max}} c_{\mu_1 \dots \mu_r} \mathcal{I}^{\mu_1 \dots \mu_r}$$

- Tensor integral reduction tries to reduce  $\{ [g]^1 [p_0]^0 [p_1]^2 \}^{\mu_1 \dots \mu_4} \equiv g^{\mu_1 \mu_2} p_1^{\mu_3} p_1^{\mu_4} + g^{\mu_1 \mu_3} p_1^{\mu_2} p_1^{\mu_4} + g^{\mu_1 \mu_4} p_1^{\mu_2} p_1^{\mu_3}$

$$\begin{aligned} \mathcal{I}^{\mu_1 \dots \mu_r} &\equiv \int d^{(4-2\epsilon)} l \frac{l^{\mu_1} \dots l^{\mu_r}}{D_0 D_1 D_2 \dots D_{m-1}} \\ &= \sum_{2j+i_0+i_1+\dots+i_{m-1}=r} \{ [g]^j [p_0]^{i_0} \dots [p_{m-1}]^{i_{m-1}} \}^{\mu_1 \dots \mu_r} \mathcal{I}_{j i_0 \dots i_{m-1}} \end{aligned}$$

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- Te **We have PJFry++, IREGI, Golem95 working in MadGraph5\_aMC@NLO**

$$J \quad D_0 D_1 D_2 \dots D_{m-1} \quad \sum_{r=0}$$

- Tensor integral reduction tries to reduce  $\{ [g]^1 [p_0]^0 [p_1]^2 \}^{\mu_1 \dots \mu_4} \equiv g^{\mu_1 \mu_2} p_1^{\mu_3} p_1^{\mu_4} + g^{\mu_1 \mu_3} p_1^{\mu_2} p_1^{\mu_4} + g^{\mu_1 \mu_4} p_1^{\mu_2} p_1^{\mu_3}$

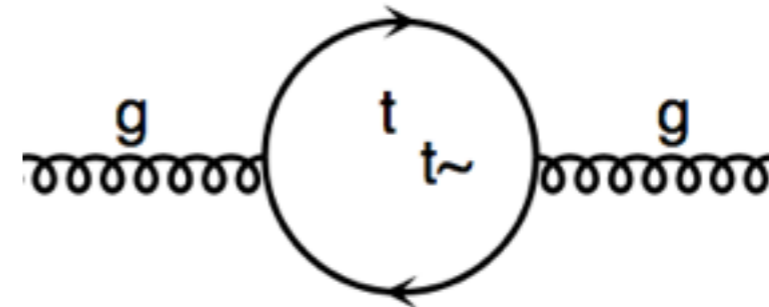
$$\mathcal{I}^{\mu_1 \dots \mu_r} \equiv \int d^{(4-2\epsilon)} l \frac{l^{\mu_1} \dots l^{\mu_r}}{D_0 D_1 D_2 \dots D_{m-1}}$$

$$= \sum_{2j+i_0+i_1+\dots+i_{m-1}=r} \{ [g]^j [p_0]^{i_0} \dots [p_{m-1}]^{i_{m-1}} \}^{\mu_1 \dots \mu_r} \mathcal{I}_{j i_0 \dots i_{m-1}}$$

# R2

- The numerator  $N(l)$  is a complicated function (Clifford algebra etc) in  $d$ - and 4-dimensional quantities.
- It is usually conv. to work  $N(l)$  in 4-dim  $\rightarrow$  super useful for numerical calculations.
- We need a special rational term R2 !

- For example, gluon SE:



$$N(l) = -\frac{\alpha_S}{(2\pi)^3} \delta_{ab} \text{Tr}[\gamma^\mu (\not{l} + m_t) \gamma^\nu (\not{l} + \not{p} + m_t)] \varepsilon_\mu \varepsilon_\nu$$

- Dirac algebra gives the (d-4) numerator

$$\tilde{N}(\tilde{l}) = 4 \frac{\alpha_S}{(2\pi)^3} \delta_{ab} g^{\mu\nu} \tilde{l}^2 \varepsilon_\mu \varepsilon_\nu$$

- With the integration

$$\int d^{(4-2\epsilon)} l \frac{\tilde{l}^2}{(l^2 - m_t^2)((l+p)^2 - m_t^2)} = -\frac{i\pi^2}{2} \left( 2m_t^2 - \frac{p^2}{3} \right) + \mathcal{O}(\epsilon)$$

- The corresponding R2 term

$$R_2 = -\frac{i\alpha_S}{4\pi} \left( 2m_t^2 - \frac{p^2}{3} \right) \delta_{ab} g^{\mu\nu} \varepsilon_\mu \varepsilon_\nu$$



# R2

Draggiotis, Garzelli, Papadopoulos, Pittau (JHEP'09); HSS, Zhang, Chao (JHEP'11)

- It was proven that R2 is only UV related, hence universal (i.e. model dependent only), which can be derived by R2 counterterm Feynman rules and should be derived once for all in each model.

# R2

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- It was proven that R2 is only UV related, hence universal (i.e. model dependent only), which can be derived by R2 counterterm Feynman rules and should be derived once for all in each model.

$$\begin{aligned}
 G_\mu^a \xrightarrow{p} \text{---} \bullet \text{---} G_\nu^b &= \text{Vert}(G_\mu^a, G_\nu^b) \\
 Q_l^i \xrightarrow{p} \text{---} \bullet \text{---} \bar{Q}_m^j &= \text{Vert}(Q_l^i, \bar{Q}_m^j)
 \end{aligned}$$

$$\text{Vert}(G_\mu^a, G_\nu^b) = \frac{ig_s^2 N_c}{48\pi^2} \delta^{ab} \left[ \frac{p^2}{2} g_{\mu\nu} + \lambda_{HV} (g_{\mu\nu} p^2 - p_\mu p_\nu) + \sum_Q \frac{p^2 - 6m_Q^2}{N_c} g_{\mu\nu} \right]$$

$$\text{Vert}(Q_l^i, \bar{Q}_m^j) = \frac{ig_s^2}{16\pi^2} \frac{N_c^2 - 1}{2N_c} \delta^{ij} \delta_{lm} (-\not{p} + 2m_{Q_l}) \lambda_{HV}.$$

$$\begin{aligned}
 G_\mu^a \xrightarrow{p_1} \text{---} \bullet \begin{cases} \nearrow G_\nu^b \\ \searrow G_\rho^c \end{cases} &= \text{Vert}(G_\mu^a, G_\nu^b, G_\rho^c)
 \end{aligned}$$

$$\text{Vert}(G_\mu^a, G_\nu^b, G_\rho^c) = -\frac{g_s^3 N_c}{48\pi^2} \left( \frac{7}{4} + \lambda_{HV} + \frac{2N_f}{N_c} \right) f^{abc} V_{\mu\nu\rho}(p_1, p_2, p_3)$$

$$V_{\mu\nu\rho}(p_1, p_2, p_3) = g_{\mu\nu}(p_2 - p_1)_\rho + g_{\nu\rho}(p_3 - p_2)_\mu + g_{\rho\mu}(p_1 - p_3)_\nu.$$

$$\begin{aligned}
 G_\mu^a \text{---} \bullet \begin{cases} \nearrow Q_l^i \\ \searrow \bar{Q}_m^j \end{cases} &= \text{Vert}(G_\mu^a, Q_l^i, \bar{Q}_m^j)
 \end{aligned}$$

$$\text{Vert}(G_\mu^a, Q_l^i, \bar{Q}_m^j) = \delta_{lm} \frac{ig_s^3}{16\pi^2} T_{ji}^a \frac{N_c^2 - 1}{2N_c} \gamma_\mu (1 + \lambda_{HV})$$

$$\text{Vert}(G_\mu^a, G_\nu^b, G_\rho^c, G_\sigma^d) = \frac{ig_s^4}{48\pi^2} (C_1 g_{\mu\nu} g_{\rho\sigma} + C_2 g_{\mu\rho} g_{\nu\sigma} + C_3 g_{\mu\sigma} g_{\nu\rho}),$$

$$\begin{aligned}
 G_\nu^b \text{---} \bullet \begin{cases} \nearrow G_\rho^c \\ \searrow G_\mu^a \\ \nearrow G_\mu^a \\ \searrow G_\sigma^d \end{cases} &= \text{Vert}(G_\mu^a, G_\nu^b, G_\rho^c, G_\sigma^d)
 \end{aligned}$$

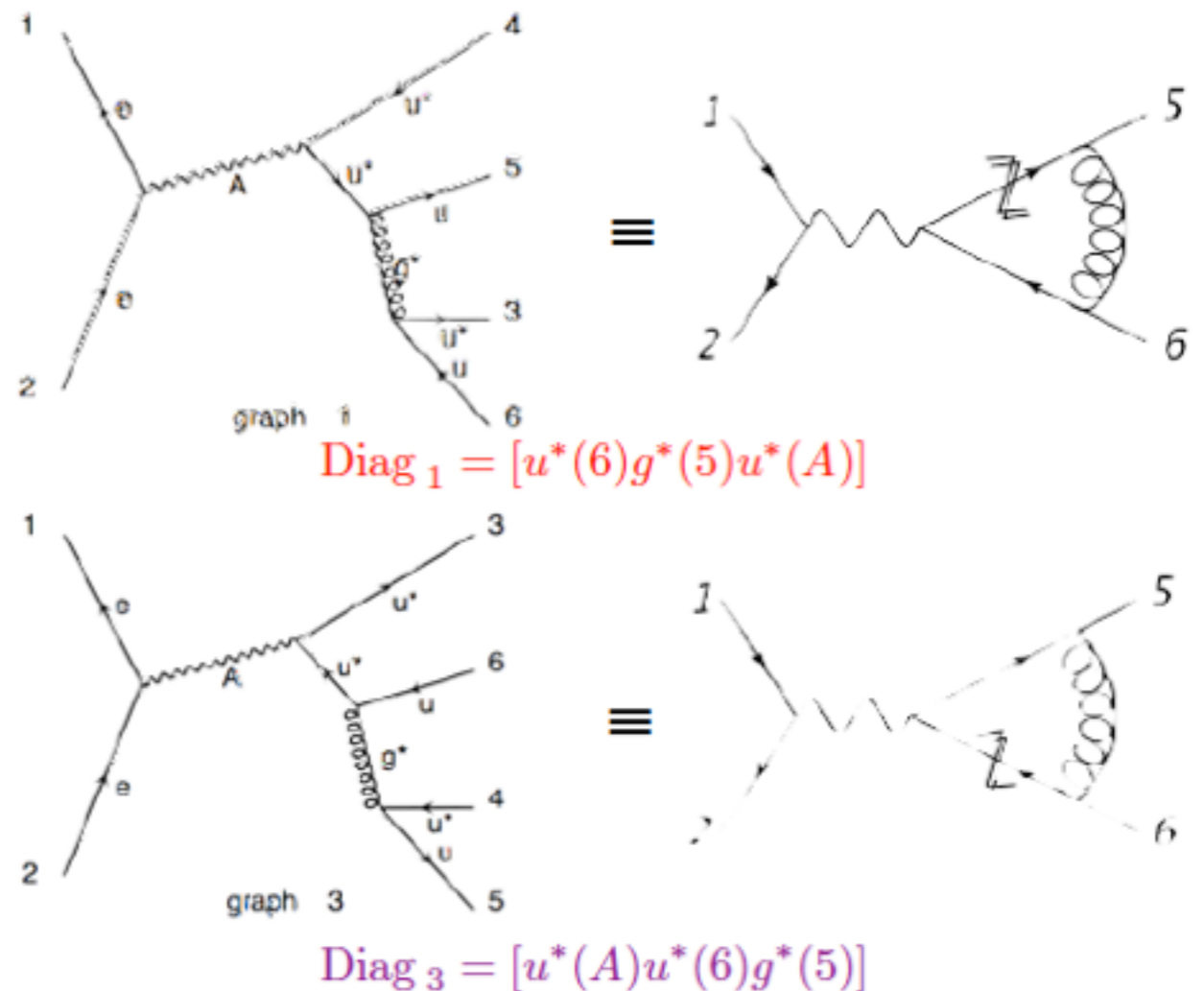
$$\begin{aligned}
 C_1 &= \text{Tr}(\{T^a, T^b\}\{T^c, T^d\}) (5N_c + 2\lambda_{HV} N_c + 6N_f) \\
 &\quad - (\text{Tr}(T^a T^c T^b T^d) + \text{Tr}(T^a T^d T^b T^c)) (12N_c + 4\lambda_{HV} N_c + 10N_f) \\
 &\quad - (\delta^{ab} \delta^{cd} + \delta^{ac} \delta^{bd} + \delta^{ad} \delta^{bc}), \quad C_2 = C_1(b \leftrightarrow c) \quad C_3 = C_1(b \leftrightarrow d)
 \end{aligned}$$

# MADLOOP

Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau (JHEP'11)

- Instead of using an external tool for loop diagram generation, we recycle **MadGraph** algorithms for tree-level diagram generation.
- A loop diagrams with the loop cut open has two extra external particles. Consider  $e^+e^- \rightarrow u u\bar{u}$  (**loop particle** are in red). **MadLoop** will generate 8 L-cut diagrams. Here are two of them:

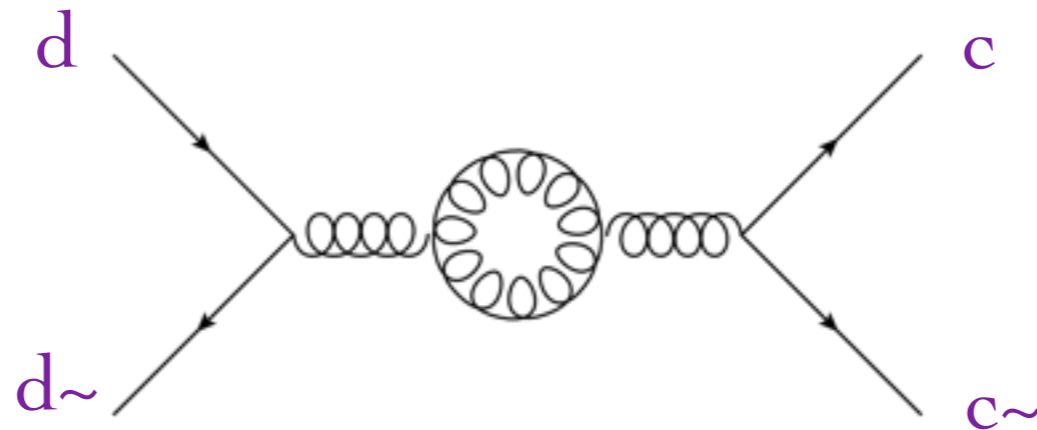
- All diagrams with two extra particles generated and the ones that are redundant need be filtered out
- Each diagram gets an unique tag: any mirror and/or cyclic permutations of tags of diagrams already in the set are taken out
- Additional filter to eliminate tadpole and bubbles attached to external lines.



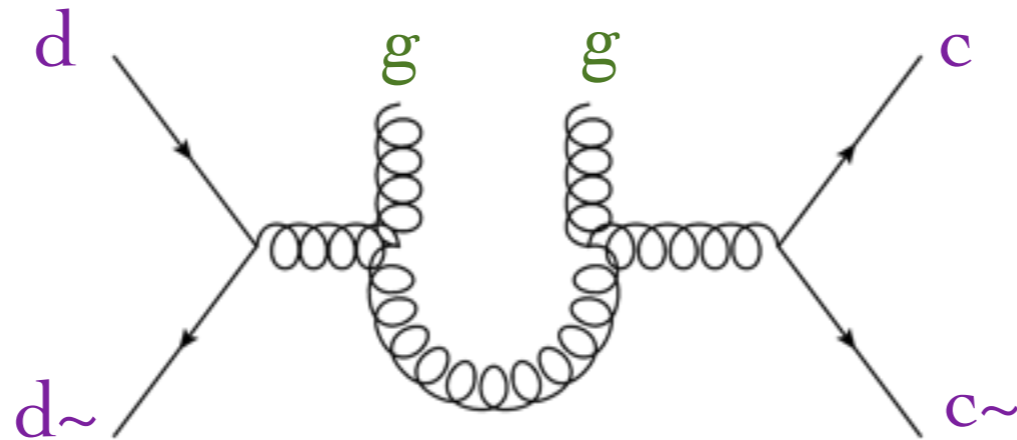
# MADLOOP

Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau (JHEP'11)

- It is clear though that  $d d^{\sim} \rightarrow c c^{\sim} u u^{\sim}$  will not get you this loop :



- For this one you necessarily need to generate the **born** process with the additional **two L-cut particles** being **gluons**!

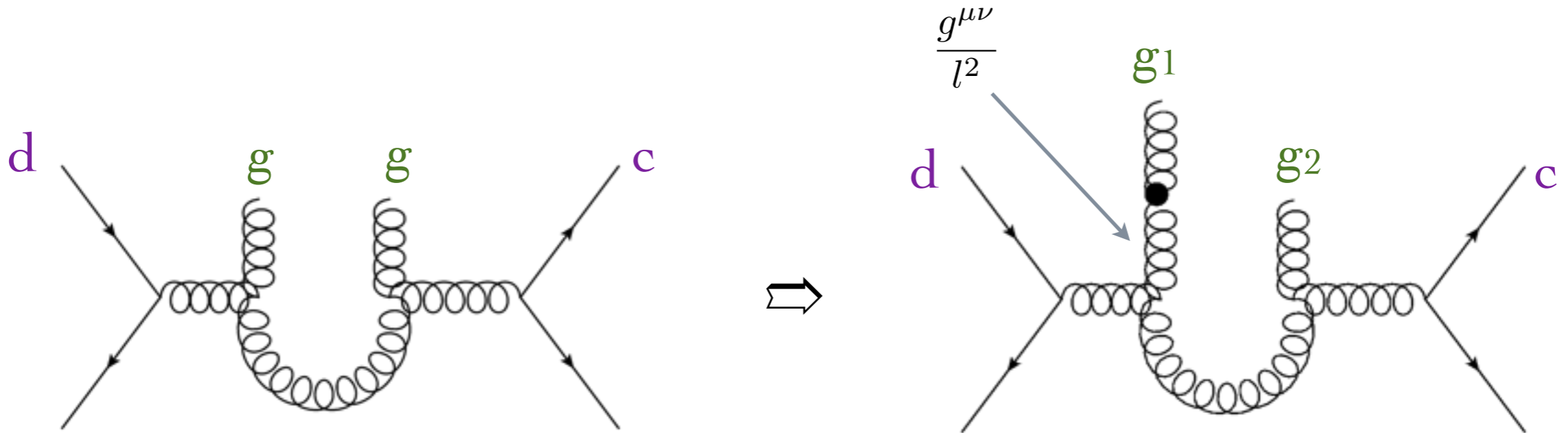


- Loops including a **u-quark** were already generated with  $d d^{\sim} \rightarrow c c^{\sim} u u^{\sim}$ , so you can speed up the  $d d^{\sim} \rightarrow c c^{\sim} g g$  generation forbidding **u** in the loop!

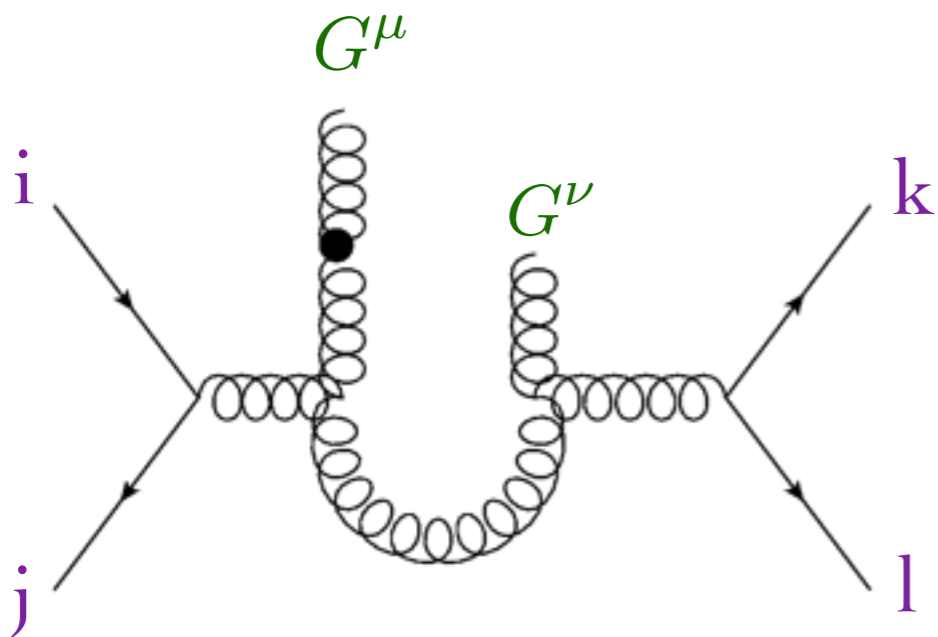
# MADLOOP

Hirschi, Frederix, Frixione, Garzelli, Maltoni, Pittau (JHEP'11)

- We want to use (modified) HELAS method



- Closing the Lorentz trace :



$$\delta^{\mu\nu} = \sum_{i=0}^4 \underbrace{\delta^{\mu i}}_{G^{\mu}} \underbrace{\delta^{i\nu}}_{G^{\nu}}$$

External Wavefunction for HELAS

# RENORMALIZATION

- Renormalization is a non-trivial task in principle.
- In QFT, renormalization is widely used to absorb (the divergence from) the high-momentum mode.
- The renormalization of some theories is quite well known, such as QCD (or the Standard Model).

# RENORMALIZATION

- Renormalization is a non-trivial task in principle.
- In QFT, renormalization is widely used to absorb (the divergence from) the high-momentum mode.
- The renormalization of some theories is quite well known, such as QCD (or the Standard Model).
- In general, the UV divergences should be absorbed by a redefinition of
  - the free parameters (such as mass, couplings, mixing angles etc

$$x_0 \rightarrow x + \delta x$$

- the fields

$$\phi_0 \rightarrow \left(1 + \frac{1}{2}\delta Z_{\phi\phi}\right)\phi + \sum_{\chi} \frac{1}{2}\delta Z_{\phi\chi}\chi$$







# EXAMPLE: RENORMALIZATION

- Coupling constant renormalization (match to PDF)
  - Keep scale dependence of massive mode to gluon self-energy
  - MSbar renormalize for massless mode to gluon self-energy

$$\delta g_s^{\overline{\text{MS}}} = \delta V_{q\bar{q}G}^{\overline{\text{MS}}} - \delta Z_q^{\overline{\text{MS}}} - \frac{\delta Z_g^{\text{ZS}}}{2}$$

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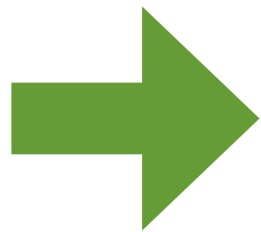
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- Renormalization with UV counterterm

$$\mathcal{L}_{Q\bar{Q}G} = \bar{Q}(i\not{\partial} - m_Q + g_s T^a \not{G})Q$$



$$\mathcal{L}_{Q\bar{Q}G} + \delta\mathcal{L}_{Q\bar{Q}G}^{\text{UV}} \quad \text{where}$$

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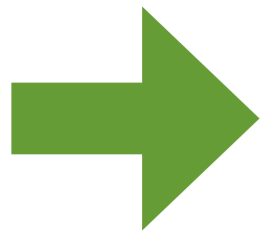
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Propagator



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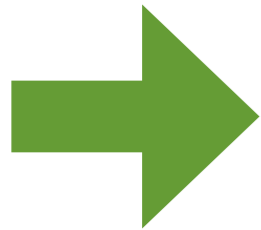
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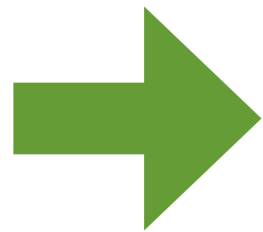
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UV Vertex

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# REAL SUBTRACTION

- Because of IR div, difficult to integrate real phase-space !
- Subtraction the IR piece by a constructed function  $S$

$$\int_3 \left( \underbrace{\left| \begin{array}{c} 2 \\ \swarrow \gamma^- \\ \text{---} \\ \downarrow \\ \text{---} \\ \swarrow \gamma^+ \\ 4 \\ \downarrow \\ \text{---} \\ \searrow \\ 1 \\ \swarrow \\ \text{---} \\ \downarrow \\ \text{---} \\ \searrow \\ 3 \\ \downarrow \\ \text{---} \\ \swarrow \\ 5 \end{array} \right|^2}_{\mathbf{R}} + \dots + \mathbf{S} \right) + \int_3 \mathbf{S}$$

- Requirement:
  - The IR singularity of  $\mathbf{R}$  and  $\mathbf{S}$  are completely same (i.e. local)
  - $\mathbf{S}$  is much easier to integrate analytically at least one particle's phase space for NLO computation.

*Details please refer to Marco's talk on Wednesday*

# REAL SUBTRACTION

Frixione, Kunszt, Signer (NPB'96); Frederix, Frixione, Maltoni, Stelzer (JHEP'09)

- MG5\_aMC used Frixione-Kunszt-Signer (FKS) subtraction of **S**
- The real IR singular form is

$$R \xrightarrow{\text{IR sing.}} \frac{1}{\chi_i} \frac{1}{1 - y_{ij}}$$

where  $\chi_i \equiv \frac{E_i}{\sqrt{\hat{s}}}$ ,  $y_{ij} \equiv \cos \theta_{ij}$

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$\chi_i \rightarrow 0$  **soft**

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↓

$y_{ij} \rightarrow 1$  **collinear**

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$$\int_3 R = \sum_{i,j} \int_3 S_{ij} R \quad \sum_{i,j} S_{ij} = 1$$

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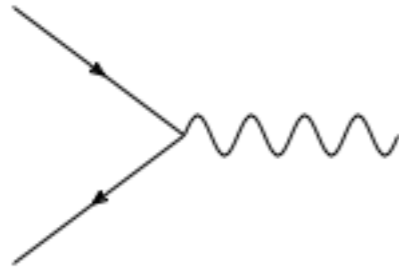
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$$\int_3 R = \sum_{i,j} \int_3 S_{ij} R \quad \sum_{i,j} S_{ij} = 1$$

- The real can be regulated as  $\sum_{i,j} \int_3 \left(\frac{1}{\chi_i}\right)_+ \left(\frac{1}{1 - y_{ij}}\right)_+ \chi_i (1 - y_{ij}) S_{ij} R$
- Soft counterterm is blind of spin, but the splitting kernel in collinear counterterm is dependent of spin/gauge/...

*Details please refer to Marco's talk on Wednesday*

# MATCHING TO PARTON SHOWER

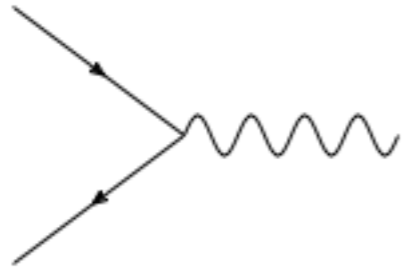


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Parton shower

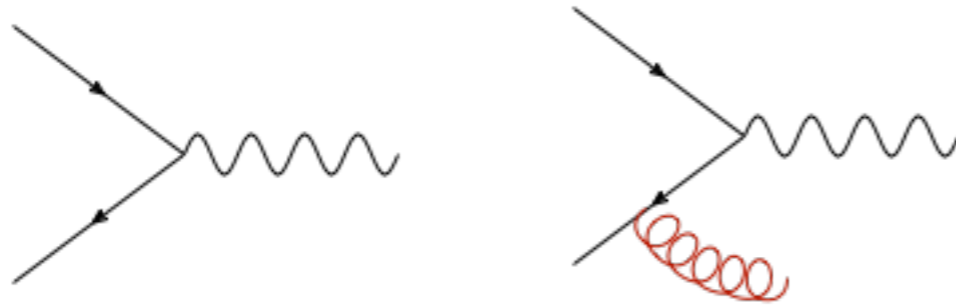


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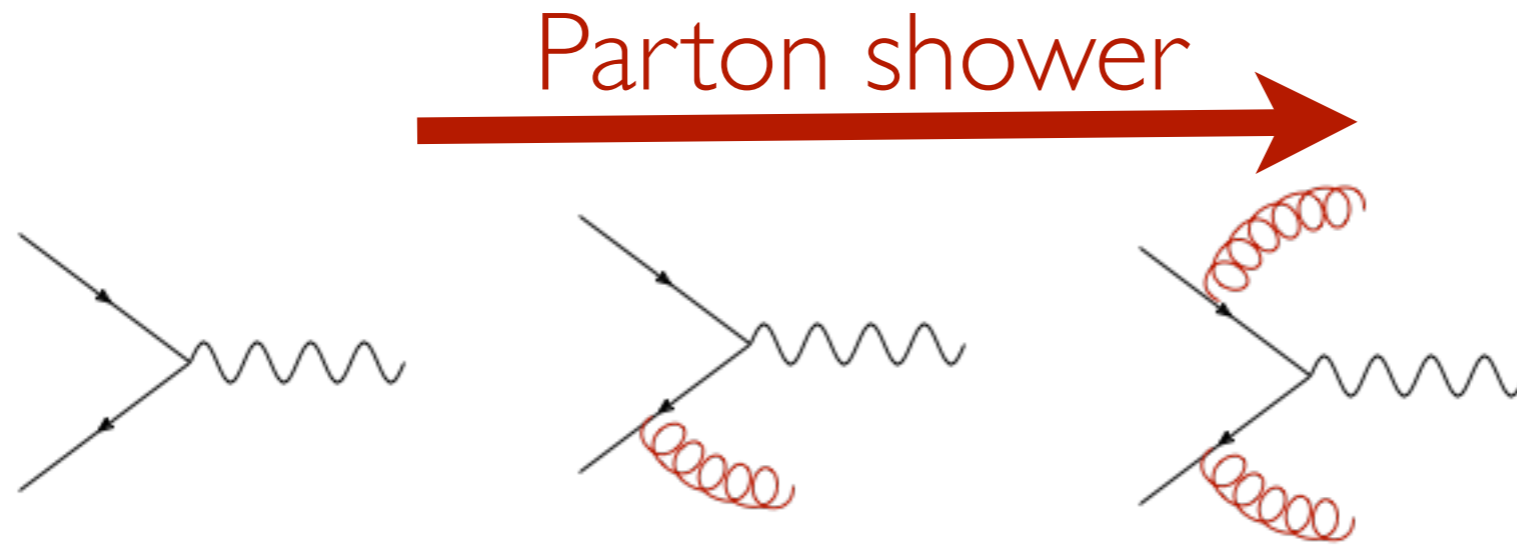


Parton shower



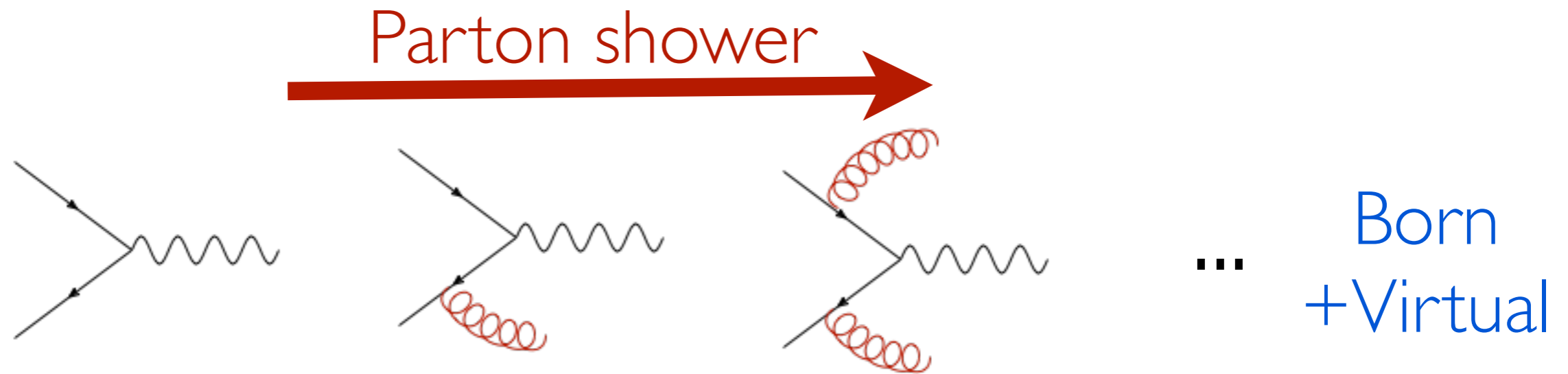
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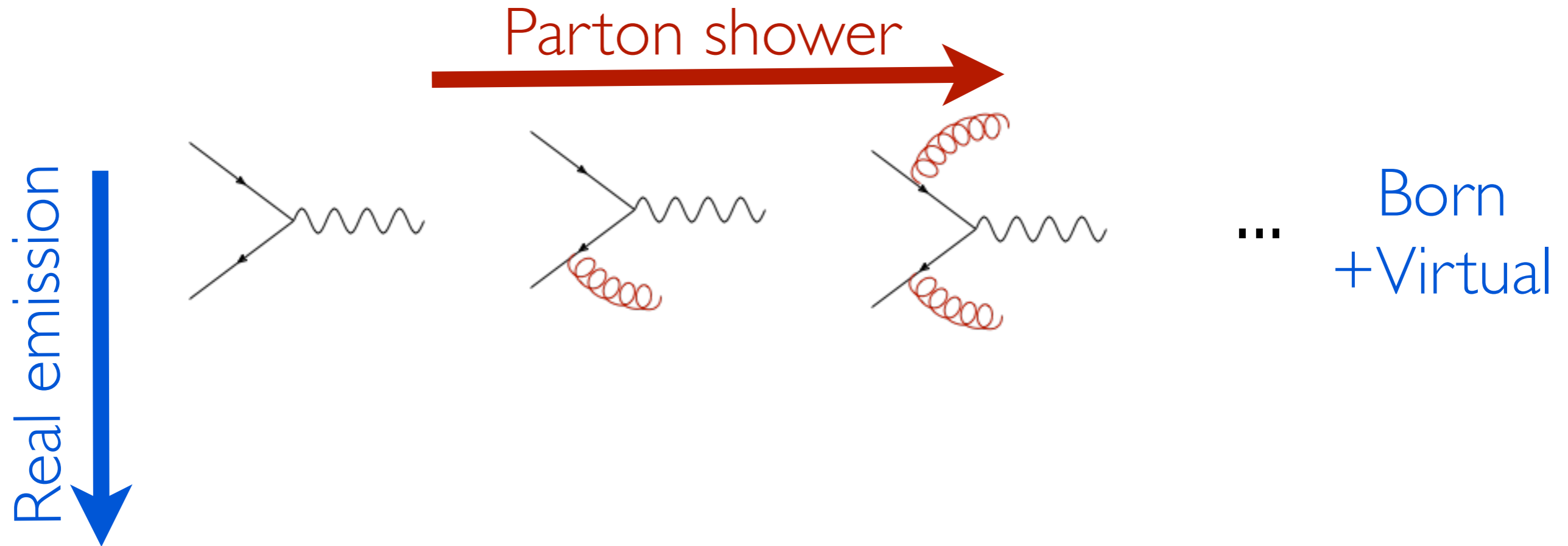
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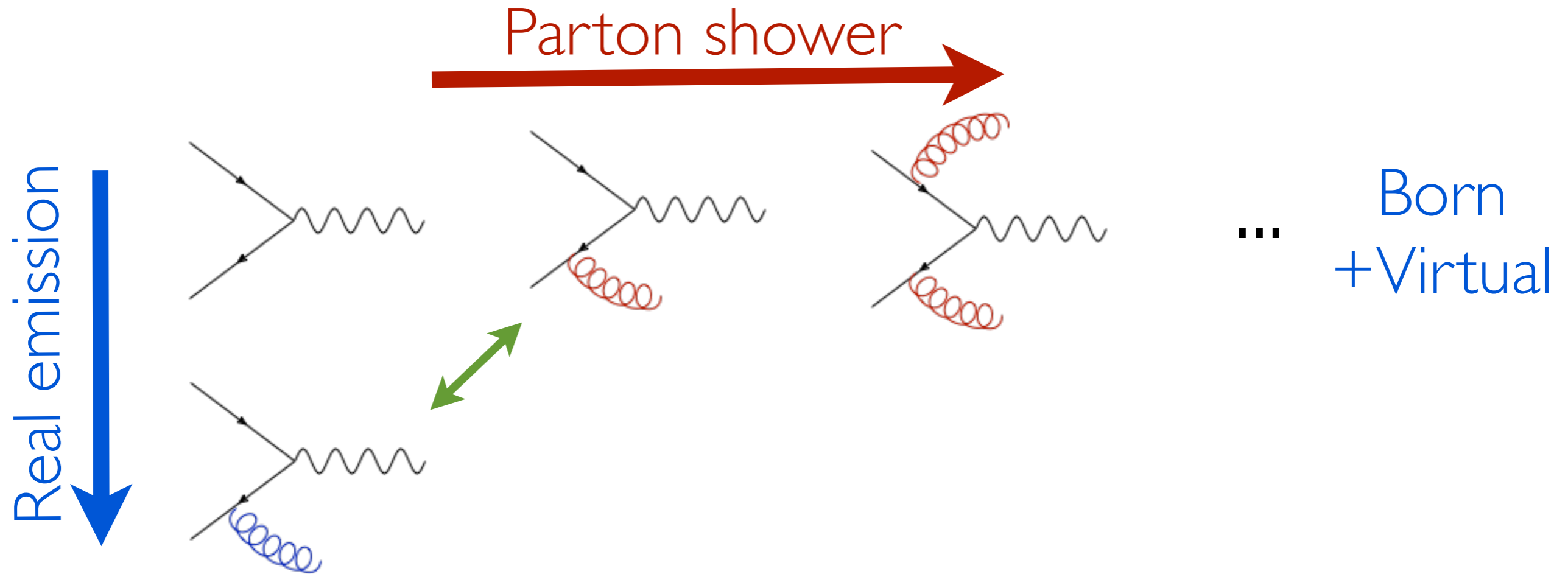


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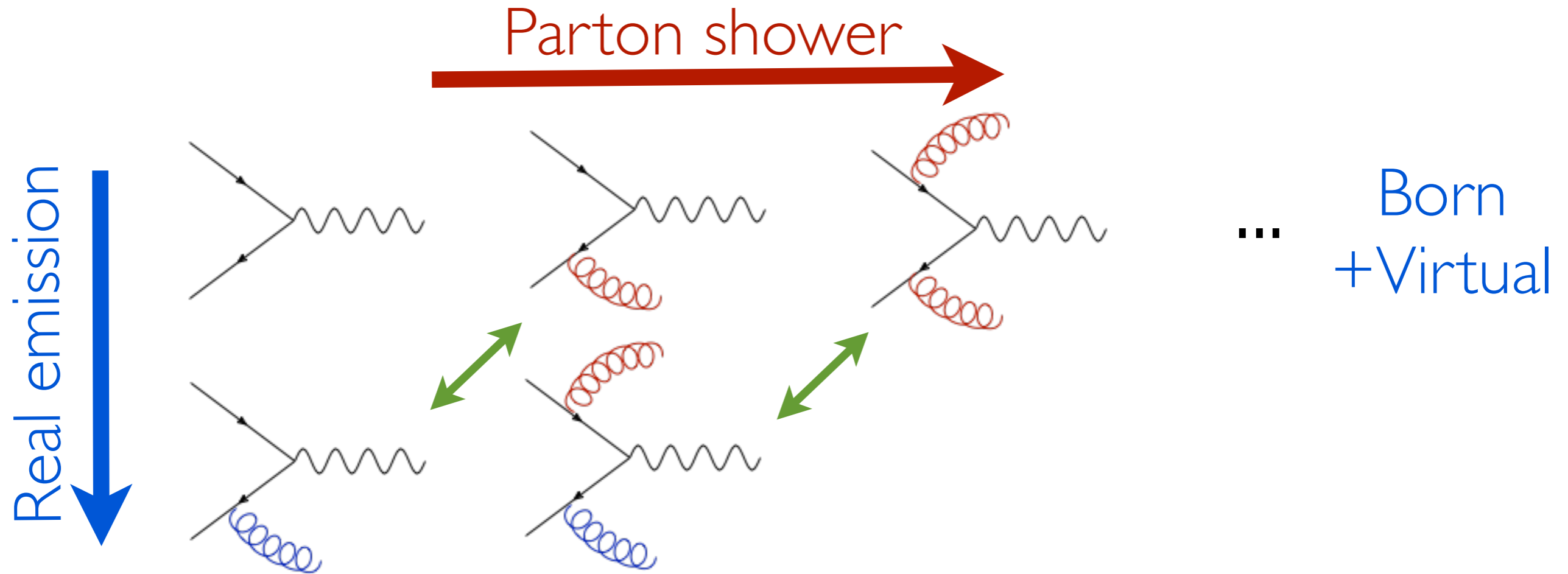
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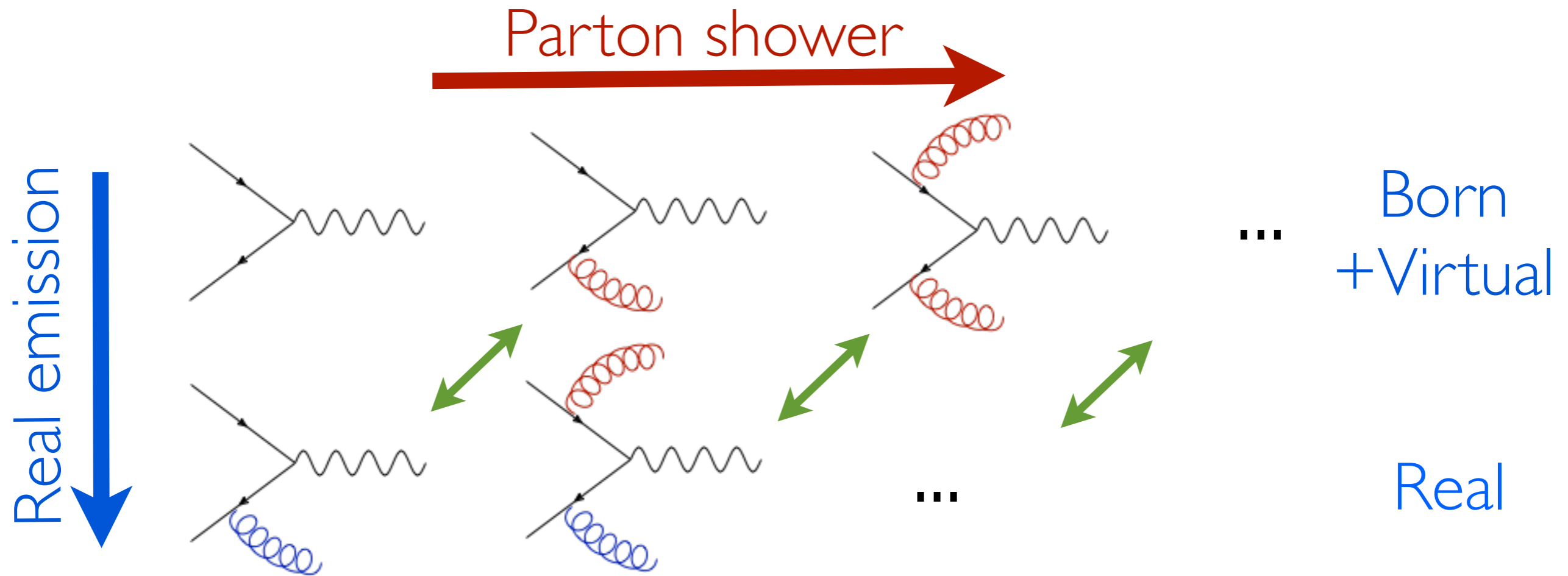
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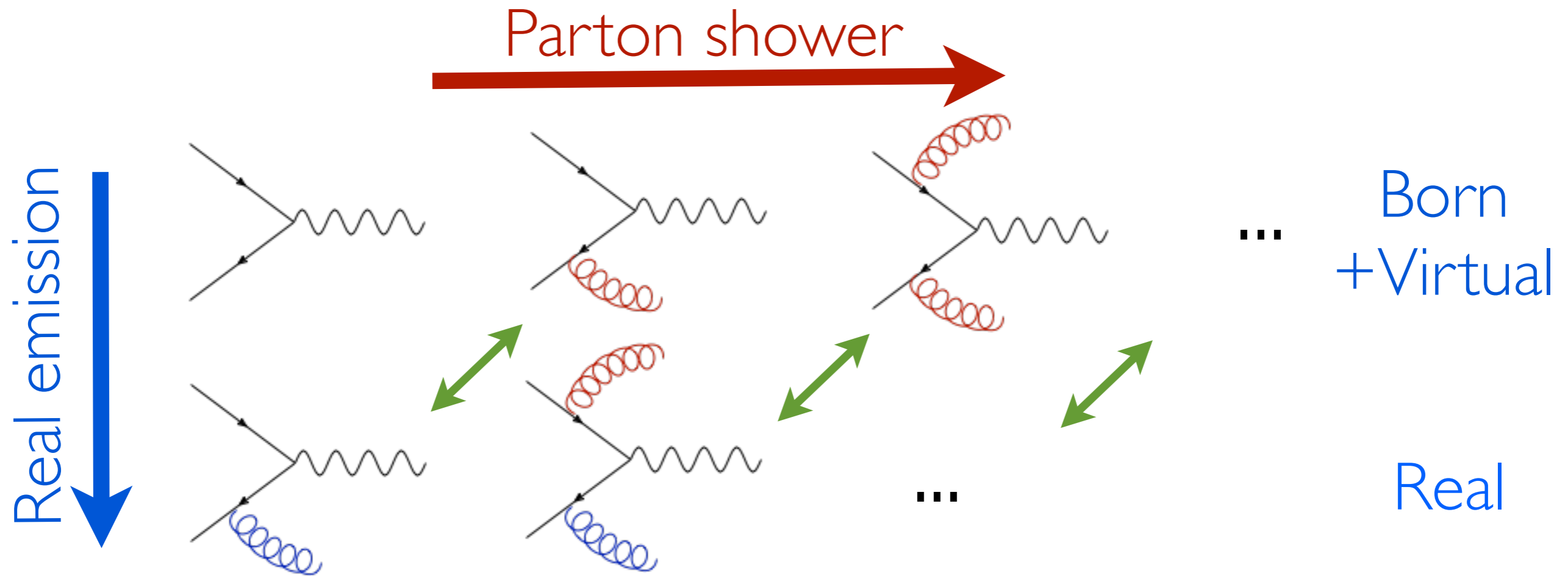
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# MATCHING TO PARTON SHOWER



- When matching **NLO** events to **PS**, one faces **double counting** issues.
  - And also part of the **virtual contribution** is **double counted** through the definition of the **Sudakov factor**.
  - Two ways out have been proposed: **POWHEG** and **MC@NLO**
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**used by MG5\_aMC**

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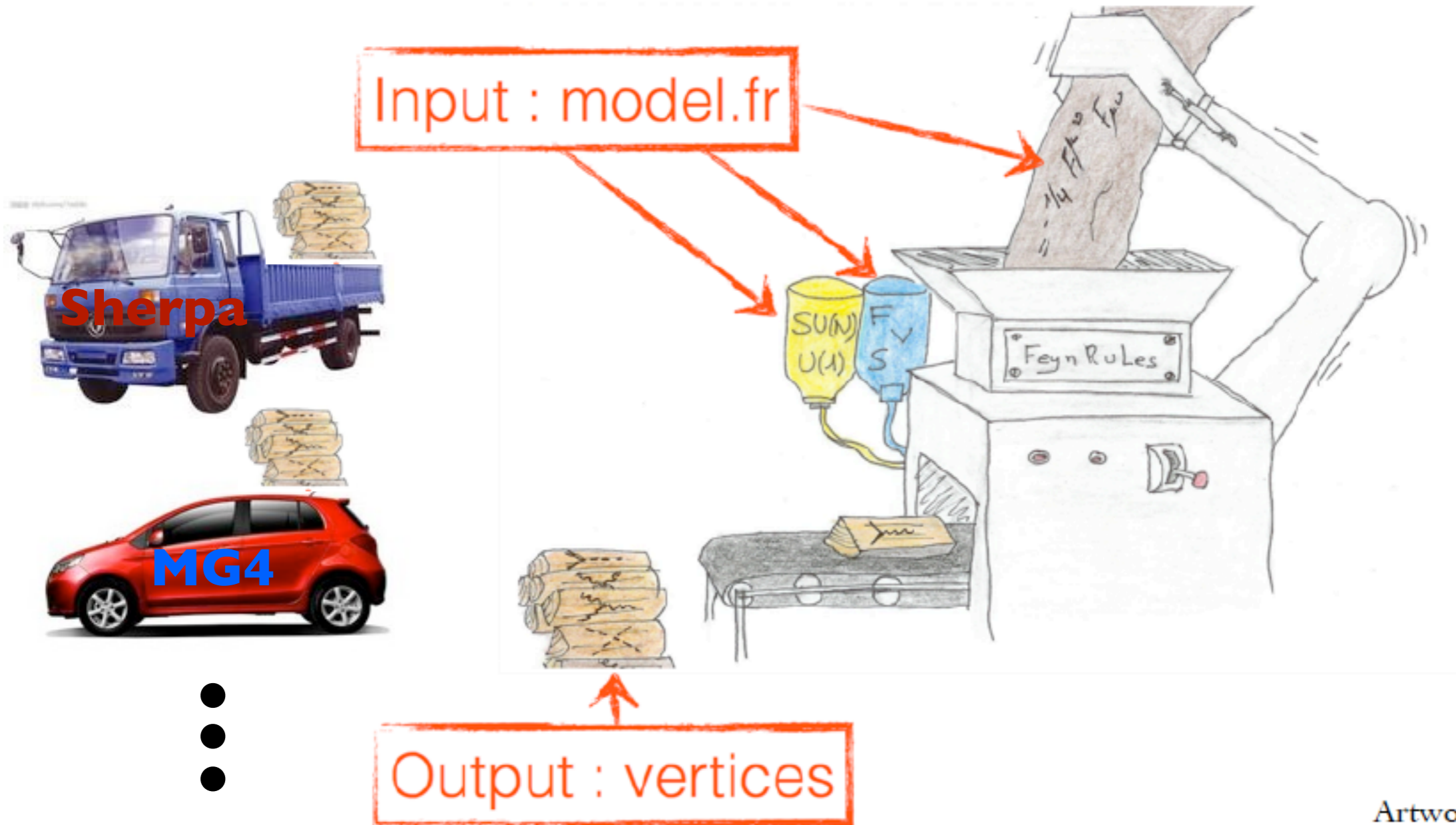
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# FEYNRULES

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- How to incorporate all of above information in a model file ?

*Details please refer to Claude's talk on Tuesday*



Artwork by C. Degrande

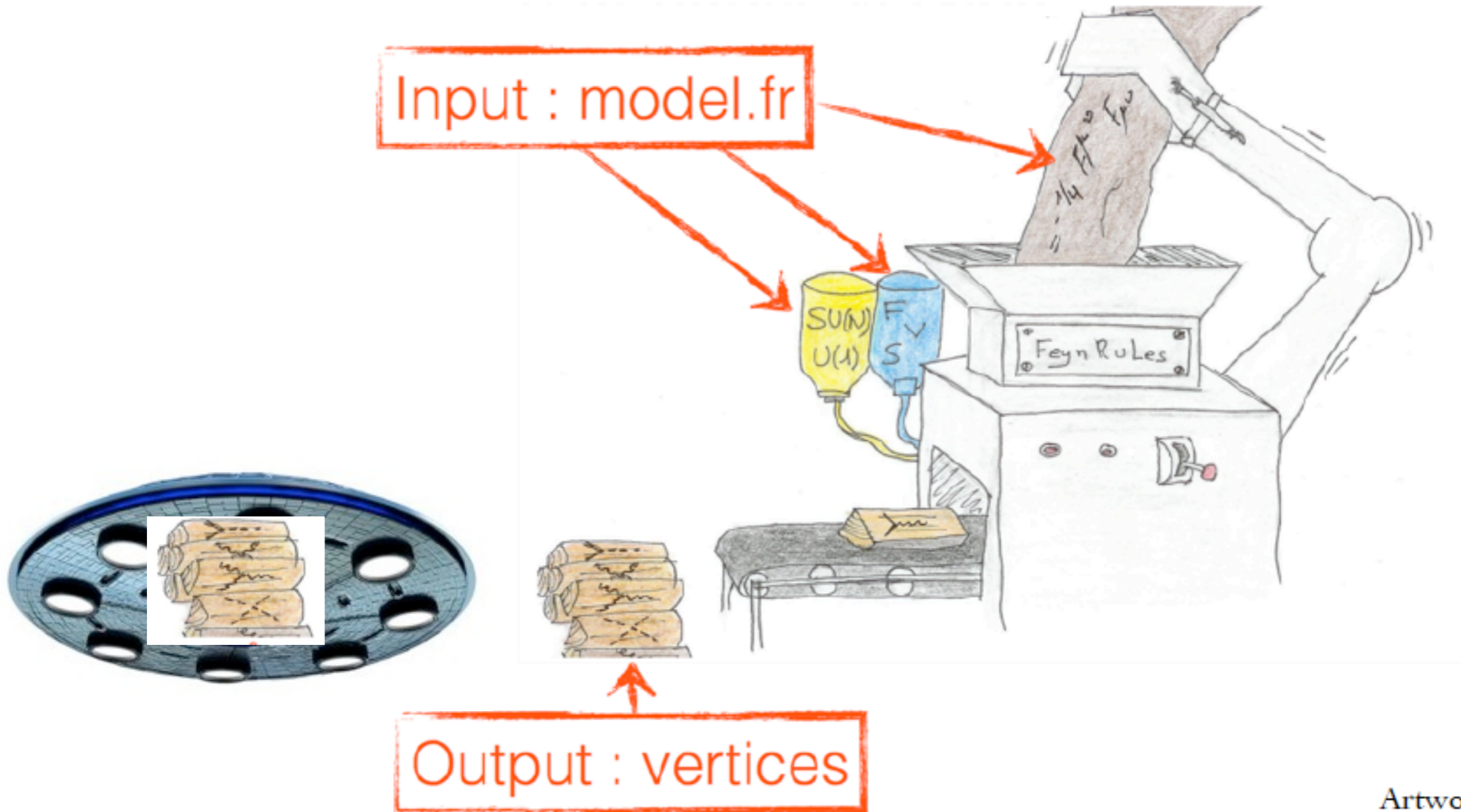


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- How to incorporate all of above information in a model file ?

*Details please refer to Claude's talk on Tuesday*



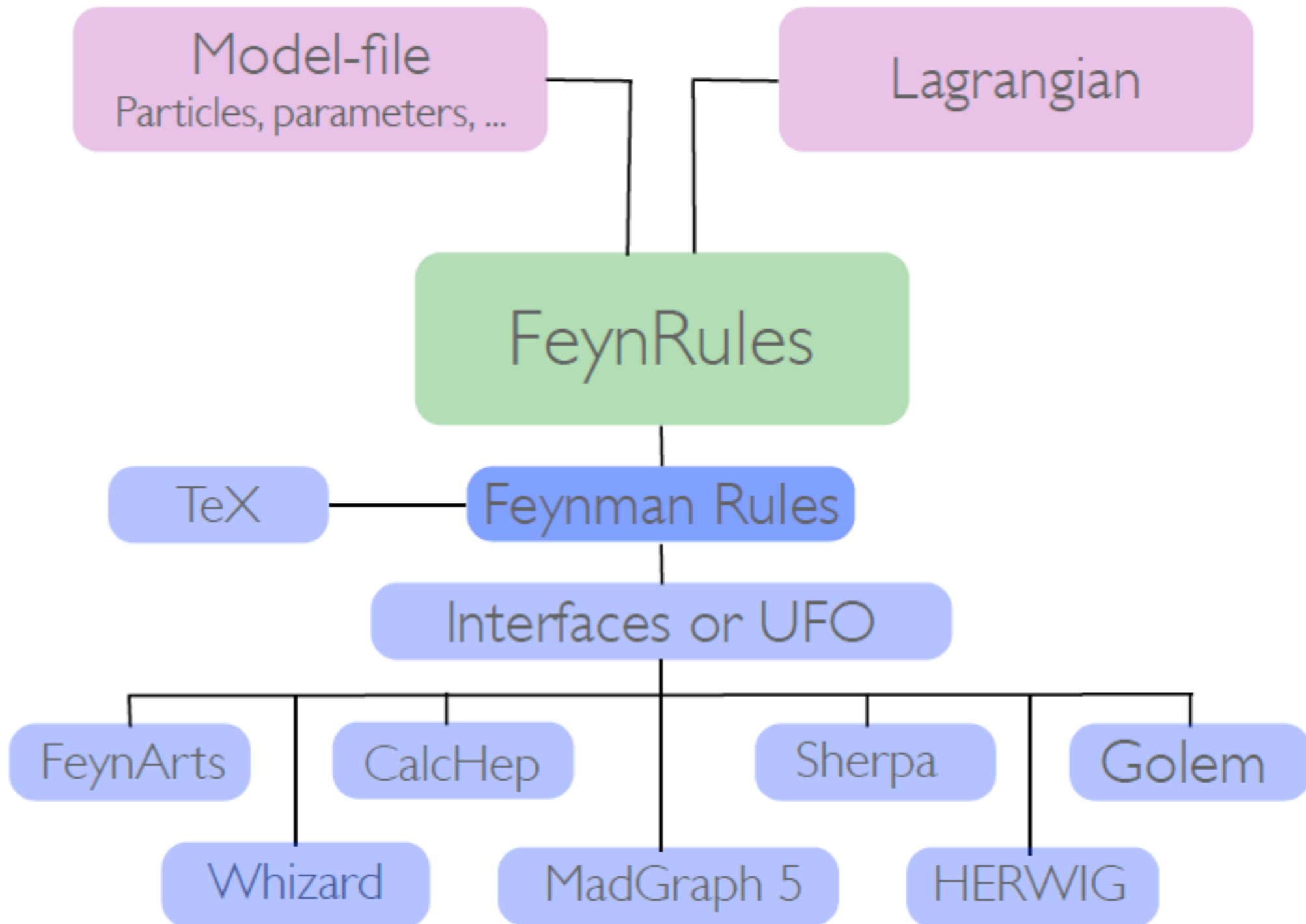
Artwork by C. Degrande

- UFO stands for Universal FeynRules Output:

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

# FEYNRULES: STRUCTURE

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)







# FEYNRULES: INPUT

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

# FEYNRULES: INPUT

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- Definitions of particles

```
(* ***** *)
(* **** Particle classes **** *)
(* ***** *)
M$ClassesDescription = {
    . . .
    V[4] == {
        ClassName      -> G,
        SelfConjugate  -> True,
        Indices        -> {Index[Gluon]},
        Mass           -> 0,
        Width          -> 0,
        ParticleName   -> "g",
        PDG            -> 21,
        PropagatorLabel -> "G",
        PropagatorType -> C,
        PropagatorArrow -> None,
        FullName       -> "G"
    },
    . . .
};
```

# FEYNRULES: INPUT

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- Definitions of particles

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        PDG            -> 21,
        PropagatorLabel -> "G",
        PropagatorType -> C,
        PropagatorArrow -> None,
        FullName       -> "G"
    },
    . . .
};
```

- Definitions of parameters

```
(* ***** *)
(* ***** Parameters ***** *)
(* ***** *)
M$Parameters = {
    . . .
    aS == {
        ParameterType -> External,
        BlockName     -> SMINPUTS,
        OrderBlock    -> 3,
        Value         -> 0.1184,
        InteractionOrder -> {QCD,2},
        TeX           -> Subscript[\[Alpha],s],
        Description   -> "Strong coupling constant at the Z pole",
    },
    . . .
};
```

# FEYNRULES: INPUT

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- Definitions of particles

```
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        PropagatorLabel -> "G",
        PropagatorType -> C,
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    },
    . . .
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```

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        Value         -> 0.1184,
        InteractionOrder -> {QCD,2},
        TeX           -> Subscript[\[Alpha],s],
        Description   -> "Strong coupling constant at the Z pole"
    },
    . . .
};
```

- Definitions of gauge groups

```
(* ***** *)
(* ***** Gauge groups ***** *)
(* ***** *)
M$GaugeGroups = {
    SU3C == {
        Abelian          -> False,
        CouplingConstant -> gs,
        GaugeBoson       -> G,
        StructureConstant -> f,
        Representations  -> {T,Colour},
        SymmetricTensor  -> dSUN
    }
};
```



# FEYNRULES: INPUT

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- Definitions of particles

```
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(* ***** *)
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        Width          -> 0,
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        PropagatorLabel -> "G",
        PropagatorType -> C,
        PropagatorArrow -> None,
        FullName       -> "G"
    },
    . . .
};
```

- Definitions of gauge groups

```
(* ***** *)
(* ***** Gauge groups ***** *)
(* ***** *)
M$GaugeGroups = {
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        GaugeBoson       -> G,
        StructureConstant -> f,
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};
```

- Definitions of parameters

```
(* ***** *)
(* ***** Parameters ***** *)
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        InteractionOrder -> {QCD, 2},
        TeX           -> Subscript[\[Alpha], s],
        Description   -> "Strong coupling constant at the Z pole"
    },
    . . .
};
```

- The Lagrangian

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + i\bar{q}\gamma^\mu D_\mu q - M_q \bar{q}q$$

```
L =
-1/4 FS[G,mu,nu,a] FS[G,mu,nu,a]
+ l qbar.Ga[mu].DC[q,mu]
- MQ qbar.q
```

# FEYNRULES: DERIVATION

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14)

- Above information can be incorporated in .fr files and load the file via

```
LoadModel[ < file.fr >, < file2.fr >, ... ]
```

- Extracting the Feynman rules

```
FeynmanRules[ L ]
```

- Output the model files for various generators

|                          |   |          |
|--------------------------|---|----------|
| WriteCHOutput[ L ]       | → | CalcHep  |
| WriteFeynArtsOutput[ L ] | → | FeynArts |
| WriteSHOutput[ L ]       | → | Sherpa   |
| WriteWOOOutput[ L ]      | → | Whizard  |

|               |   |   |                   |
|---------------|---|---|-------------------|
| WriteUFO[ L ] | ← | { | MadGraph5_aMC@NLO |
|               |   |   | Sherpa            |
|               |   |   | GoSam             |

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|                          |   |          |
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| WriteSHOutput[ L ]       | → | Sherpa   |
| WriteWOOOutput[ L ]      | → | Whizard  |

WriteUFO[ L ] **NEW Standard!** { MadGraph5\_aMC@NLO  
Sherpa  
GoSam

# WHY IS THE UFO NOW A STANDARD ?



Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

## ◆ Color structures: not supported in full generality by Monte Carlo generators

- ❖ The treatment of the color information is hard-coded
- ❖ The interfaces to a specific tool discard all non-supported vertices
- ❖ Representations usually handled: 1, 3, 8 (limited in CALCHEP), sometimes 6

## ◆ Lorentz structures and spins not supported in full generality by Monte Carlo programs

- ❖ The treatment of the Lorentz structures of the different vertices is hard-coded
- ❖ The possible spins for the particles are restricted
- ❖ The interfaces discard all non-supported vertices
- ❖ Spin representations usually handled: 0, 1/2, 1; sometimes 3/2, 2
- ❖ Lorentz structures usually handled: MSSM-like; sometimes any

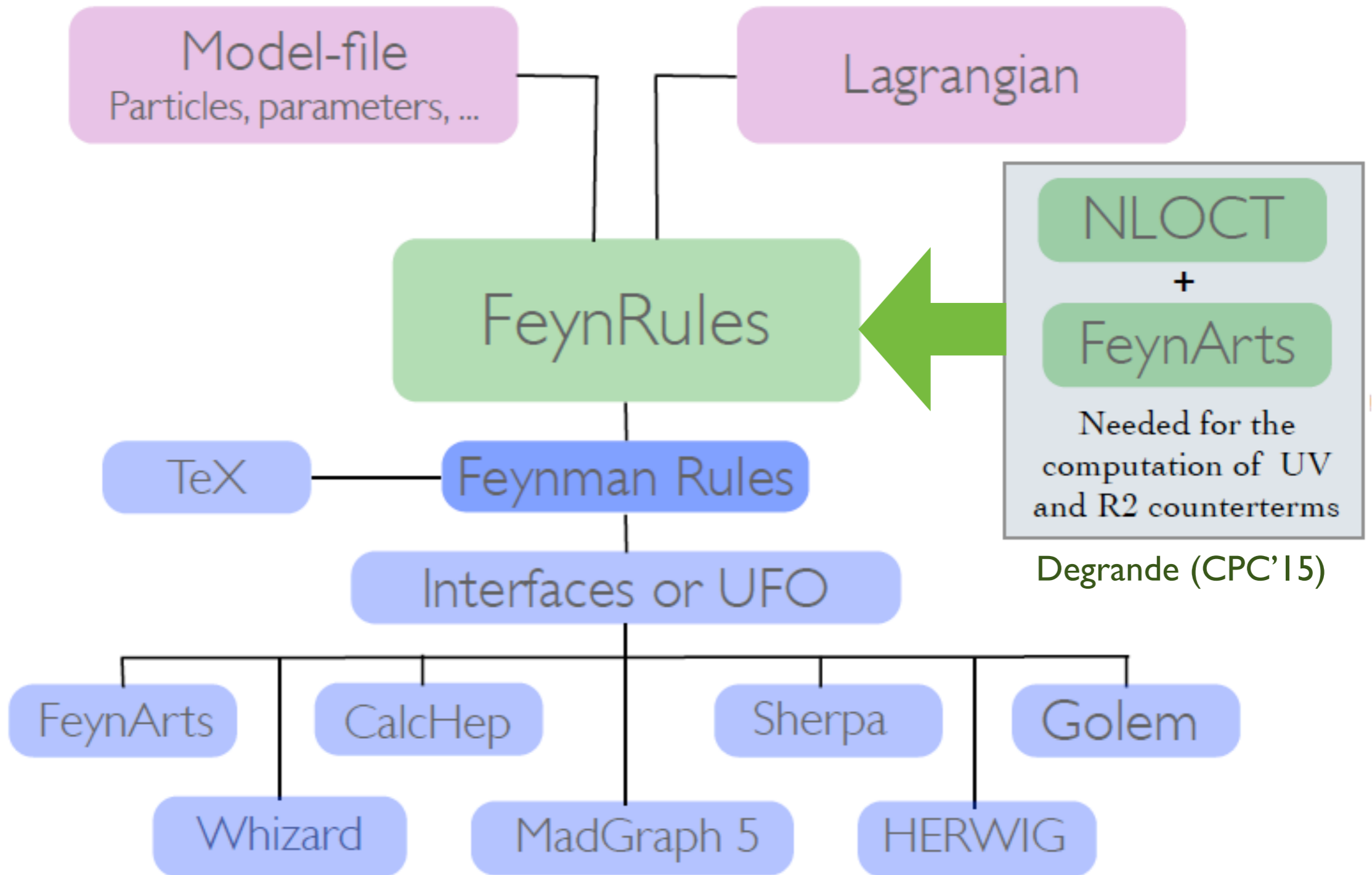
Each interface dedicated to a given tool is specific

- ★ Removal of vertices not compliant with the tool
- ★ Translation to a specific format and programming language
- ⇒ not efficient
- ⇒ better: one translation and the tools parse it



# FEYNRULES: STRUCTURE

Christensen, Duhr (CPC'09); Alloul, Christensen, Duhr, Degrande, Fuks (CPC'14); Degrande (CPC'15)



# FEYNRULES: DERIVATION@NLO I

Degrade (CPC'15)



## Load FeynRules and Model file

```
$FeynRulesPath = SetDirectory["~/feynrules/trunk/feynrules-development"]; << FeynRules`  
LoadModel["~/feynrules/trunk/feynrules-development/Models/SM/SM.fr",  
  "~/Dropbox/aMCatNLO-MSSM/FeynRulesInput/coloredscalars.fr"];
```

## Load restrict card

```
LoadRestriction["~/feynrules/trunk/feynrules-development/Models/SM/Masslessbuttb.rst"]  
LoadRestriction["~/feynrules/trunk/feynrules-development/Models/SM/DiagonalCKM.rst"]
```

## Derive Feynman rule (optional)

```
FeynmanRules [LSM + LagNP]
```

## Get renormalization Lagrangian

```
Lren = OnShellRenormalization[LSM + LagNP (*ExpandIndices[LSM, FlavorExpand→True] /.  
  {u[___]→0, c[___]→0, d[___]→0, s[___]→0, ve[___]→0, vm[___]→0, e[___]→0, mu[___]→0} *) , QCDOnly → True, FlavorMixing → False]; //  
Timing
```

## Generate NLO FeynArts Model

```
SetDirectory["~/FeynArts-3.8/Models"];  
WriteFeynArtsOutput[Lren, Output → "colscalarsnomixgs"]
```

*Tutorial this afternoon !*

## Quit kernel

```
Quit[]
```

## Load FeynArts and NLOCT

```
SetDirectory["~/FeynArts-3.8"];  
<< FeynArts`  
SetDirectory["~/feynrules/trunk/feynrules-development"];  
<< NLOCT`  
SetDirectory["~/feynrules/trunk/R2"];
```

## Compute UV and R2 CT

```
WriteCT["colscalarsnomix/colscalarsnomix", "colscalarsnomix/colscalarsnomix", Output -> "colscalartest",  
LabelInternal -> True, QCDOnly -> True, CTparameters -> False, KeptIndices -> {}, ZeroMom -> {{aS, {F[7], V[4], -F[7]}, 0},  
Assumptions -> {MT > 0},  
GenericVertexList -> {{F, F}, {S, S}, {V, V}, {F, F, V}, {F, F, S}, {F, F, V, V} (*, {V, V, S}, {V, S, S}, {S, S, S}, {V, V, V},  
{V, V, V, V}, {V, V, S, S} *)}, MaxDim -> 5, EvenOnly -> False, IsFeynmanGauge -> False] // Timing
```

*Tutorial this afternoon !*

## Quit kernel

```
Quit[]
```

## Load FeynRules and Model file again

```
$FeynRulesPath = SetDirectory["~/feynrules/trunk/feynrules-development"]; << FeynRules`  
LoadModel["~/feynrules/trunk/feynrules-development/Models/SM/SM.fr",  
  "~/Dropbox/aMCatNLO-MSSM/FeynRulesInput/coloredscalars.fr"];
```

## Load restrict card again

```
LoadRestriction["~/feynrules/trunk/feynrules-development/Models/SM/DiagonalCKM.rst"]  
LoadRestriction["~/feynrules/trunk/feynrules-development/Models/SM/Masslessbuttb.rst"]
```

## Get the UV and R2 computed by NLOCT

```
SetDirectory["~/feynrules/trunk/R2"];  
Get["colscalartest.nlo"];
```

## Write out NLO UFO model

```
FR$Loop = False;  
SetDirectory["~/2.2.0/models"];  
WriteUFO[LSM + LagNP, UVCounterterms → (UV$vertlist /. FR$IR → 1), R2Vertices → R2$vertlist, Output → "ColScalarFull",  
  Debug → False]
```

*Tutorial this afternoon !*



# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

## ◆ The UFO is a set of PYTHON files

- ✦ Particle information (particles.py)
- ✦ Interaction information (vertices.py, couplings.py, lorentz.py, couplings\_orders.py)
- ✦ Parameter information (parameters.py)
- ✦ Propagator information (propagators.py)
- ✦ Tools (function\_library.py, object\_library.py, write\_param\_card.py, decays.py)
- ✦ NLO counterterms (CT\_couplings.py, CT\_parameters.py, CT\_vertices.py) ..

For example: SUSY QCD

```

bogon:SUSYQCD_CTprm_UFO erdissshaw$ ls
CT_couplings.py          SUSYQCD_CTprm_UFO.log  couplings.py           object_library.py      propagators.py
CT_parameters.py        __init__.py            function_library.py    parameters.py          vertices.py
CT_vertices.py          coupling_orders.py     lorentz.py             particles.py            write_param_card.py
  
```

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CT_vertices.py          coupling_orders.py     lorentz.py              particles.py             write_param_card.py
  
```

**Particles**

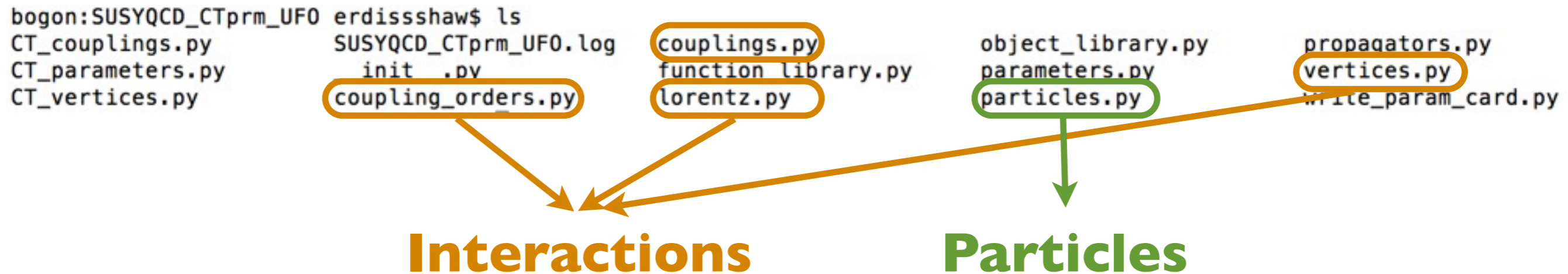
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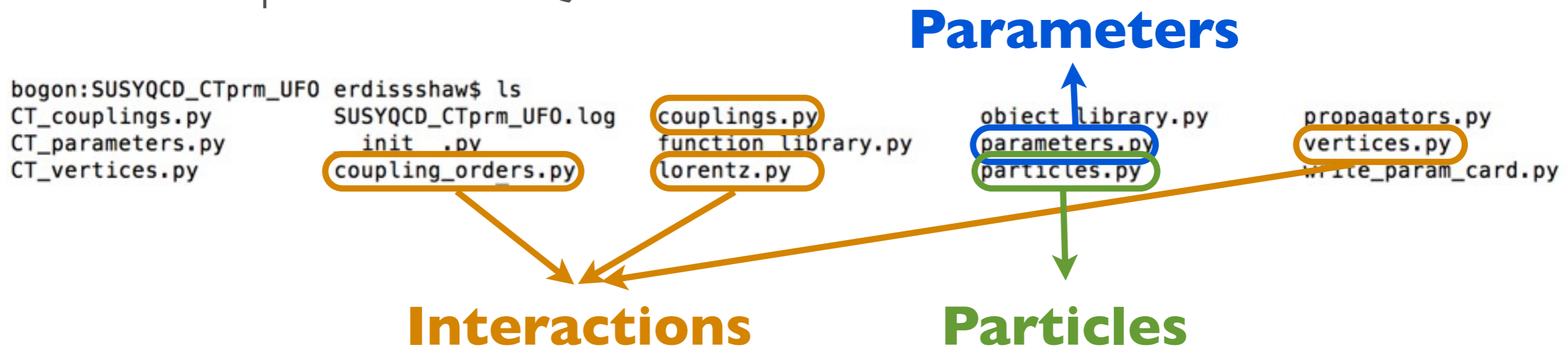
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For example: SUSY QCD





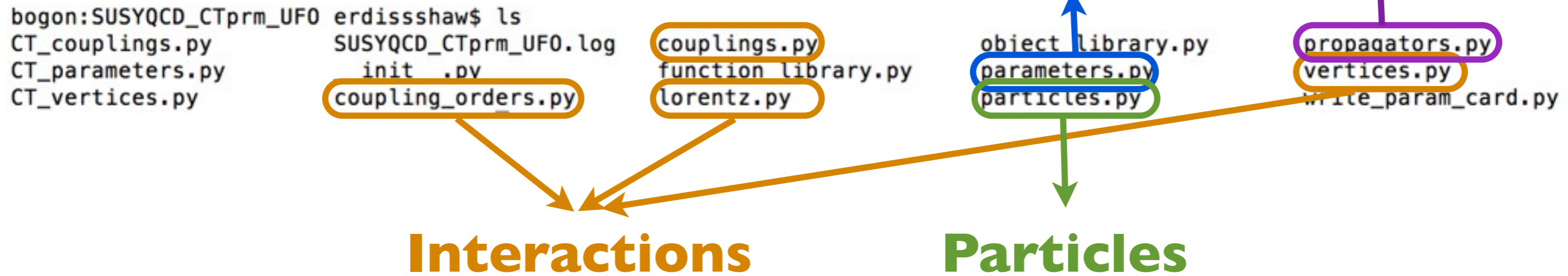
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For example: SUSY QCD



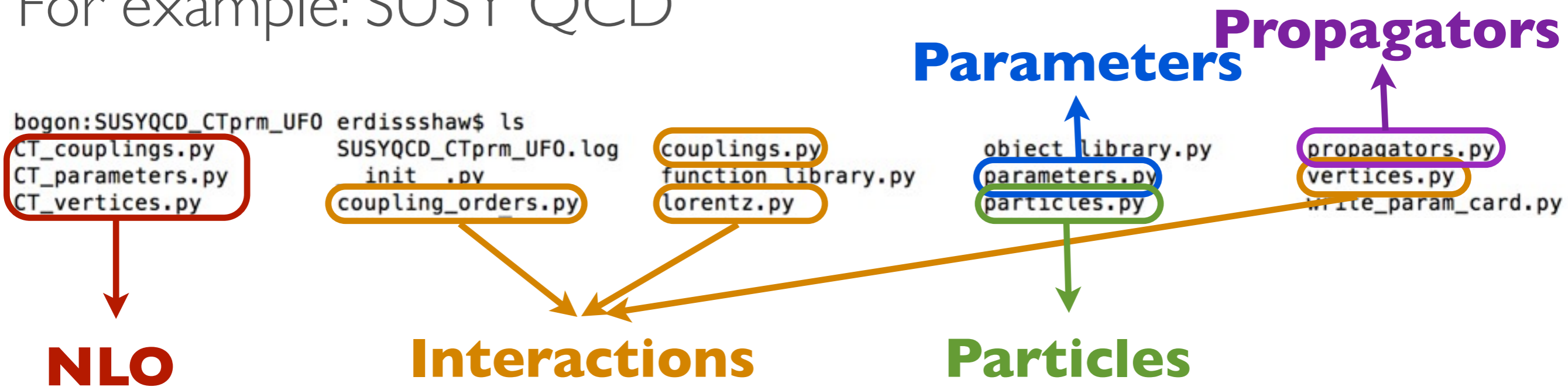
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For example: SUSY QCD



# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

- **Particles are in** `particles.py`
  - Instances of the particle class
  - `spin`, `color`, `mass`, `width`, `PDG` etc

```
go = Particle(pdg_code = 1000021,  
             name = 'go',  
             antiname = 'go',  
             spin = 2,  
             color = 8,  
             mass = Param.Mgo,  
             width = Param.Wgo,  
             texname = 'go',  
             antitexname = 'go',  
             charge = 0,  
             GhostNumber = 0,  
             LeptonNumber = 0,  
             Y = 0)
```

# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

- **Particles are in** particles.py
- **Parameters are in** parameters.py
- Instances of the particle class
- External parameters are in LHA-like
- spin, color, mass, width, PDG etc
- Python-compliant formula for int. para

```
go = Particle(pdg_code = 1000021,
              name = 'go',
              antiname = 'go',
              spin = 2,
              color = 8,
              mass = Param.Mgo,
              width = Param.Wgo,
              texname = 'go',
              antitexname = 'go',
              charge = 0,
              GhostNumber = 0,
              LeptonNumber = 0,
              Y = 0)
```

```
aS = Parameter(name = 'aS',
               nature = 'external',
               type = 'real',
               value = 0.1184,
               texname = '\\alpha_s',
               lhablock = 'SMINPUTS',
               lhacode = [ 3 ])
```

```
G = Parameter(name = 'G',
               nature = 'internal',
               type = 'real',
               value = '2*cmath.sqrt(aS)*cmath.sqrt(cmath.pi)',
               texname = 'G')
```



# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

- Interactions are in** `vertices.py`, `couplings.py`, `lorentz.py`, `coupling_orders.py`

- Vertices are decomposed in a spin x color basis, coupling being coordinates
- Example: the quartic gluon vertex can be written as

$$\begin{aligned}
 & ig_s^2 f^{a_1 a_2 b} f^{b a_3 a_4} (\eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4}) \\
 & + ig_s^2 f^{a_1 a_3 b} f^{b a_2 a_4} (\eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4}) \\
 & + ig_s^2 f^{a_1 a_4 b} f^{b a_2 a_3} (\eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4})
 \end{aligned}
 \Rightarrow
 \begin{aligned}
 & (f^{a_1 a_2 b} f^{b a_3 a_4}, f^{a_1 a_3 b} f^{b a_2 a_4}, f^{a_1 a_4 b} f^{b a_2 a_3}) \\
 & \times \begin{pmatrix} ig_s^2 & 0 & 0 \\ 0 & ig_s^2 & 0 \\ 0 & 0 & ig_s^2 \end{pmatrix} \begin{pmatrix} \eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} \\ \eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4} \\ \eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4} \end{pmatrix}
 \end{aligned}$$

- vertices.py**: define all Feynman rules for vertices in the model

```

V_37 = Vertex(name = 'V_37',
              particles = [ P.g, P.g, P.g, P.g ],
              color = [ 'f(-1,1,2)*f(3,4,-1)', 'f(-1,1,3)*f(2,4,-1)', 'f(-1,1,4)*f(2,3,-1)' ],
              lorentz = [ L.VVVV2, L.VVVV3, L.VVVV4 ],
              couplings = {(1,0):C.GC_20,(0,0):C.GC_20,(2,1):C.GC_20,(0,1):C.GC_19,(2,2):C.GC_19,(1,2):C.GC_19})

```

- lorentz.py**: define the Lorentz structure in the model

```

VVVV2 = Lorentz(name = 'VVVV2',
                spins = [ 3, 3, 3, 3 ],
                structure = 'Metric(1,4)*Metric(2,3)')

```

- couplings.py**: define the coupling constant in the model

```

GC_20 = Coupling(name = 'GC_20',
                 value = 'complex(0,1)*G**2',
                 order = {'QCD':2})

```

- coupling\_orders.py**: define the coupling orders in the model

```

QCD = CouplingOrder(name = 'QCD',
                    expansion_order = 99,
                    hierarchy = 1,
                    perturbative_expansion = 1)

```

# UFO

Degrande, Duhr, Fuks, Grellscheid, Mattelaer, Reiter (CPC'12)

- Interactions are in** `vertices.py`, `couplings.py`, `lorentz.py`, `coupling_orders.py`

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- Example: the quartic gluon vertex can be written as

$$\begin{aligned}
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 & + ig_s^2 f^{a_1 a_3 b} f^{b a_2 a_4} (\eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4}) \\
 & + ig_s^2 f^{a_1 a_4 b} f^{b a_2 a_3} (\eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4})
 \end{aligned}
 \Rightarrow
 \begin{aligned}
 & (f^{a_1 a_2 b} f^{b a_3 a_4}, f^{a_1 a_3 b} f^{b a_2 a_4}, f^{a_1 a_4 b} f^{b a_2 a_3}) \\
 & \times \begin{pmatrix} ig_s^2 & 0 & 0 \\ 0 & ig_s^2 & 0 \\ 0 & 0 & ig_s^2 \end{pmatrix} \begin{pmatrix} \eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} \\ \eta^{\mu_1 \mu_4} \eta^{\mu_2 \mu_3} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4} \\ \eta^{\mu_1 \mu_3} \eta^{\mu_2 \mu_4} - \eta^{\mu_1 \mu_2} \eta^{\mu_3 \mu_4} \end{pmatrix}
 \end{aligned}$$

- `vertices.py`: define all Feynman rules for vertices in the model

```

V_37 = Vertex(name = 'V_37',
              particles = [ P.g, P.g, P.g, P.g ],
              color = [ 'f(-1,1,2)*f(3,4,-1)', 'f(-1,1,3)*f(2,4,-1)', 'f(-1,1,4)*f(2,3,-1)' ],
              lorentz = [ L.VVVV2, L.VVVV3, L.VVVV4 ],
              couplings = {(1,0):C.GC_20,(0,0):C.GC_20,(2,1):C.GC_20,(0,1):C.GC_19,(2,2):C.GC_19,(1,2):C.GC_19})

```

- `lorentz.py`: define the Lorentz structure in the model

```

VVVV2 = Lorentz(name = 'VVVV2',
                 spins = [ 3, 3, 3, 3 ],
                 structure = 'Metric(1,4)*Metric(2,3)')

```

- `couplings.py`: define the coupling constant in the model

```

GC_20 = Coupling(name = 'GC_20',
                  value = 'complex(0,1)*G**2',
                  order = {'QCD':2})

```

- `coupling_orders.py`: define the coupling orders in the model

```

QCD = CouplingOrder(name = 'QCD',
                    expansion_order = 99,
                    hierarchy = 1,
                    perturbative_expansion = 1)

```

**Make sure > 0 for NLO QCD**



# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)



# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in [parameters.py](#)

```
MU_R = Parameter(name = 'MU_R',  
                 nature = 'external',  
                 type = 'real',  
                 value = 91.188,  
                 texname = '\\text{\\mu}_r',  
                 lhablock = 'LOOP',  
                 lhacode = [1])
```

# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in `parameters.py`

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu_r}',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- `CT_vertices.py`: UV, R2 counter term vertices

```
V_2 = CTVertex(name = 'V_2',
              type = 'R2',
              particles = [ P.g, P.g, P.g, P.g ],
              color = [ 'd(-1,1,3)*d(-1,2,4)', 'd(-1,1,3)*f(-1,2,4)', 'd(-1,1,4)*d(-1,2,3)', 'd(-1,1,4)*f(-1,2,3)', 'd(-1,2,3)*f(-1,1,4)', 'd(-1,2,4)*f(-1,1,3)', 'f(-1,1,2)*f(-1,3,4)', 'f(-1,1,3)*f(-1,2,4)', 'f(-1,1,4)*f(-1,2,3)', 'Identity(1,2)*Identity(3,4)', 'Identity(1,3)*Identity(2,4)', 'Identity(1,4)*Identity(2,3)' ],
              lorentz = [ L.VVVV2, L.VVVV3, L.VVVV4 ],
              loop_particles = [ [ [P.b], [P.c], [P.d], [P.s], [P.t], [P.u] ], [ [P.g] ], [ [P.go] ] ],
              couplings = {(2,0,0):C.R2GC_101_4,(2,0,1):C.R2GC_100_3,(2,0,2):C.R2GC_100_2,(0,0,0):C.R2GC_101_4,(0,0,1):C.R2GC_100_3,(0,0,2):C.R2GC_100_2,(4,0,0):C.R2GC_99_171,(4,0,1):C.R2GC_99_172,(4,0,2):C.R2GC_99_173,(3,0,0):C.R2GC_99_171,(3,0,1):C.R2GC_99_172,(3,0,2):C.R2GC_99_173,(8,0,0):C.R2GC_100_1,(8,0,1):C.R2GC_100_2,(8,0,2):C.R2GC_100_3,(6,0,0):C.R2GC_110_22,(6,0,1):C.R2GC_112_26,(6,0,2):C.R2GC_110_23,(7,0,0):C.R2GC_111_24,(7,0,1):C.R2GC_105_11,(7,0,2):C.R2GC_111_25,(5,0,0):C.R2GC_99_171,(5,0,1):C.R2GC_99_172,(5,0,2):C.R2GC_99_173,(1,0,0):C.R2GC_99_171,(1,0,1):C.R2GC_99_172,(1,0,2):C.R2GC_99_173,(11,0,0):C.R2GC_103_7,(11,0,1):C.R2GC_103_8,(11,0,2):C.R2GC_103_9,(10,0,0):C.R2GC_103_7,(10,0,1):C.R2GC_103_8,(10,0,2):C.R2GC_103_9,(9,0,1):C.R2GC_102_5,(9,0,2):C.R2GC_102_6,(2,1,0):C.R2GC_101_4,(2,1,1):C.R2GC_100_3,(2,1,2):C.R2GC_100_2,(0,1,0):C.R2GC_101_4,(0,1,1):C.R2GC_100_3,(0,1,2):C.R2GC_100_2,(4,1,0):C.R2GC_99_171,(4,1,1):C.R2GC_99_172,(4,1,2):C.R2GC_99_173,(3,1,0):C.R2GC_99_171,(3,1,1):C.R2GC_99_172,(3,1,2):C.R2GC_99_173,(8,1,0):C.R2GC_100_1,(8,1,1):C.R2GC_105_11,(8,1,2):C.R2GC_100_3,(6,1,0):C.R2GC_115_29,(6,1,1):C.R2GC_115_30,(6,1,2):C.R2GC_115_31,(7,1,0):C.R2GC_111_24,(7,1,1):C.R2GC_100_2,(7,1,2):C.R2GC_111_25,(5,1,0):C.R2GC_99_171,(5,1,1):C.R2GC_99_172,(5,1,2):C.R2GC_99_173,(1,1,0):C.R2GC_99_171,(1,1,1):C.R2GC_99_172,(1,1,2):C.R2GC_99_173,(11,1,0):C.R2GC_103_7,(11,1,1):C.R2GC_103_8,(11,1,2):C.R2GC_103_9,(10,1,0):C.R2GC_103_7,(10,1,1):C.R2GC_103_8,(10,1,2):C.R2GC_103_9,(9,1,1):C.R2GC_102_5,(9,1,2):C.R2GC_102_6,(0,2,0):C.R2GC_101_4,(0,2,1):C.R2GC_100_3,(0,2,2):C.R2GC_100_2,(2,2,0):C.R2GC_101_4,(2,2,1):C.R2GC_100_3,(2,2,2):C.R2GC_100_2,(5,2,0):C.R2GC_99_171,(5,2,1):C.R2GC_99_172,(5,2,2):C.R2GC_99_173,(1,2,0):C.R2GC_99_171,(1,2,1):C.R2GC_99_172,(1,2,2):C.R2GC_99_173,(7,2,0):C.R2GC_114_27,(7,2,1):C.R2GC_104_10,(7,2,2):C.R2GC_114_28,(4,2,0):C.R2GC_99_171,(4,2,1):C.R2GC_99_172,(4,2,2):C.R2GC_99_173,(3,2,0):C.R2GC_99_171,(3,2,1):C.R2GC_99_172,(3,2,2):C.R2GC_99_173,(8,2,0):C.R2GC_100_1,(8,2,1):C.R2GC_100_2,(8,2,2):C.R2GC_100_3,(6,2,0):C.R2GC_110_22,(6,2,2):C.R2GC_110_23,(11,2,0):C.R2GC_103_7,(11,2,1):C.R2GC_103_8,(11,2,2):C.R2GC_103_9,(10,2,0):C.R2GC_103_7,(10,2,1):C.R2GC_103_8,(10,2,2):C.R2GC_103_9,(9,2,1):C.R2GC_102_5,(9,2,2):C.R2GC_102_6})
```



# UFO@NLO

Degrade, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in `parameters.py`

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu_r}',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- `CT_vertices.py`: UV, R2 counter term vertices

```
V_351 = CTVertex(name = 'V_351',
                type = 'UV',
                particles = [ P.g, P.g, P.g, P.g ],
                color = [ 'd(-1,1,3)=d(-1,2,4)', 'd(-1,1,3)*f(-1,2,4)', 'd(-1,1,4)=d(-1,2,3)', 'd(-1,1,4)*f(-1,2,3)', 'd(-1,2,3)*f(-1,1,4)', 'd(-1,2,4)*f(-1,1,3)', 'f(-1,1,2)*f(-1,3,4)', 'f(-1,1,3)*f(-1,2,4)', 'f(-1,1,4)*f(-1,2,3)', 'Identity(1,2)*Identity(3,4)', 'Identity(1,3)*Identity(2,4)', 'Identity(1,4)*Identity(2,3)' ],
                lorentz = [ L.VVVV2, L.VVVV3, L.VVVV4 ],
                loop_particles = [ [ [P.b], [P.b], [P.c], [P.d], [P.s], [P.sBL], [P.sBR], [P.sCL], [P.sCR], [P.sDL], [P.sDR], [P.sSL], [P.sSR], [P.stL], [P.stR], [P.suL], [P.suR], [P.t], [P.u] ],
                                [ [P.b], [P.c], [P.d], [P.s], [P.t], [P.u] ], [ [P.c], [P.d] ], [ [P.g] ], [ [P.ghG] ], [ [P.go] ], [ [P.s] ], [ [P.sBL] ], [ [P.sBR] ], [ [P.sCL] ], [ [P.sCR] ], [ [P.sDL] ], [ [P.sDR] ], [ [P.sSL] ], [ [P.sSR] ], [ [P.stL] ], [ [P.stR] ], [ [P.suL] ], [ [P.suR] ], [ [P.t] ], [ [P.u] ] ],
                                couplings = {(2,0,5):C.UVGC_100_2,(2,0,6):C.UVGC_100_1,(0,0,5):C.UVGC_100_2,(0,0,6):C.UVGC_100_1,(4,0,5):C.UVGC_99_1085,(4,0,6):C.UVGC_99_1086,(3,0,5):C.UVGC_99_1085,(3,0,6):C.UVGC_99_1086,(8,0,5):C.UVGC_100_1,(8,0,6):C.UVGC_100_2,(6,0,0):C.UVGC_112_137,(6,0,3):C.UVGC_112_138,(6,0,4):C.UVGC_112_139,(6,0,5):C.UVGC_112_140,(6,0,6):C.UVGC_112_141,(6,0,7):C.UVGC_112_142,(6,0,8):C.UVGC_112_143,(6,0,9):C.UVGC_112_144,(6,0,11):C.UVGC_112_145,(6,0,12):C.UVGC_112_146,(6,0,13):C.UVGC_112_147,(6,0,14):C.UVGC_112_148,(6,0,15):C.UVGC_112_149,(6,0,16):C.UVGC_112_150,(6,0,17):C.UVGC_112_151,(6,0,18):C.UVGC_112_152,(6,0,19):C.UVGC_112_153,(6,0,20):C.UVGC_112_154,(6,0,21):C.UVGC_112_155,(6,0,22):C.UVGC_112_156,(6,0,23):C.UVGC_112_157,(7,0,0):C.UVGC_112_137,(7,0,3):C.UVGC_112_138,(7,0,4):C.UVGC_112_139,(7,0,5):C.UVGC_105_31,(7,0,6):C.UVGC_113_158,(7,0,7):C.UVGC_112_142,(7,0,8):C.UVGC_112_143,(7,0,9):C.UVGC_112_144,(7,0,11):C.UVGC_112_145,(7,0,12):C.UVGC_112_146,(7,0,13):C.UVGC_112_147,(7,0,14):C.UVGC_112_148,(7,0,15):C.UVGC_112_149,(7,0,16):C.UVGC_112_150,(7,0,17):C.UVGC_112_151,(7,0,18):C.UVGC_112_152,(7,0,19):C.UVGC_112_153,(7,0,20):C.UVGC_112_154,(7,0,21):C.UVGC_112_155,(7,0,22):C.UVGC_112_156,(7,0,23):C.UVGC_112_157,(5,0,5):C.UVGC_99_1085,(5,0,6):C.UVGC_99_1086,(1,0,5):C.UVGC_99_1085,(1,0,6):C.UVGC_99_1086,(11,0,5):C.UVGC_103_5,(11,0,6):C.UVGC_103_6,(10,0,5):C.UVGC_103_5,(10,0,6):C.UVGC_103_6,(9,0,5):C.UVGC_102_3,(9,0,6):C.UVGC_102_4,(2,1,5):C.UVGC_100_2,(2,1,6):C.UVGC_100_1,(0,1,5):C.UVGC_100_2,(0,1,6):C.UVGC_100_1,(4,1,5):C.UVGC_99_1085,(4,1,6):C.UVGC_99_1086,(3,1,5):C.UVGC_99_1085,(3,1,6):C.UVGC_99_1086,(8,1,0):C.UVGC_105_28,(8,1,3):C.UVGC_105_29,(8,1,4):C.UVGC_105_30,(8,1,5):C.UVGC_105_31,(8,1,6):C.UVGC_105_32,(8,1,7):C.UVGC_105_33,(8,1,8):C.UVGC_105_34,(8,1,9):C.UVGC_105_35,(8,1,11):C.UVGC_105_36,(8,1,12):C.UVGC_105_37,(8,1,13):C.UVGC_105_38,(8,1,14):C.UVGC_105_39,(8,1,15):C.UVGC_105_40,(8,1,16):C.UVGC_105_41,(8,1,17):C.UVGC_105_42,(8,1,18):C.UVGC_105_43,(8,1,19):C.UVGC_105_44,(8,1,20):C.UVGC_105_45,(8,1,21):C.UVGC_105_46,(8,1,22):C.UVGC_105_47,(8,1,23):C.UVGC_105_48,(6,1,0):C.UVGC_114_159,(6,1,3):C.UVGC_114_160,(6,1,4):C.UVGC_114_161,(6,1,5):C.UVGC_115_179,(6,1,6):C.UVGC_115_180,(6,1,7):C.UVGC_114_163,(6,1,8):C.UVGC_114_164,(6,1,9):C.UVGC_115_181,(6,1,11):C.UVGC_115_182,(6,1,12):C.UVGC_115_183,(6,1,13):C.UVGC_115_184,(6,1,14):C.UVGC_115_185,(6,1,15):C.UVGC_115_186,(6,1,16):C.UVGC_115_187,(6,1,17):C.UVGC_115_188,(6,1,18):C.UVGC_115_189,(6,1,19):C.UVGC_115_190,(6,1,20):C.UVGC_115_191,(6,1,21):C.UVGC_115_192,(6,1,22):C.UVGC_114_177,(6,1,23):C.UVGC_114_178,(7,1,1):C.UVGC_110_133,(7,1,5):C.UVGC_100_1,(7,1,6):C.UVGC_111_136,(7,1,7):C.UVGC_110_134,(5,1,5):C.UVGC_99_1085,(5,1,6):C.UVGC_99_1086,(1,1,5):C.UVGC_99_1085,(1,1,6):C.UVGC_99_1086,(11,1,5):C.UVGC_103_5,(11,1,6):C.UVGC_103_6,(10,1,5):C.UVGC_103_5,(10,1,6):C.UVGC_103_6,(9,1,5):C.UVGC_102_3,(9,1,6):C.UVGC_102_4,(0,2,5):C.UVGC_100_2,(0,2,6):C.UVGC_100_1,(2,2,5):C.UVGC_100_2,(2,2,6):C.UVGC_100_1,(5,2,5):C.UVGC_99_1085,(5,2,6):C.UVGC_99_1086,(1,2,5):C.UVGC_99_1085,(1,2,6):C.UVGC_99_1086,(7,2,0):C.UVGC_114_159,(7,2,3):C.UVGC_114_160,(7,2,4):C.UVGC_114_161,(7,2,5):C.UVGC_104_10,(7,2,6):C.UVGC_114_162,(7,2,7):C.UVGC_114_163,(7,2,8):C.UVGC_114_164,(7,2,9):C.UVGC_114_165,(7,2,11):C.UVGC_114_166,(7,2,12):C.UVGC_114_167,(7,2,13):C.UVGC_114_168,(7,2,14):C.UVGC_114_169,(7,2,15):C.UVGC_114_170,(7,2,16):C.UVGC_114_171,(7,2,17):C.UVGC_114_172,(7,2,18):C.UVGC_114_173,(7,2,19):C.UVGC_114_174,(7,2,20):C.UVGC_114_175,(7,2,21):C.UVGC_114_176,(7,2,22):C.UVGC_114_177,(7,2,23):C.UVGC_114_178,(4,2,5):C.UVGC_99_1085,(4,2,6):C.UVGC_99_1086,(3,2,5):C.UVGC_99_1085,(3,2,6):C.UVGC_99_1086,(8,2,0):C.UVGC_104_7,(8,2,3):C.UVGC_104_8,(8,2,4):C.UVGC_104_9,(8,2,5):C.UVGC_104_10,(8,2,6):C.UVGC_104_11,(8,2,7):C.UVGC_104_12,(8,2,8):C.UVGC_104_13,(8,2,9):C.UVGC_104_14,(8,2,11):C.UVGC_104_15,(8,2,12):C.UVGC_104_16,(8,2,13):C.UVGC_104_17,(8,2,14):C.UVGC_104_18,(8,2,15):C.UVGC_104_19,(8,2,16):C.UVGC_104_20,(8,2,17):C.UVGC_104_21,(8,2,18):C.UVGC_104_22,(8,2,19):C.UVGC_104_23,(8,2,20):C.UVGC_104_24,(8,2,21):C.UVGC_104_25,(8,2,22):C.UVGC_104_26,(8,2,23):C.UVGC_104_27,(6,2,2):C.UVGC_110_133,(6,2,6):C.UVGC_102_3,(6,2,7):C.UVGC_110_134,(6,2,10):C.UVGC_110_135,(11,2,5):C.UVGC_103_5,(11,2,6):C.UVGC_103_6,(10,2,5):C.UVGC_103_5,(10,2,6):C.UVGC_103_6,(9,2,5):C.UVGC_102_3,(9,2,6):C.UVGC_102_4}}
```

# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in [parameters.py](#)

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu}_r',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- [CT\\_vertices.py](#): UV, R2 counter term vertices

- [CT\\_couplings.py](#): couplings for UV and R2 counter terms

```
UVGC_104_23 = Coupling(name = 'UVGC_104_23',
                      value = '-((FRCTdelta $\alpha_s$ s $\sigma$ R*complex(0,1)*G**2)/aS) - 2*FRCTdeltaZxGGxstR*complex(0,1)*G**2 + (complex(0,1)*G**4*invFREps)/(32.*cmath.pi**2)',
                      order = {'QCD':4})
```



# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in [parameters.py](#)

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
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```
UVGC_104_23 = Coupling(name = 'UVGC_104_23',
                      value = '-((FRCTdeltaaSxstR*complex(0,1)*G**2)/aS) - 2*FRCTdeltaZxGGxstR*complex(0,1)*G**2 + (complex(0,1)*G**4*invFREps)/(32.*cmath.pi**2)',
                      order = {'QCD':4})
```

- [CT\\_parameters.py](#): parameters for UV and R2

```
FRCTdeltaZxttLxtG = CTPParameter(name = 'FRCTdeltaZxttLxtG',
                                  type = 'complex',
                                  value = {-1: '-G**2/(6.*cmath.pi**2)', 0: '-G**2/(3.*cmath.pi**2) + (G**2*reglog(MT/MU_R))/(2.*cmath.pi**2)'},
                                  texname = 'FRCTdeltaZxttLxtG')
```

# UFO@NLO

Degrande, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in [parameters.py](#)

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu}_r',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- [CT\\_vertices.py](#): UV, R2 counter term vertices
- [CT\\_couplings.py](#): couplings for UV and R2 counter terms

```
UVGC_104_23 = Coupling(name = 'UVGC_104_23',
                      value = '-((FRCTdeltaXsXstR*complex(0,1)*G**2)/aS) - 2*FRCTdeltaZxGGxstR*complex(0,1)*G**2 + (complex(0,1)*G**4*invFREps)/(32.*cmath.pi**2)',
                      order = {'QCD':4})
```

- [CT\\_parameters.py](#): parameters for UV and R2

```
FRCTdeltaZxttLxtG = CTPParameter(name = 'FRCTdeltaZxttLxtG',
                                 type = 'complex',
                                 value = '-1: -G**2/(6.*cmath.pi**2)', 0: '-G**2/(3.*cmath.pi**2) + (G**2*reglog(MT/MU_R))/(2.*cmath.pi**2)',
                                 texname = 'FRCTdeltaZxttLxtG')
```

coefficient of  $\frac{1}{\epsilon}$

# UFO@NLO

Degrade, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in [parameters.py](#)

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu}_r',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- [CT\\_vertices.py](#): UV, R2 counter term vertices

- [CT\\_couplings.py](#): couplings for UV and R2 counter terms

```
UVGC_104_23 = Coupling(name = 'UVGC_104_23',
                      value = '-((FRCTdeltaXsxtR*complex(0,1)*G**2)/aS) - 2*FRCTdeltaZxGGxstR*complex(0,1)*G**2 + (complex(0,1)*G**4*invFREps)/(32.*cmath.pi**2)',
                      order = {'QCD':4})
```

- [CT\\_parameters.py](#): parameters for UV and R2

```
FRCTdeltaZxttLxtG = CTPParameter(name = 'FRCTdeltaZxttLxtG',
                                  type = 'complex',
                                  value = '-1: -G**2/(6.*cmath.pi**2), 0: -G**2/(3.*cmath.pi**2) + (G**2*reglog(MT/MU_R))/(2.*cmath.pi**2)',
                                  texname = 'FRCTdeltaZxttLxtG')
```

coefficient of  $\frac{1}{\epsilon}$

finite piece



# UFO@NLO

Degrade, Duhr, Fuks, Grellscheid, Hirschi, Mattelaer, Reiter, HSS ... (in preparation)

- Provide renormalization scale in `parameters.py`

```
MU_R = Parameter(name = 'MU_R',
                 nature = 'external',
                 type = 'real',
                 value = 91.188,
                 texname = '\\text{\\mu}_r',
                 lhablock = 'LOOP',
                 lhacode = [1])
```

- `CT_vertices.py`: UV, R2 counter term vertices
- `CT_couplings.py`: couplings for UV and R2 counter terms

```
UVGC_104_23 = Coupling(name = 'UVGC_104_23',
                      value = '-((FRCTdelta $\alpha$ s $\chi$ stR*complex(0,1)*G**2)/aS) - 2*FRCTdelta $\chi$ GG $\chi$ stR*complex(0,1)*G**2 + (complex(0,1)*G**4*invFREps)/(32.*cmath.pi**2)',
                      order = {'QCD':4})
```

- `CT_parameters.py`: parameters for UV and R2

```
FRCTdel FRCTdelta $\chi$ xttl $\chi$ gostL = CTPParameter(name = 'FRCTdelta $\chi$ xttl $\chi$ gostL',
                                           type = 'complex',
                                           value = {0: '(0 if 2*Mgo*MstL + MT**2 >= Mgo**2 + MstL**2 and MT**2 <= (Mgo + MstL)**2 else (0 if Mgo==MstL else (0 if Mgo==MT else (0 if MstL==MT else \
(G**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2))/(12.*cmath.pi**2*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 \
+ (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)) + (G**2*Mgo**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2) \
)/MU_R**2))/(12.*cmath.pi**2*MT**2*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)) - (G**2*MstL**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) \
+ MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2))/(12.*cmath.pi**2*MT**2*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - \
MT**2/MU_R**2)**2)) - (G**2*Mgo**4*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL))/(12.*cm \
ath.pi**2*MT**4*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)) - (G**2*Mgo**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2) \
- MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL))/(6.*cmath.pi**2*MT**4*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 \
- MT**2/MU_R**2)**2)) - (G**2*MstL**4*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL))/(12 \
.*cmath.pi**2*MT**4*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)) - (G**2*Mgo**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2) \
- MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL))/(12.*cmath.pi**2*MT**2*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - \
MT**2/MU_R**2)**2)) + (G**2*MstL**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL))/(12.*cm \
math.pi**2*MT**2*cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)) + ( (0 if Mgo==MstL else (0 if Mgo==MT else (0 if MstL==MT el \
se (G**2*Mgo*MstL**2*(-(MU_R**2*(Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2) + cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)))/(2.*Mgo*MstL \
)))*reglog((MU_R**2*(Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2) + cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)))/(2.*Mgo*MstL) \
)/(12.*cmath.pi**2*MT**2) ) ) if 2*Mgo*MstL + MT**2 >= Mgo**2 + MstL**2 and MT**2 <= (Mgo + MstL)**2 else 0 ) + ( (0 if Mgo==MstL else (0 if Mgo==MT else (0 if MstL==MT else (MU_R**2*G**2* \
Mgo**2*ere((MT**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2) + (-Mgo**2/MU_R**2) + MstL**2/MU_R \
**2)*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL) + (MstL**4/MU_R**4 + (Mgo**2*(Mgo**2/MU_R \
**2 - MT**2/MU_R**2))/MU_R**2 - (MstL**2*((2*Mgo**2)/MU_R**2 + MT**2/MU_R**2))/MU_R**2 + MT**2/MU_R**2))/MU_R**2 + cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - \
MT**2/MU_R**2)**2)))/(2.*Mgo*MstL))/cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)))/(12 \
.*cmath.pi**2*MT**4) - (MU_R**2*G**2*MstL**2*ere((MT**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2) \
)/MU_R**2 + (-Mgo**2/MU_R**2) + MstL**2/MU_R**2)*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)*reglog(Mgo/MstL) + \
(MstL**4/MU_R**4 + (Mgo**2*(Mgo**2/MU_R**2 - MT**2/MU_R**2))/MU_R**2 - (MstL**2*((2*Mgo**2)/MU_R**2 + MT**2/MU_R**2))/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)/MU_R**2 + cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - \
MT**2/MU_R**2)**2)))/(2.*Mgo*MstL))/cmath.sqrt((-4*Mgo**2*MstL**2)/MU_R**4 + (Mgo**2/MU_R**2 + MstL**2/MU_R**2 - MT**2/MU_R**2)**2)))/(12.*cmath.pi**2*MT**4) + (MU_R**2*G**2*ere((MT**2*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + \
MT**2/MU_R**2))/MU_R**2) + (-Mgo**2/MU_R**2) + MstL**2/MU_R**2)*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2) \
)/MU_R**2 + (-Mgo**2/MU_R**2) + MstL**2/MU_R**2)*cmath.sqrt(MstL**4/MU_R**4 + (-Mgo**2/MU_R**2) + MT**2/MU_R**2)**2 - (2*MstL**2*(Mgo**2/MU_R**2 + MT**2/MU_R**2))/MU_R**2)
```





# APPLICATION 1: A STOP SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudom, HSS (PRD'15)

Available models

| Description                                  | Contact     | Reference                                | FeynRules model files | UFO libraries      | Validation material   |
|--|-------------|--|-----------------------|--------------------|---|
| Dark matter simplified models (more details) | K. Mawatari | -  | -                     | DMSimp_UFO.2.zip   | -   |
| Gluino pair production (SUSY-QCD)            | B. Fuks     | ⇒ arXiv:1510.00391                       | -                     | susyqcd_ufo.tgz    | All figures available from the arxiv                          |
| Higgs characterisation (more details)        | K. Mawatari | ⇒ arXiv:1311.1829 ,<br>⇒ arXiv:1407.5089 | -                     | HC_NLO_X0_UFO.zip  | -   |
| Inclusive sgluon pair production             | B. Fuks     | ⇒ arXiv:1412.5589                        | sgluons.fr            | sgluons_ufo.tgz    | sgluons_validation.pdf ;<br>sgluons_validation_root.tgz       |
| Stop pair → t tbar → missing energy          | B. Fuks     | ⇒ arXiv:1412.5589                        | stop_ttmet.fr         | stop_ttmet_ufo.tgz | stop_ttmet_validation.pdf ;<br>stop_ttmet_validation_root.tgz |
| Two-Higgs-Doublet Model (more details)       | C. Degrande | ⇒ arXiv:1406.3030                        | -                     | 2HDM_NLO           | -   |

1. Download UFO from FR Wiki
2. Put the UFO model in models
3. ./bin/mg5\_aMC
4. > import model stop\_ttmet\_ufo
5. > generate p p > sig3 sig3~ [QCD]
6. > output pp2t|t|QCD
7. > launch

## ◆ The stop ( $\sigma_3$ ) / bino ( $\chi$ ) model

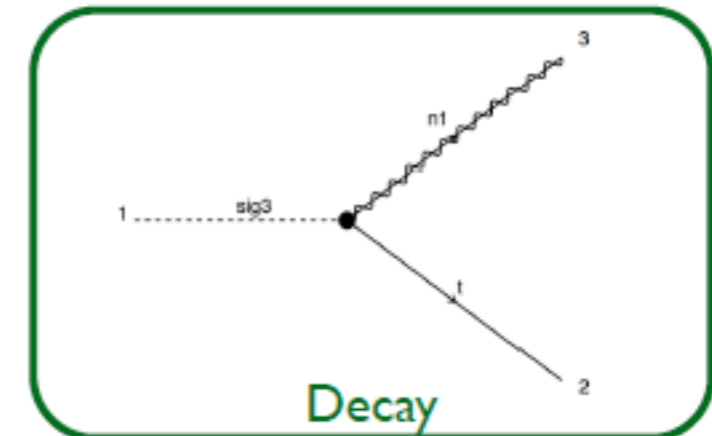
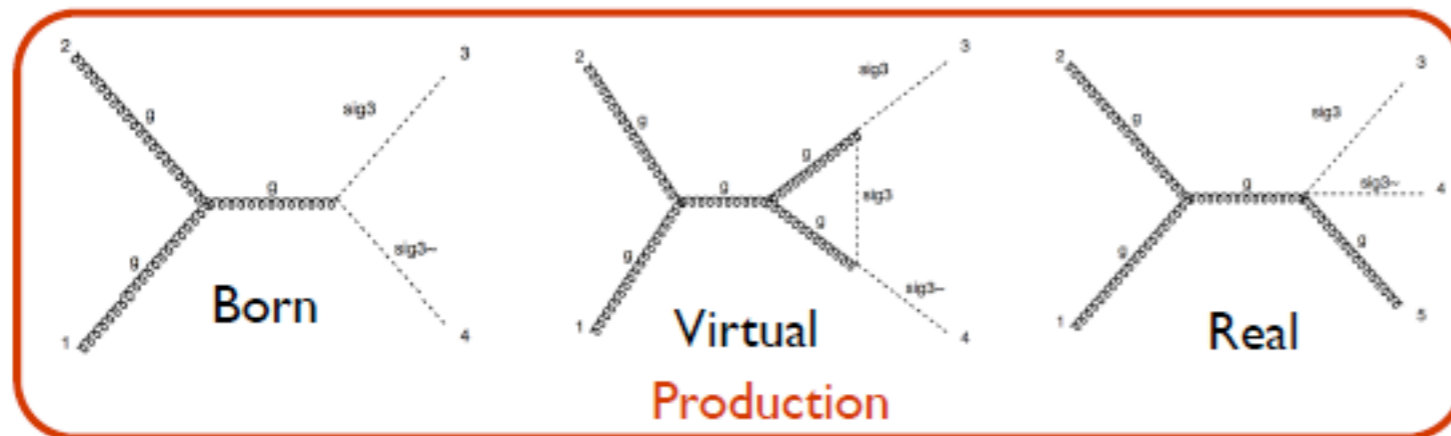
$$\mathcal{L}_3 = \underbrace{D_\mu \sigma_3^\dagger D^\mu \sigma_3 - m_3^2 \sigma_3^\dagger \sigma_3}_{\text{Production}} + \underbrace{\frac{i}{2} \bar{\chi} \not{\partial} \chi - \frac{1}{2} m_\chi \bar{\chi} \chi + \left[ \sigma_3 \bar{t} (\tilde{g}_L P_L + \tilde{g}_R P_R) \chi + \text{h.c.} \right]}_{\text{Decay}}$$

Production

Decay

- ❖ One scalar field in the fundamental representation ( $\sigma_3$ )
- ❖ One gauge-singlet Majorana fermion ( $\chi$ ) coupling the stop to the top

## ◆ Representative Feynman diagrams (yielding a top-antitop plus missing energy signature)





# APPLICATION 1: A STOP SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudome, HSS (PRD'15)

## ◆ UV behavior (on-shell scheme, zero-momentum subtraction for $\alpha_s$ )

Analytical validation

### ♣ Analytical checks are important (the fully automated approach is new)

$$\delta Z_g = \delta Z_g^{(SM)} - \frac{g_s^2}{96\pi^2} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_3^2}{\mu_R^2} \right]$$

$$\delta Z_{\sigma_3} = 0 \quad \text{and} \quad \delta m_3^2 = -\frac{g_s^2 m_3^2}{12\pi^2} \left[ \frac{3}{\bar{\epsilon}} + 7 - 3 \log \frac{m_3^2}{\mu_R^2} \right]$$

$$\frac{\delta \alpha_s}{\alpha_s} = \frac{\alpha_s}{2\pi\bar{\epsilon}} \left[ \frac{n_f}{3} - \frac{11}{2} \right] + \frac{\alpha_s}{6\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_t^2}{\mu_R^2} \right] + \frac{\alpha_s}{24\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_3^2}{\mu_R^2} \right]$$

$$R_2^{\sigma_3^\dagger \sigma_3} = \frac{ig_s^2}{72\pi^2} \delta_{c_1 c_2} [3m_3^2 - p^2]$$

$$R_2^{g\sigma_3^\dagger \sigma_3} = \frac{53ig_s^3}{576\pi^2} T_{c_2 c_3}^{a_1} (p_2 - p_3)^{\mu_1}$$

$$R_2^{gg\sigma_3^\dagger \sigma_3} = \frac{ig_s^4}{1152\pi^2} \eta^{\mu_1 \mu_2} [3\delta^{a_1 a_2} - 187\{T^{a_1}, T^{a_2}\}]_{c_3 c_4}$$

## ◆ Total rates at 8 TeV and 13 TeV

Numerical validation

| $m_3$ [GeV] | $\sigma^{\text{LO}}$ [pb]                            | $\sigma^{\text{NLO}}$ [pb]   | $\sigma^{\text{LO}}$ [pb]                            | $\sigma^{\text{NLO}}$ [pb]                                      |
|-------------|--|--|--|---|
| 100         | $3.893 \pm 0.0095 \cdot 10^2$<br>+34.2%<br>-23.9%    | $5.548 \pm 0.018 \cdot 10^2$<br>+14.9% +1.6%<br>-13.5% -1.6%       | $1.066 \pm 0.0025 \cdot 10^3$<br>+29.1%<br>-21.4%    | $1.497 \pm 0.0054 \cdot 10^3$<br>+14.1% +1.2%<br>-12.1% -1.2%   |
| 250         | $4.118 \pm 0.0096 \cdot 10^0$<br>+40.4%<br>-27.2%    | $5.503 \pm 0.017 \cdot 10^0$<br>+13.1% +3.7%<br>-13.7% -3.7%       | $1.553 \pm 0.0037 \cdot 10^1$<br>+35.2%<br>-24.8%    | $2.156 \pm 0.0067 \cdot 10^1$<br>+12.1% +2.4%<br>-12.3% -2.4%   |
| 500         | $6.594 \pm 0.016 \cdot 10^{-2}$<br>+45.5%<br>-29.1%  | $7.764 \pm 0.025 \cdot 10^{-2}$<br>+12.1% +6.7%<br>-14.1% -6.7%    | $3.890 \pm 0.0093 \cdot 10^{-1}$<br>+39.6%<br>-26.4% | $5.062 \pm 0.015 \cdot 10^{-1}$<br>+11.2% +4.4%<br>-12.8% -4.4% |
| 750         | $3.504 \pm 0.0084 \cdot 10^{-3}$<br>+48.8%<br>-30.5% | $3.699 \pm 0.012 \cdot 10^{-3}$<br>+12.3% +10.2%<br>-14.6% -10.2%  | $3.306 \pm 0.0081 \cdot 10^{-2}$<br>+41.8%<br>-27.5% | $4.001 \pm 0.012 \cdot 10^{-2}$<br>+10.8% +6.1%<br>-12.9% -6.1% |
| 1000        | $2.875 \pm 0.0067 \cdot 10^{-4}$<br>+51.5%<br>-31.5% | $2.775 \pm 0.0087 \cdot 10^{-4}$<br>+13.1% +15.5%<br>-15.2% -15.5% | $4.614 \pm 0.011 \cdot 10^{-3}$<br>+43.6%<br>-28.3%  | $5.219 \pm 0.016 \cdot 10^{-3}$<br>+10.9% +7.9%<br>-13.2% -7.9% |

8 TeV

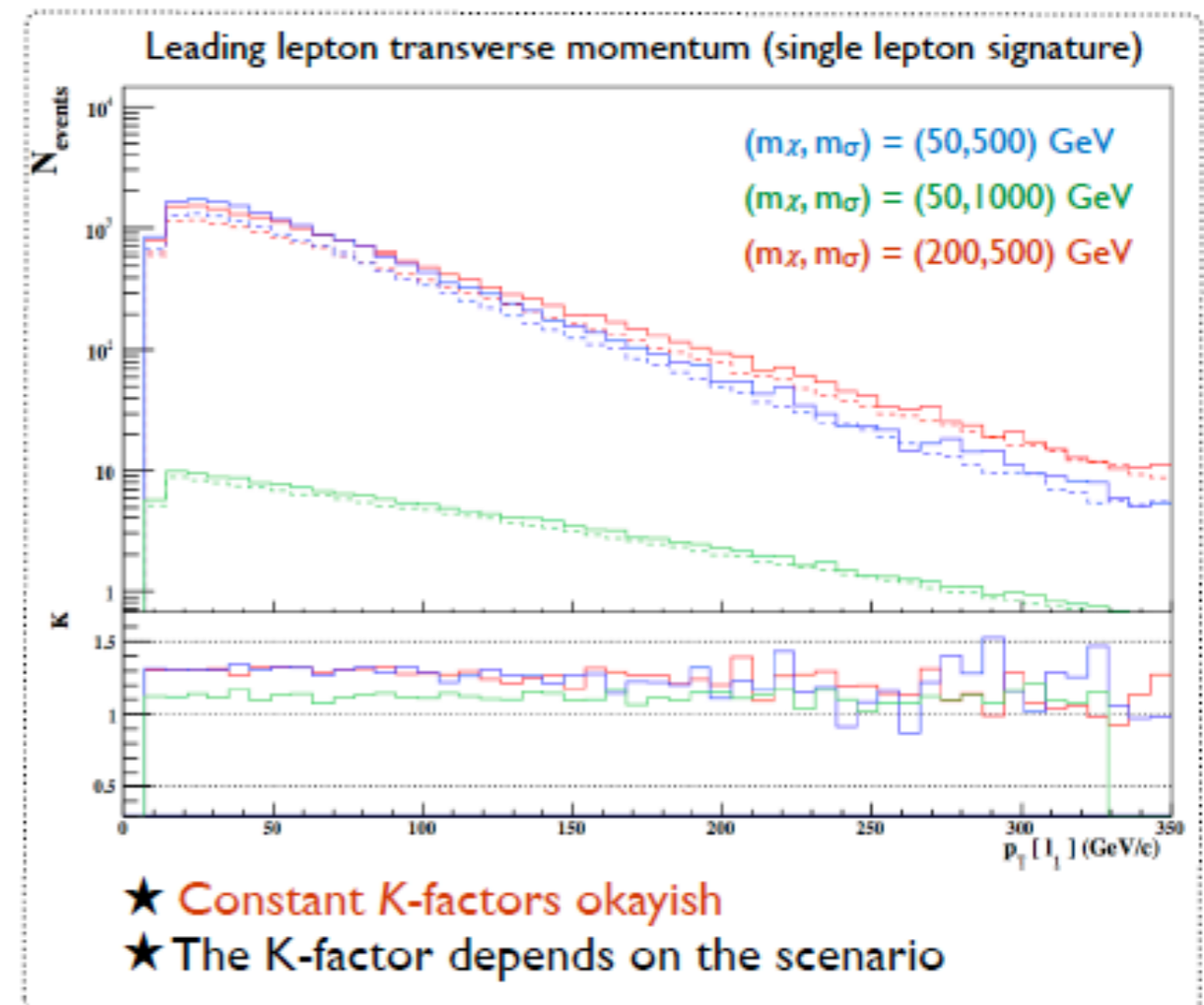
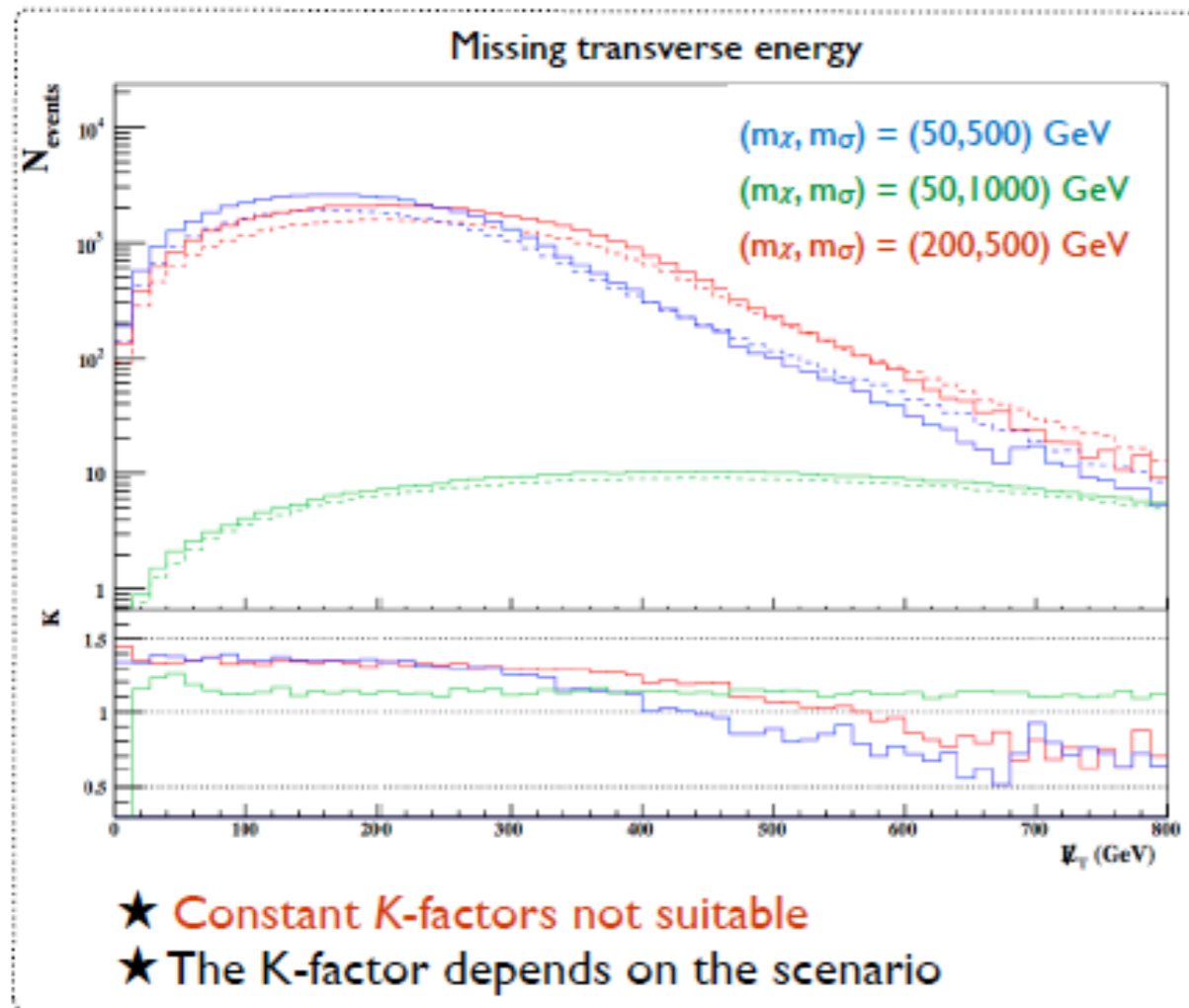
13 TeV

- ♣ NNPDF2.3; scales set to the stop mass
- ♣ Agrees with PROSPINO [ Beenakker, Kramer, Plehn, Spira & Zerwas (NPB'98) ]
- ♣ Scale varied by a factor of two up and down
- ♣ PDF variations obtained with the 100 NNPDF replica provided with the central set of densities

# APPLICATION 1: A STOP SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudom, HSS (PRD'15)

- ◆ NLO matrix elements matched to parton showering: differential distributions
- ❖ Test case: 500/1000 GeV stop; 50/200 GeV bino; 13 TeV collisions
- ❖ Standard coupling strengths for a maximally mixing stop and a bino
- ❖ Shower: PYTHIA 8.2 [ Sjostrand, Mrenna & Skands (CPC'08) ]
- ❖ Jet reconstruction: anti- $k_T$  & FASTJET [ Cacciari, Salam & Soyez (JHEP'08, EPJC'12) ]
- ❖ Analysis (single lepton case) & figures: MADANALYSIS 5 [ Conte, BF, Serret (CPC'13) ]



# APPLICATION 2: A SGLUON SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudome, HSS (PRD'15)

Available models

| Description                                  | Contact     | Reference  | FeynRules model files | UFO libraries      | Validation material   |
|--|-------------|--|-----------------------|--------------------|---|
| Dark matter simplified models (more details) | K. Mawatari | -  | -                     | DMSimp_UFO.2.zip   | -   |
| Glino pair production (SUSY-QCD)             | B. Fuks     | <a href="https://arxiv.org/abs/1510.00391">arXiv:1510.00391</a>  | -                     | susyqcd_ufo.tgz    | All figures available from the arxiv                          |
| Higgs characterisation (more details)        | K. Mawatari | <a href="https://arxiv.org/abs/1311.1829">arXiv:1311.1829</a> ,<br><a href="https://arxiv.org/abs/1407.5089">arXiv:1407.5089</a> | -                     | HC_NLO_X0_UFO.zip  | -   |
| Inclusive sgluon pair production             | B. Fuks     | <a href="https://arxiv.org/abs/1412.5589">arXiv:1412.5589</a>  | sgluons.fr            | sgluons_ufo.tgz    | sgluons_validation.pdf ;<br>sgluons_validation_root.tgz       |
| Stop pair → t tbar + missing energy          | B. Fuks     | <a href="https://arxiv.org/abs/1412.5589">arXiv:1412.5589</a>  | stop_ttmet.fr         | stop_ttmet_ufo.tgz | stop_ttmet_validation.pdf ;<br>stop_ttmet_validation_root.tgz |
| Two-Higgs-Doublet Model (more details)       | C. Degrande | <a href="https://arxiv.org/abs/1406.3030">arXiv:1406.3030</a>  | -                     | ZHDM_NLO           | -   |

1. Download UFO from FR Wiki
2. Put the UFO model in models
3. ./bin/mg5\_aMC
4. > import model sgluon\_ufo
5. > generate p p > sig8 sig8~ [QCD]
6. > output pp2sig8sig8QCD
7. > launch

## ◆ The sgluon ( $\sigma_8$ ) model

$$\mathcal{L}_8 = \underbrace{\frac{1}{2} D_\mu \sigma_8 D^\mu \sigma_8 - \frac{1}{2} m_8^2 \sigma_8 \sigma_8}_{\text{Production}} + \underbrace{\frac{\hat{g}g}{\Lambda} \sigma_8 G_{\mu\nu} G^{\mu\nu} + \sum_{q=u,d} \left[ \sigma_8 \bar{q} (\hat{g}_q^L P_L + \hat{g}_q^R P_R) q + \text{h.c.} \right]}_{\text{Decay}}$$

- ❖ One scalar field in the adjoint representation ( $\sigma_8$ )
- ❖ Effective couplings ( $g$ ): **only for the decay that is enforced to be at the leading order**
- ❖  $g$  couplings at NLO: a consistent effective theory is required for a proper renormalization

## ◆ UV behavior (on-shell scheme, zero-momentum subtraction for $\alpha_s$ )

- ❖ Analytical checks

$$\delta Z_g = \delta Z_g^{(SM)} - \frac{g_s^2}{32\pi^2} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_8^2}{\mu_R^2} \right],$$

$$\delta Z_{\sigma_8} = 0 \quad \text{and} \quad \delta m_8^2 = -\frac{3g_s^2 m_8^2}{16\pi^2} \left[ \frac{3}{\bar{\epsilon}} + 7 - 3 \log \frac{m_8^2}{\mu_R^2} \right]$$

$$\frac{\delta \alpha_s}{\alpha_s} = \frac{\alpha_s}{2\pi\bar{\epsilon}} \left[ \frac{n_f}{3} - \frac{11}{2} \right] + \frac{\alpha_s}{6\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_t^2}{\mu_R^2} \right] + \frac{\alpha_s}{8\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_8^2}{\mu_R^2} \right]$$

$$\begin{aligned} R_2^{\sigma_8 \sigma_8} &= \frac{ig_s^2}{32\pi^2} \delta_{a_1 a_2} \left[ 3m_8^2 - p^2 \right], \\ R_2^{g \sigma_8 \sigma_8} &= \frac{7g_s^3}{64\pi^2} f_{a_1 a_2 a_3} (p_2 - p_3)^{\mu_1}, \\ R_2^{gg \sigma_8 \sigma_8} &= \frac{ig_s^4}{384\pi^2} \eta^{\mu_1 \mu_2} \left[ 72(d_{a_1 a_4 e} d_{a_2 a_3 e} + d_{a_1 a_3 e} d_{a_2 a_4 e}) \right. \\ &\quad \left. - 141 d_{a_1 a_2 e} d_{a_3 a_4 e} - 92 \delta_{a_1 a_2} \delta_{a_3 a_4} \right. \\ &\quad \left. + 50(\delta_{a_1 a_3} \delta_{a_2 a_4} + \delta_{a_1 a_4} \delta_{a_2 a_3}) \right], \end{aligned}$$



# APPLICATION 2: A SGLUON SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudome, HSS (PRD'15)

Available models

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| Higgs characterisation (more details)        | K. Mawatari | <a href="https://arxiv.org/abs/1311.1829">arXiv:1311.1829</a> ,<br><a href="https://arxiv.org/abs/1407.5089">arXiv:1407.5089</a> | -                     | HC_NLO_X0_UFO.zip  | -   |
| Inclusive sgluon pair production             | B. Fuks     | <a href="https://arxiv.org/abs/1412.5589">arXiv:1412.5589</a>  | sgluons.fr            | sgluons_ufo.tgz    | sgluons_validation.pdf ;<br>sgluons_validation_root.tgz       |
| Stop pair → t tbar + missing energy          | B. Fuks     | <a href="https://arxiv.org/abs/1412.5589">arXiv:1412.5589</a>  | stop_ttmet.fr         | stop_ttmet_ufo.tgz | stop_ttmet_validation.pdf ;<br>stop_ttmet_validation_root.tgz |
| Two-Higgs-Doublet Model (more details)       | C. Degrande | <a href="https://arxiv.org/abs/1406.3030">arXiv:1406.3030</a>  | -                     | 2HDM_NLO           | -   |

1. Download UFO from FR Wiki
2. Put the UFO model in models
3. ./bin/mg5\_aMC
4. > import model sgluon\_ufo
5. > generate p p > sig8 sig8~ [QCD]
6. > output pp2sig8sig8QCD
7. > launch

## Non-renormalizable operator

### ◆ The sgluon ( $\sigma_8$ ) model

$$\mathcal{L}_8 = \underbrace{\frac{1}{2} D_\mu \sigma_8 D^\mu \sigma_8 - \frac{1}{2} m_8^2 \sigma_8 \sigma_8}_{\text{Production}} + \underbrace{\frac{\hat{g}g}{\Lambda} \sigma_8 G_{\mu\nu} G^{\mu\nu} + \sum_{q=u,d} [\sigma_8 \bar{q} (\hat{g}_q^L P_L + \hat{g}_q^R P_R) q + \text{h.c.}]}_{\text{Decay}}$$

- ❖ One scalar field in the adjoint representation ( $\sigma_8$ )
- ❖ Effective couplings ( $g$ ): **only for the decay that is enforced to be at the leading order**
- ❖  $g$  couplings at NLO: a consistent effective theory is required for a proper renormalization

### ◆ UV behavior (on-shell scheme, zero-momentum subtraction for $\alpha_s$ )

- ❖ Analytical checks

$$\delta Z_g = \delta Z_g^{(SM)} - \frac{g_s^2}{32\pi^2} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_8^2}{\mu_R^2} \right],$$

$$\delta Z_{\sigma_8} = 0 \quad \text{and} \quad \delta m_8^2 = -\frac{3g_s^2 m_8^2}{16\pi^2} \left[ \frac{3}{\bar{\epsilon}} + 7 - 3 \log \frac{m_8^2}{\mu_R^2} \right]$$

$$\frac{\delta \alpha_s}{\alpha_s} = \frac{\alpha_s}{2\pi\bar{\epsilon}} \left[ \frac{n_f}{3} - \frac{11}{2} \right] + \frac{\alpha_s}{6\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_t^2}{\mu_R^2} \right] + \frac{\alpha_s}{8\pi} \left[ \frac{1}{\bar{\epsilon}} - \log \frac{m_8^2}{\mu_R^2} \right]$$

$$R_2^{\sigma_8 \sigma_8} = \frac{ig_s^2}{32\pi^2} \delta_{a_1 a_2} [3m_8^2 - p^2],$$

$$R_2^{g\sigma_8 \sigma_8} = \frac{7g_s^3}{64\pi^2} f_{a_1 a_2 a_3} (p_2 - p_3)^{\mu_1},$$

$$R_2^{gg\sigma_8 \sigma_8} = \frac{ig_s^4}{384\pi^2} \eta^{\mu_1 \mu_2} \left[ 72(d_{a_1 a_4 e} d_{a_2 a_3 e} + d_{a_1 a_3 e} d_{a_2 a_4 e}) - 141 d_{a_1 a_2 e} d_{a_3 a_4 e} - 92 \delta_{a_1 a_2} \delta_{a_3 a_4} + 50(\delta_{a_1 a_3} \delta_{a_2 a_4} + \delta_{a_1 a_4} \delta_{a_2 a_3}) \right],$$



# APPLICATION 2: A SGLUON SIMPLIFIED MODEL

Degrande, Fuks, Hirschi, Proudoum, HSS (PRD'15)

## ◆ Total rates at 8 TeV and 13 TeV

Numerically validated

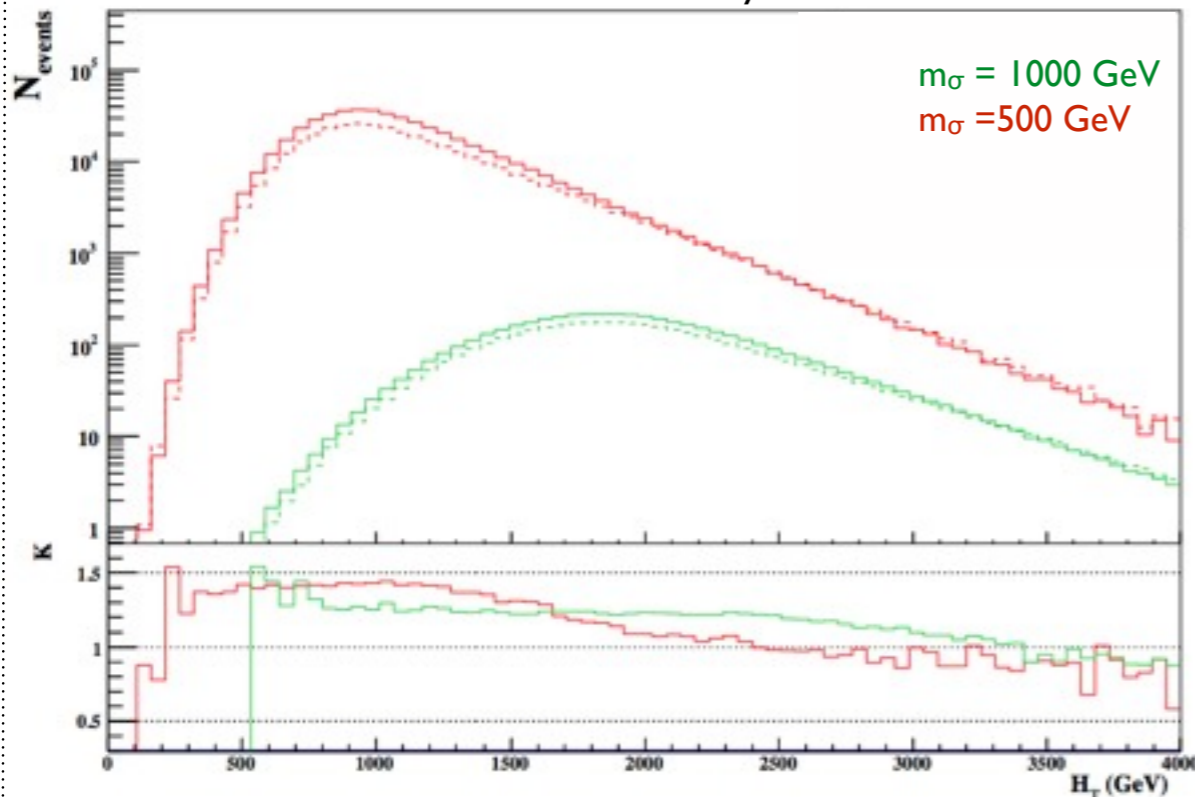
| $m_s$ [GeV] | $\sigma^{\text{LO}}$ [pb]   | $\sigma^{\text{NLO}}$ [pb]  | $\sigma^{\text{LO}}$ [pb]   | $\sigma^{\text{NLO}}$ [pb]   |
|-------------|---|---|---|--|
| 100         | $3.854 \pm 0.0094 \cdot 10^3$ <sup>+34.4%</sup><br><sub>-24.1%</sub>    | $5.573 \pm 0.02 \cdot 10^3$ <sup>+14.9%</sup> <sup>+1.6%</sup><br><sub>-13.6%</sub> <sub>-1.6%</sub>        | $1.056 \pm 0.0029 \cdot 10^4$ <sup>+29.2%</sup><br><sub>-21.5%</sub>    | $1.470 \pm 0.0058 \cdot 10^4$ <sup>+13.6%</sup> <sup>+1.2%</sup><br><sub>-11.9%</sub> <sub>-1.2%</sub>   |
| 250         | $3.889 \pm 0.010 \cdot 10^1$ <sup>+41.3%</sup><br><sub>-27.7%</sub>     | $5.432 \pm 0.019 \cdot 10^1$ <sup>+14.5%</sup> <sup>+3.9%</sup><br><sub>-14.6%</sub> <sub>-3.9%</sub>       | $1.504 \pm 0.0034 \cdot 10^2$ <sup>+35.7%</sup><br><sub>-25.1%</sub>    | $2.145 \pm 0.0077 \cdot 10^2$ <sup>+12.9%</sup> <sup>+2.5%</sup><br><sub>-12.9%</sub> <sub>-2.5%</sub>   |
| 500         | $5.878 \pm 0.015 \cdot 10^{-1}$ <sup>+47.6%</sup><br><sub>-30.0%</sub>  | $7.431 \pm 0.028 \cdot 10^{-1}$ <sup>+15.8%</sup> <sup>+7.6%</sup><br><sub>-16.2%</sub> <sub>-7.6%</sub>    | $3.619 \pm 0.0079 \cdot 10^0$ <sup>+40.8%</sup><br><sub>-27.0%</sub>    | $4.977 \pm 0.018 \cdot 10^0$ <sup>+13.3%</sup> <sup>+4.7%</sup><br><sub>-14.1%</sub> <sub>-4.7%</sub>    |
| 750         | $2.977 \pm 0.0073 \cdot 10^{-2}$ <sup>+52.0%</sup><br><sub>-31.9%</sub> | $3.353 \pm 0.012 \cdot 10^{-2}$ <sup>+17.2%</sup> <sup>+12.1%</sup><br><sub>-17.3%</sub> <sub>-12.1%</sub>  | $2.951 \pm 0.0065 \cdot 10^{-1}$ <sup>+43.6%</sup><br><sub>-28.4%</sub> | $3.817 \pm 0.015 \cdot 10^{-1}$ <sup>+14.0%</sup> <sup>+6.9%</sup><br><sub>-14.8%</sub> <sub>-6.9%</sub> |
| 1000        | $2.328 \pm 0.0058 \cdot 10^{-3}$ <sup>+55.9%</sup><br><sub>-33.4%</sub> | $2.398 \pm 0.0099 \cdot 10^{-3}$ <sup>+19.0%</sup> <sup>+19.1%</sup><br><sub>-18.4%</sub> <sub>-19.1%</sub> | $3.983 \pm 0.0087 \cdot 10^{-2}$ <sup>+46.1%</sup><br><sub>-29.5%</sub> | $4.822 \pm 0.017 \cdot 10^{-2}$ <sup>+15.1%</sup> <sup>+9.3%</sup><br><sub>-15.6%</sub> <sub>-9.3%</sub> |

8 TeV

13 TeV

- ❖ NNPDF2.3; scales set to the sgluon mass; uncertainties evaluated as for the stop case
- ❖ Validation with MADGOLEM
  - ★ Discrepancy of a 1-3 % for central scale choices; larger for other scale setups
  - ★ MADGOLEM is overestimating the numerical uncertainties

Hadronic activity  $H_T$



## ◆ Differential distributions at NLO

- ❖ Test case: 500/1000 GeV sgluons; 13 TeV collisions
- ❖ Tetratop decays
- ❖ Shower: PYTHIA 8.2 [Sjostrand, Mrenna & Skands]
- ❖ Jet reconstruction: anti- $k_T$  & FASTJET [Cacciari, Salam & Soyez (JHEP'08, EPJC'12)]
- ❖ Analysis & figure: MADANALYSIS 5 [Conte, BF, Serret]

## ◆ SUSY QCD: Production of gluino-pair

$$\mathcal{L}_{\text{SQCD}} = D_\mu \tilde{q}_L^\dagger D^\mu \tilde{q}_L + D_\mu \tilde{q}_R^\dagger D^\mu \tilde{q}_R + \frac{i}{2} \bar{g} \not{D} \tilde{g} - m_{\tilde{q}_L}^2 \tilde{q}_L^\dagger \tilde{q}_L - m_{\tilde{q}_R}^2 \tilde{q}_R^\dagger \tilde{q}_R - \frac{1}{2} m_{\tilde{g}} \bar{g} \tilde{g}$$

$$+ \sqrt{2} g_s \left[ -\tilde{q}_L^\dagger T (\bar{g} P_L q) + (\bar{q} P_L \tilde{g}) T \tilde{q}_R + \text{h.c.} \right] - \frac{g_s^2}{2} \left[ \tilde{q}_R^\dagger T \tilde{q}_R - \tilde{q}_L^\dagger T \tilde{q}_L \right] \left[ \tilde{q}_R^\dagger T \tilde{q}_R - \tilde{q}_L^\dagger T \tilde{q}_L \right]$$

- ❖ Besides new UV and R2 (I will not listed here), we also need some special counter terms
- ❖ Mixing angle renormalization (mass and wavefunction)

$$\begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \rightarrow \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} + \frac{1}{2} \begin{pmatrix} \delta Z_{\tilde{t}_L} & \delta Z_{\tilde{t},\text{LR}} \\ \delta Z_{\tilde{t},\text{RL}} & \delta Z_{\tilde{t}_R} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

$$\delta \mathcal{L}_{\text{off}} = -\delta m_{\tilde{t},\text{LR}}^2 (\tilde{t}_L^\dagger \tilde{t}_R + \tilde{t}_R^\dagger \tilde{t}_L)$$

- ❖ SUSY restoring counter terms

$$\mathcal{L}_{\text{SCT}} = \sqrt{2} g_s \frac{\alpha_s}{3\pi} \left[ -\tilde{q}_L^\dagger T_a (\bar{g}^a P_L q) + (\bar{q} P_L \tilde{g}^a) T_a \tilde{q}_R + \text{h.c.} \right]$$

$$+ \frac{g_s^2}{2} \frac{\alpha_s}{4\pi} \left[ \tilde{q}_R^\dagger \{T_a, T_b\} \tilde{q}_R + \tilde{q}_L^\dagger \{T_a, T_b\} \tilde{q}_L \right] \times \left[ \tilde{q}_R^\dagger \{T^a, T^b\} \tilde{q}_R + \tilde{q}_L^\dagger \{T^a, T^b\} \tilde{q}_L \right]$$

$$- \frac{g_s^2}{2} \frac{\alpha_s}{4\pi} \left[ \tilde{q}_R^\dagger T_a \tilde{q}_R - \tilde{q}_L^\dagger T_a \tilde{q}_L \right] \left[ \tilde{q}_R^\dagger T^a \tilde{q}_R - \tilde{q}_L^\dagger T^a \tilde{q}_L \right]$$

## ◆ Decay of gluino

$$\mathcal{L}_{\text{decay}} = \frac{i}{2} \bar{\chi} \not{\partial} \chi - \frac{1}{2} m_\chi \bar{\chi} \chi + \sqrt{2} g' \left[ -\tilde{q}_L^\dagger Y_q (\bar{\chi} P_L q) + (\bar{q} P_L \chi) Y_q \tilde{q}_R + \text{h.c.} \right]$$

Degrande, Fuks, Hirschi, Proudom, HSS (arXiv:1510.00391)

## Majorana: fermion-flow violation

### ◆ SUSY QCD: Production of gluino-pair

$$\mathcal{L}_{\text{SQCD}} = D_\mu \tilde{q}_L^\dagger D^\mu \tilde{q}_L + D_\mu \tilde{q}_R^\dagger D^\mu \tilde{q}_R + \frac{i}{2} \tilde{g} \not{D} \tilde{g} - m_{\tilde{q}_L}^2 \tilde{q}_L^\dagger \tilde{q}_L - m_{\tilde{q}_R}^2 \tilde{q}_R^\dagger \tilde{q}_R - \frac{1}{2} m_{\tilde{g}} \tilde{g} \tilde{g} \\ + \sqrt{2} g_s \left[ -\tilde{q}_L^\dagger T(\tilde{g} P_L q) + (\bar{q} P_L \tilde{g}) T \tilde{q}_R + \text{h.c.} \right] - \frac{g_s^2}{2} \left[ \tilde{q}_R^\dagger T \tilde{q}_R - \tilde{q}_L^\dagger T \tilde{q}_L \right] \left[ \tilde{q}_R^\dagger T \tilde{q}_R - \tilde{q}_L^\dagger T \tilde{q}_L \right]$$

- ❖ Besides new UV and R2 (I will not listed here), we also need some special counter terms
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$$\begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \rightarrow \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} + \frac{1}{2} \begin{pmatrix} \delta Z_{\tilde{t}_L} & \delta Z_{\tilde{t},\text{LR}} \\ \delta Z_{\tilde{t},\text{RL}} & \delta Z_{\tilde{t}_R} \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

$$\delta \mathcal{L}_{\text{off}} = -\delta m_{\tilde{t},\text{LR}}^2 (\tilde{t}_L^\dagger \tilde{t}_R + \tilde{t}_R^\dagger \tilde{t}_L)$$

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$$\mathcal{L}_{\text{SCT}} = \sqrt{2} g_s \frac{\alpha_s}{3\pi} \left[ -\tilde{q}_L^\dagger T_a (\tilde{g}^a P_L q) + (\bar{q} P_L \tilde{g}^a) T_a \tilde{q}_R + \text{h.c.} \right] \\ + \frac{g_s^2}{2} \frac{\alpha_s}{4\pi} \left[ \tilde{q}_R^\dagger \{T_a, T_b\} \tilde{q}_R + \tilde{q}_L^\dagger \{T_a, T_b\} \tilde{q}_L \right] \times \left[ \tilde{q}_R^\dagger \{T^a, T^b\} \tilde{q}_R + \tilde{q}_L^\dagger \{T^a, T^b\} \tilde{q}_L \right] \\ - \frac{g_s^2}{2} \frac{\alpha_s}{4\pi} \left[ \tilde{q}_R^\dagger T_a \tilde{q}_R - \tilde{q}_L^\dagger T_a \tilde{q}_L \right] \left[ \tilde{q}_R^\dagger T^a \tilde{q}_R - \tilde{q}_L^\dagger T^a \tilde{q}_L \right]$$

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$$\mathcal{L}_{\text{decay}} = \frac{i}{2} \bar{\chi} \not{\partial} \chi - \frac{1}{2} m_\chi \bar{\chi} \chi + \sqrt{2} g' \left[ -\tilde{q}_L^\dagger Y_q (\bar{\chi} P_L q) + (\bar{q} P_L \chi) Y_q \tilde{q}_R + \text{h.c.} \right]$$



# APPLICATION 3: GLUINO-PAIR IN SUSY QCD



Degrande, Fuks, Hirschi, Proudome, HSS (arXiv:1510.00391)

## Available models

| Description  | Contact     | Reference  | FeynRules model files         | UFO libraries                      | Validation material   |
|--|-------------|--|-------------------------------|------------------------------------|---|
| Dark matter simplified models ( <a href="#">more details</a> ) | K. Mawatari | -  | -                             | <a href="#">DMsimp_UFO.2.zip</a>   | -   |
| Glino pair production (SUSY-QCD)                               | B. Fuks     | <a href="#">arXiv:1510.00391</a>                                     | -                             | <a href="#">susyqcd_ufo.tgz</a>    | All figures available from the arxiv  |
| Higgs characterisation ( <a href="#">more details</a> )        | K. Mawatari | <a href="#">arXiv:1311.1829</a> ,<br><a href="#">arXiv:1407.5089</a> | -                             | <a href="#">HC_NLO_X0_UFO.zip</a>  | -   |
| Inclusive sgluon pair production                               | B. Fuks     | <a href="#">arXiv:1412.5589</a>                                      | <a href="#">sgluons.fr</a>    | <a href="#">sgluons_ufo.tgz</a>    | <a href="#">sgluons_validation.pdf</a> ;<br><a href="#">sgluons_validation_root.tgz</a>       |
| Stop pair -> t tbar + missing energy                           | B. Fuks     | <a href="#">arXiv:1412.5589</a>                                      | <a href="#">stop_ttmet.fr</a> | <a href="#">stop_ttmet_ufo.tgz</a> | <a href="#">stop_ttmet_validation.pdf</a> ;<br><a href="#">stop_ttmet_validation_root.tgz</a> |
| Two-Higgs-Doublet Model ( <a href="#">more details</a> )       | C. Degrande | <a href="#">arXiv:1406.3030</a>                                      | -                             | <a href="#">2HDM_NLO</a>           | -   |

1. Download UFO from FR Wiki
2. Put the UFO model in models
3. `./bin/mg5_aMC`
4. `> import model susyqcd_ufo`
5. `> generate p p > go go [QCD]`
6. `> output pp2gogoQCD`
7. `> launch`

Degrande, Fuks, Hirschi, Proudom, HSS (arXiv:1510.00391)

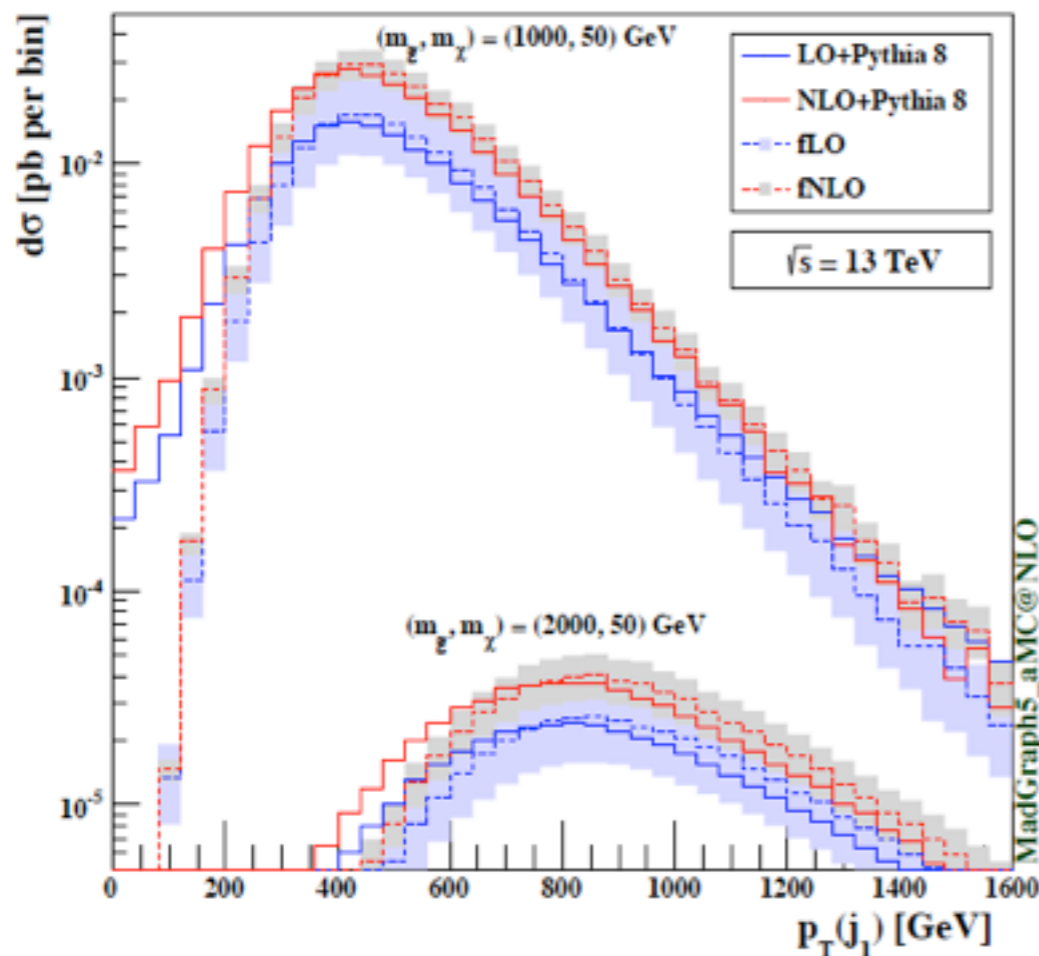
## Splitting SUSY

Numerically validated

◆ Total rates at 8 TeV and 13 TeV

| $m_{\tilde{g}}$ [GeV] | $\sigma^{\text{LO}}$ [pb]                            | $\sigma^{\text{NLO}}$ [pb]                           |
|-----------------------|--|--|
| 200                   | $2104^{+30.3\%+14.0\%}_{-21.9\%-14.0\%}$             | $3183^{+10.8\%+1.8\%}_{-11.6\%-1.8\%}$               |
| 500                   | $15.46^{+34.7\%+19.5\%}_{-24.1\%-19.5\%}$            | $24.90^{+12.5\%+3.7\%}_{-13.4\%-3.7\%}$              |
| 750                   | $1.206^{+35.9\%+23.5\%}_{-24.6\%-23.5\%}$            | $2.009^{+13.5\%+5.5\%}_{-14.1\%-5.5\%}$              |
| 1000                  | $1.608 \cdot 10^{-1+36.3\%+26.4\%}_{-24.8\%-26.4\%}$ | $2.743 \cdot 10^{-1+14.4\%+7.3\%}_{-14.8\%-7.3\%}$   |
| 1500                  | $6.264 \cdot 10^{-3+36.2\%+29.4\%}_{-24.7\%-29.4\%}$ | $1.056 \cdot 10^{-2+16.1\%+11.3\%}_{-15.8\%-11.3\%}$ |
| 2000                  | $4.217 \cdot 10^{-4+35.6\%+29.8\%}_{-24.5\%-29.8\%}$ | $6.327 \cdot 10^{-4+17.7\%+17.8\%}_{-16.6\%-17.8\%}$ |

- ❖ NNPDF3.0; scales set to the HT/2; uncertainties evaluated as for the stop case
- ❖ Validation with PROSPINO 2.1



◆ Differential distributions at NLO

- ❖ Test case: 1000/2000 GeV gluino; 13 TeV collisions
- ❖ Gluino decays: MadSpin
- ❖ Shower: PYTHIA 8.2 [Sjostrand, Mrenna & Skands]
- ❖ Jet reconstruction: anti- $k_T$  & FASTJET [Cacciari, Salam & Soyez (JHEP'08, EPJC'12)]
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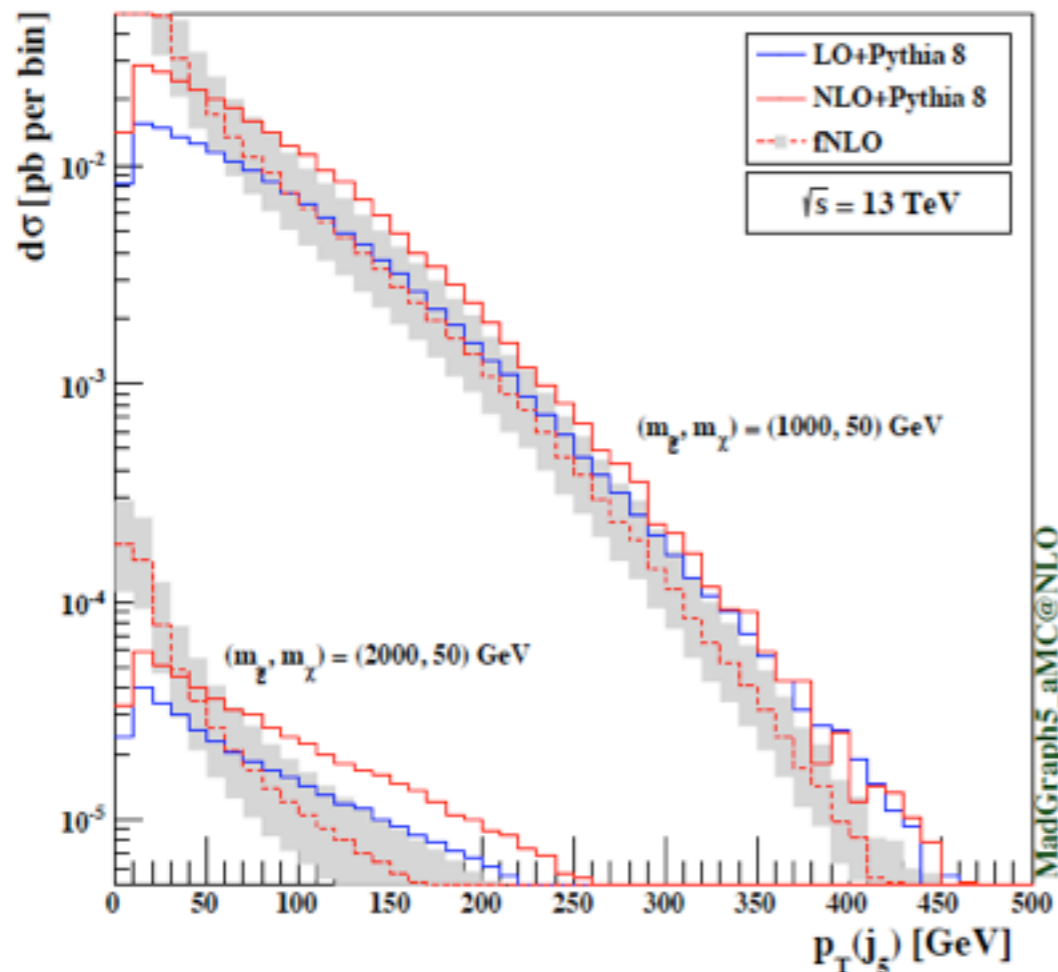
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Degrande, Fuks, Hirschi, Proudom, HSS (arXiv:1510.00391)

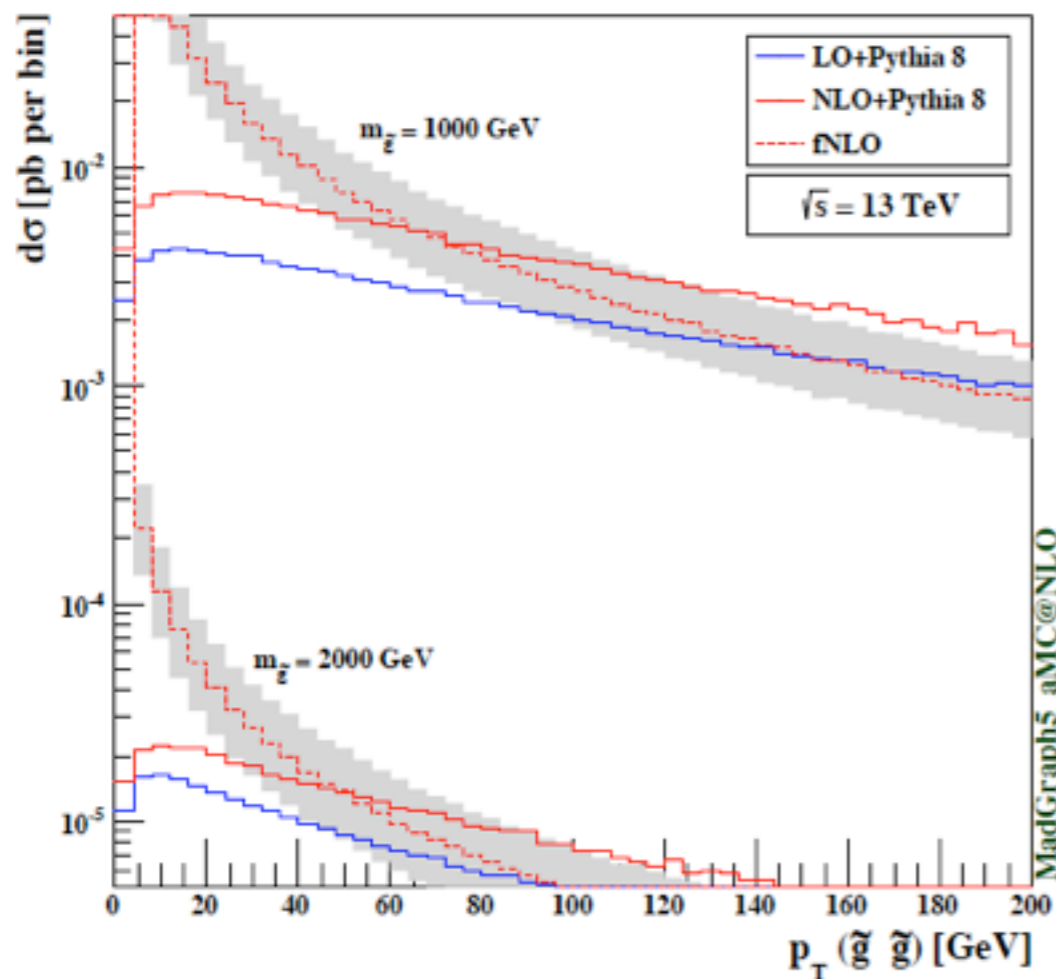
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# APPLICATION 3: GLUINO-PAIR IN SUSY QCD



Degrande, Fuks, Goncalves-Netto, Hirschi, Lopez-Val, Mawatari, Pagani, Proudome, HSS, Zaro (in preparation)

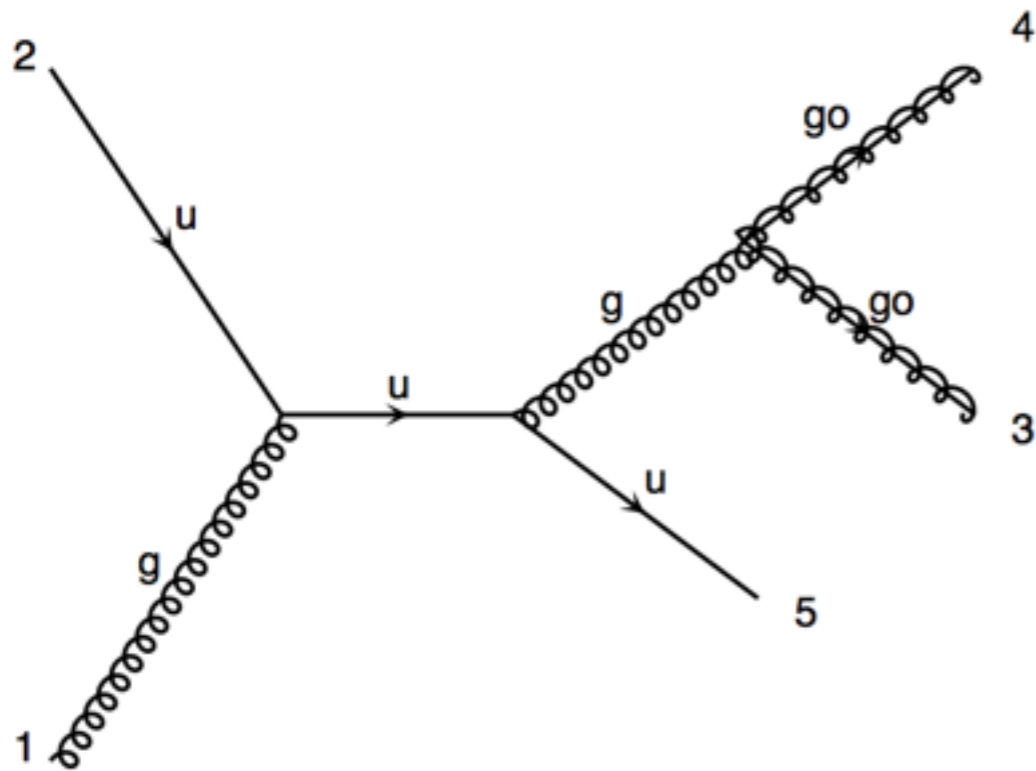
- Explore full spectrum (in the future):
  - New hadron states (R-hadron, gluinonium etc)
  - Separate resonance and non-resonance contributions

# APPLICATION 3: GLUINO-PAIR IN SUSY QCD



Degrande, Fuks, Goncalves-Netto, Hirschi, Lopez-Val, Mawatari, Pagani, Proudome, HSS, Zaro (in preparation)

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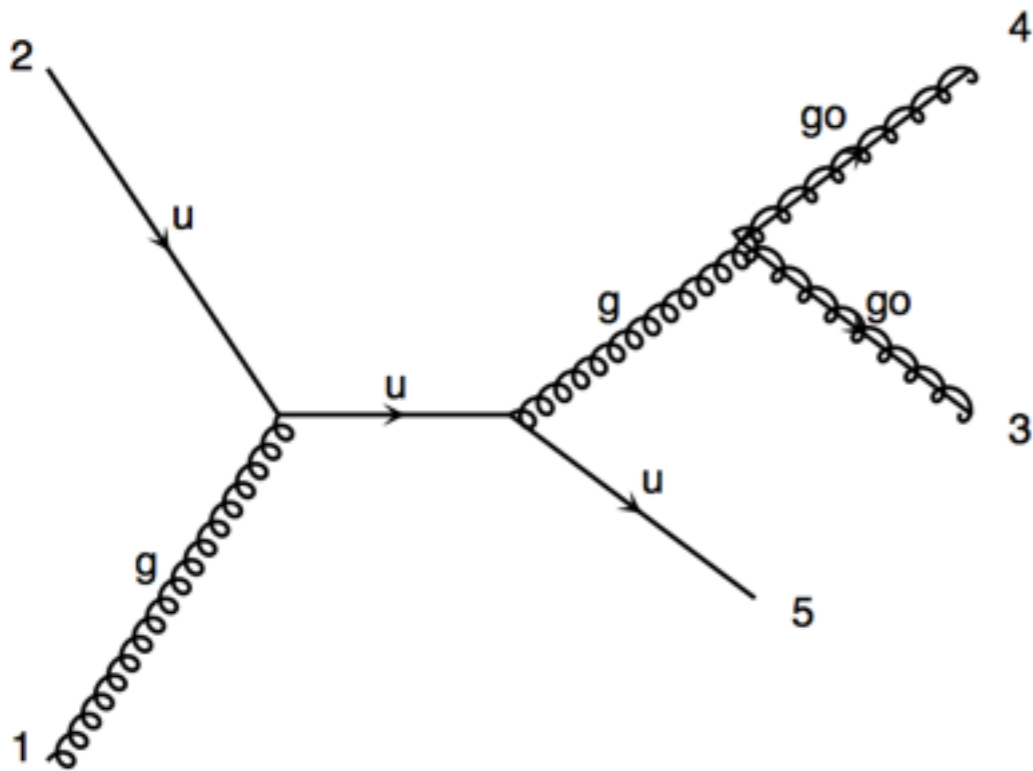
**NLO diagram for gluino-pair**

# APPLICATION 3: GLUINO-PAIR IN SUSY QCD

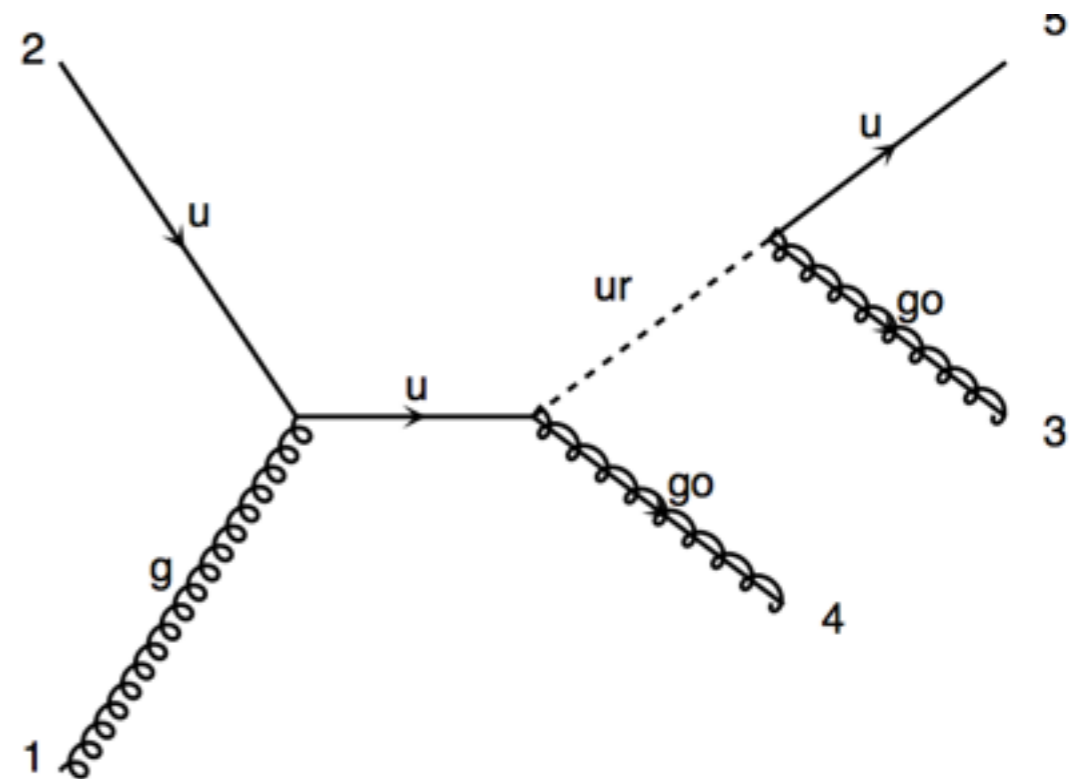


Degrande, Fuks, Goncalves-Netto, Hirschi, Lopez-Val, Mawatari, Pagani, Proudome, HSS, Zaro (in preparation)

- Explore full spectrum (in the future):
  - New hadron states (R-hadron, gluinoonium etc)
  - Separate resonance and non-resonance contributions



**NLO diagram for gluino-pair**



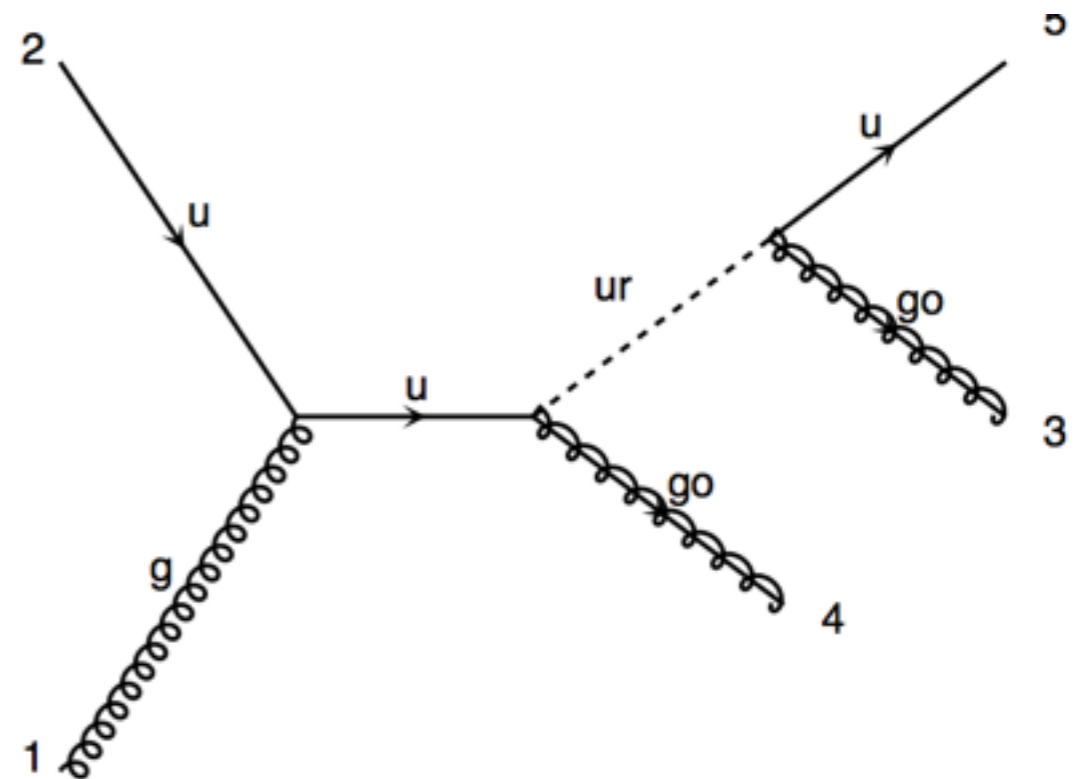
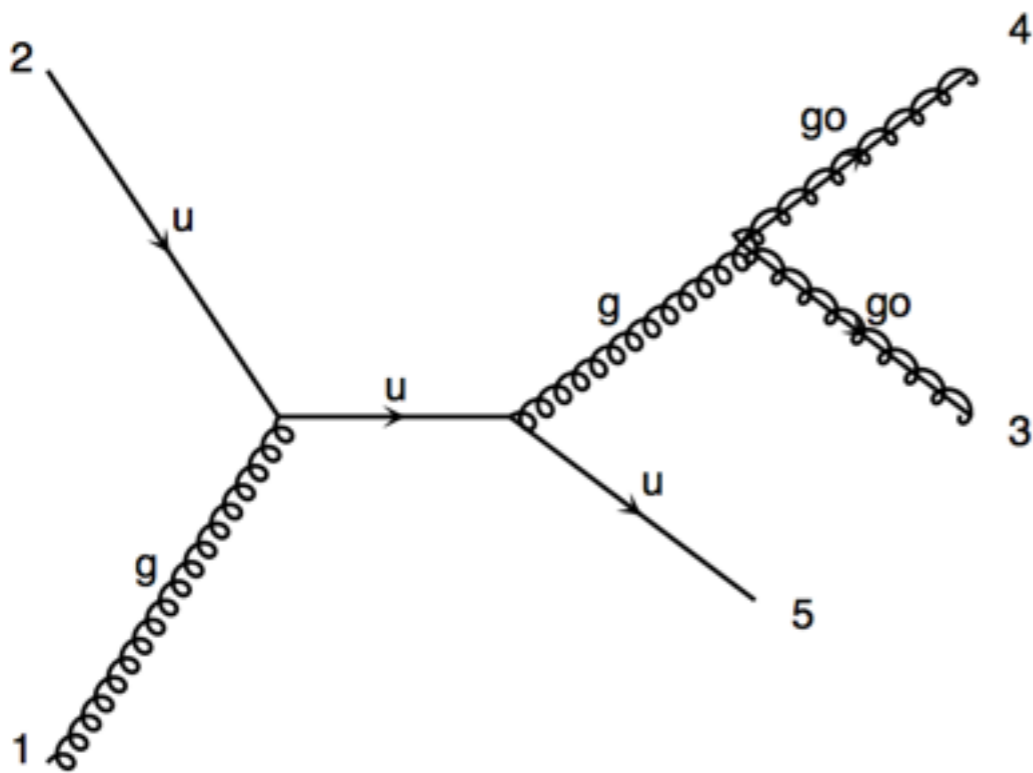
**LO diagram for gluino-squark with squark decay**

# APPLICATION 3: GLUINO-PAIR IN SUSY QCD



Degrande, Fuks, Goncalves-Netto, Hirschi, Lopez-Val, Mawatari, Pagani, Proudome, HSS, Zaro (in preparation)

- Explore full spectrum (in the future):
  - New hadron states (R-hadron, gluinoonium etc)
  - Separate resonance and non-resonance contributions



**NLO diagram for gluino-pair**

**LO diagram for gluino-squark  
with squark decay**

**On-Shell subtraction**

**MadOS**



# OTHER EFFORTS IN FR/MG5AMC @ NLO

- Top FCNC Degrande, Maltoni, Wang, Zhang (PRD'15)
- DM with spin-0/1 s-channel mediator Backovic, Kramer, Maltoni, Martini, Mawatari, Pellen (EPJC'15); Neubert, Wang, Zhang (arXiv:1509.05785)
- Other simple extension of SM: 2HDM etc Degrande (CPC'15)
- More efforts are ongoing
- We welcome the interested young students to join us.