

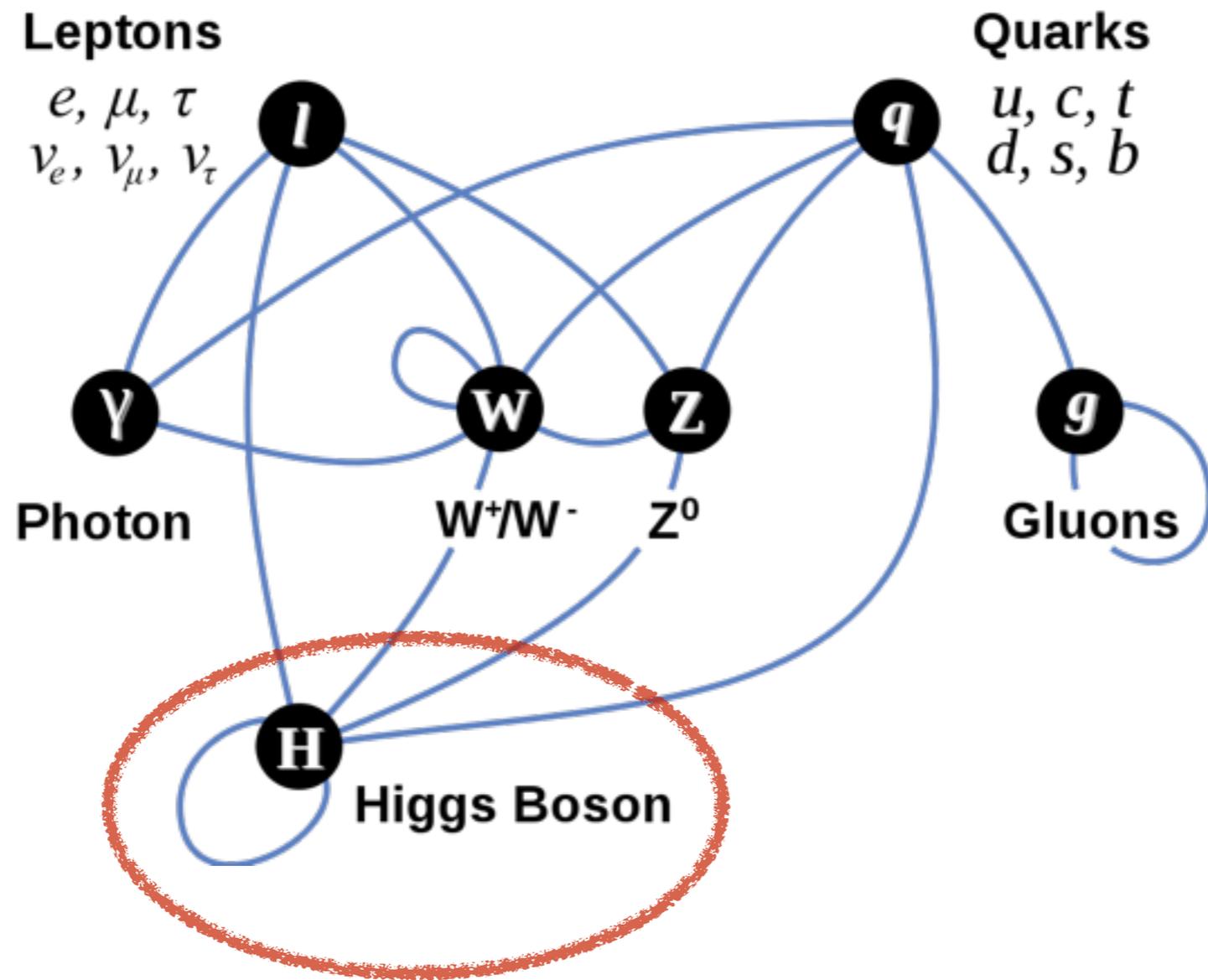
FeynRules

Neil Christensen

PITTSburgh Particle physics, Astrophysics and Cosmology Center (PITT PACC)

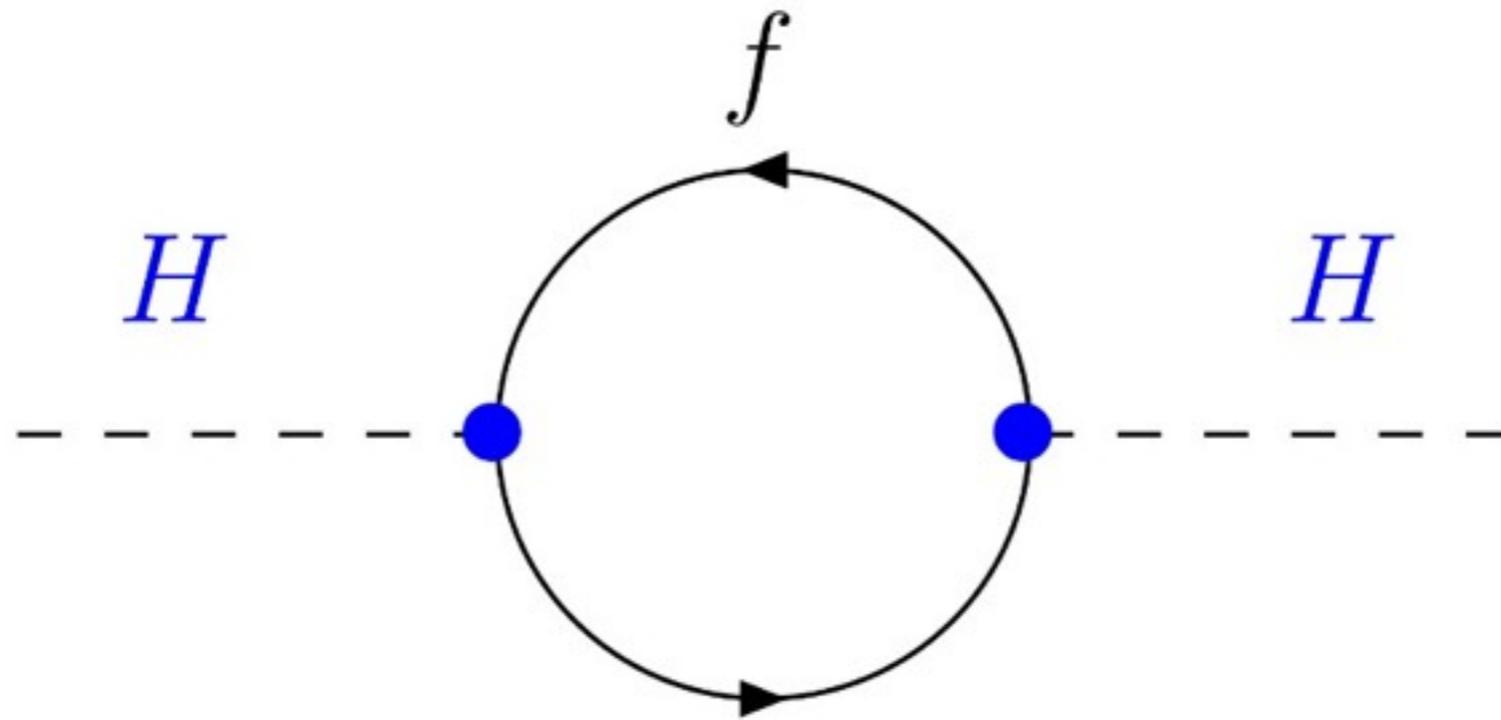
in collaboration with:

Adam Alloul, Celine DeGrande, Claude Duhr and Benjamin Fuks



The giant news of the last year is that we have discovered the Higgs boson!

Is it the SM Higgs?



$$\Delta M_H^2 = N_f \frac{\lambda_f^2}{8\pi^2} \left[-\Lambda^2 + 6m_f^2 \log \frac{\Lambda}{m_f} - 2m_f^2 \right]$$

Good reason to expect new physics beyond the Standard Model (SM).

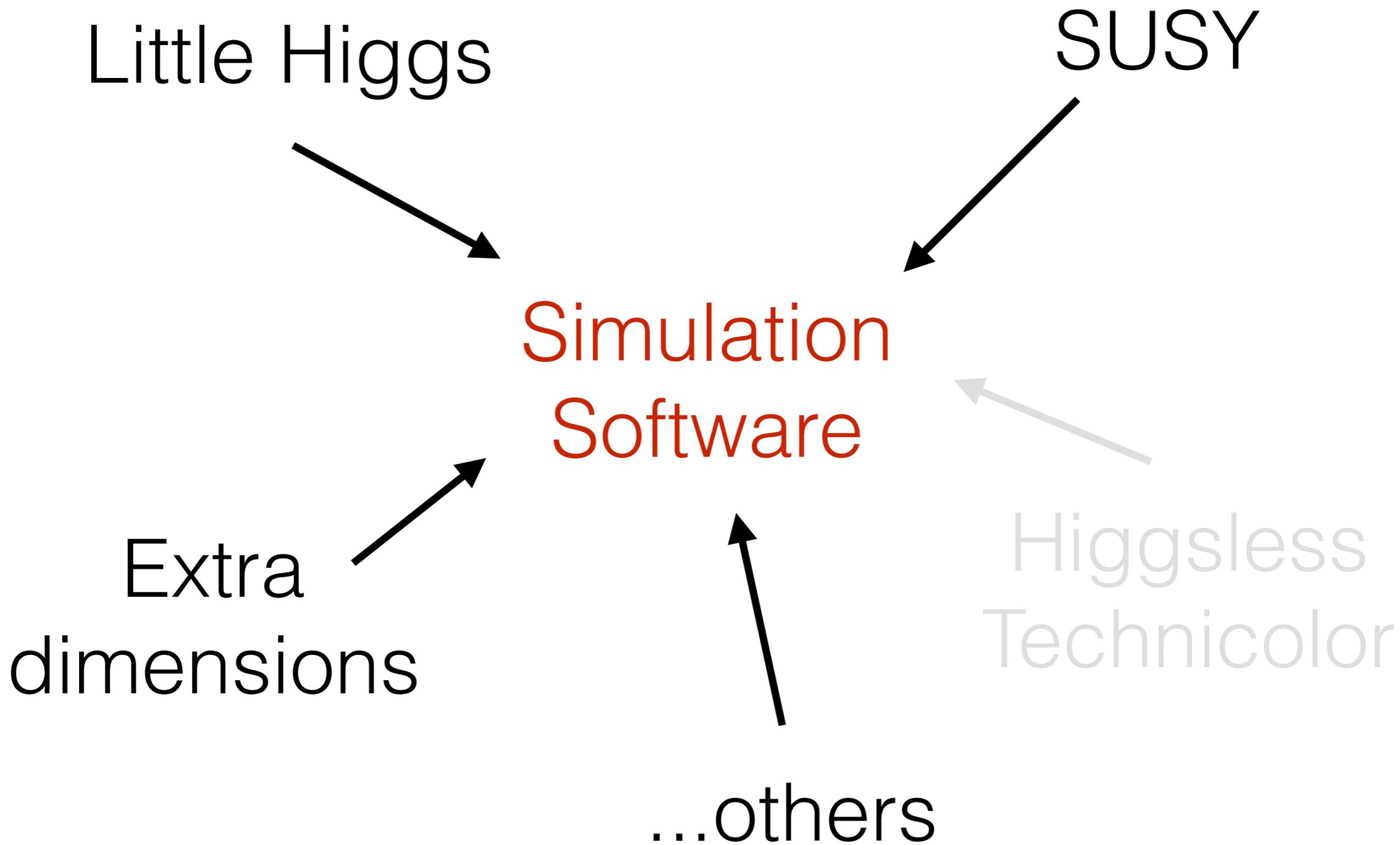
SUSY

Little Higgs

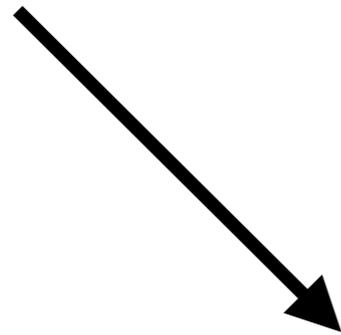
Higgsless
Technicolor

Extra
dimensions

...others

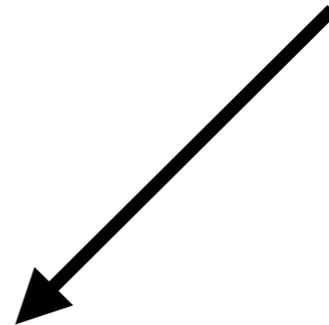


Little Higgs



SUSY

MSSM
pMSSM
NMSSM
RPVMSSM
...



Simulation
Software

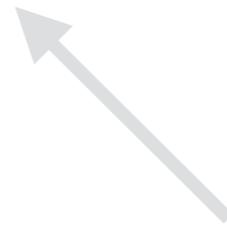
Extra
dimensions



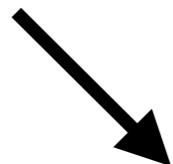
...others



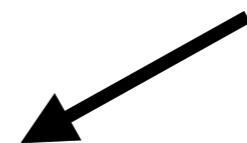
Higgsless
Technicolor



Little Higgs



CalcHEP



SUSY

- MSSM
- pMSSM
- NMSSM
- RPVMSSM
- ...

MadGraph

Sherpa

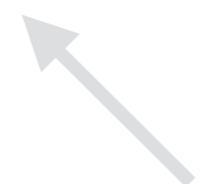
Whizard

Extra



dimensions

FeynArts



...others



Higgsless
Technicolor

What was the problem?

Problem 1:

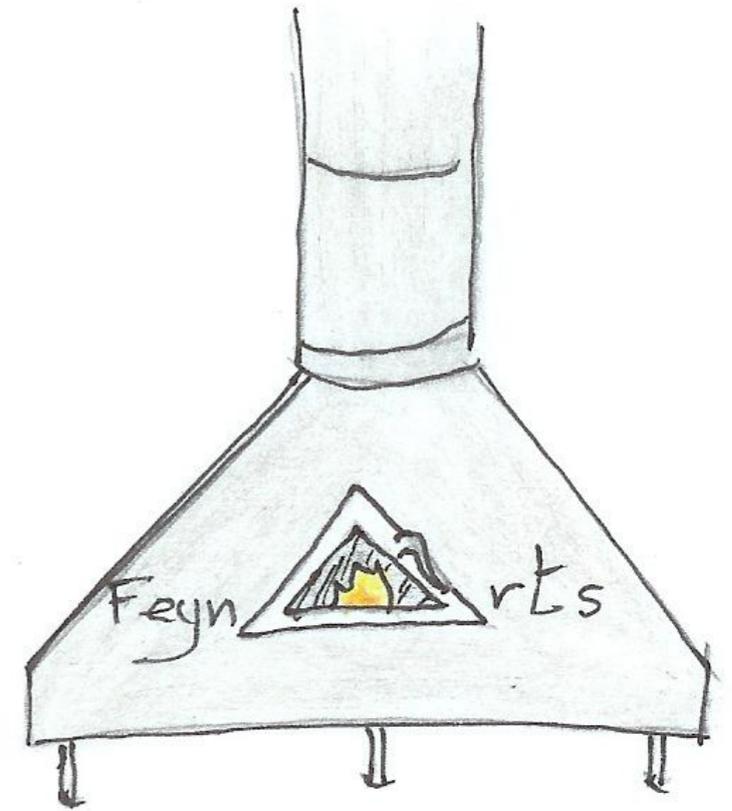
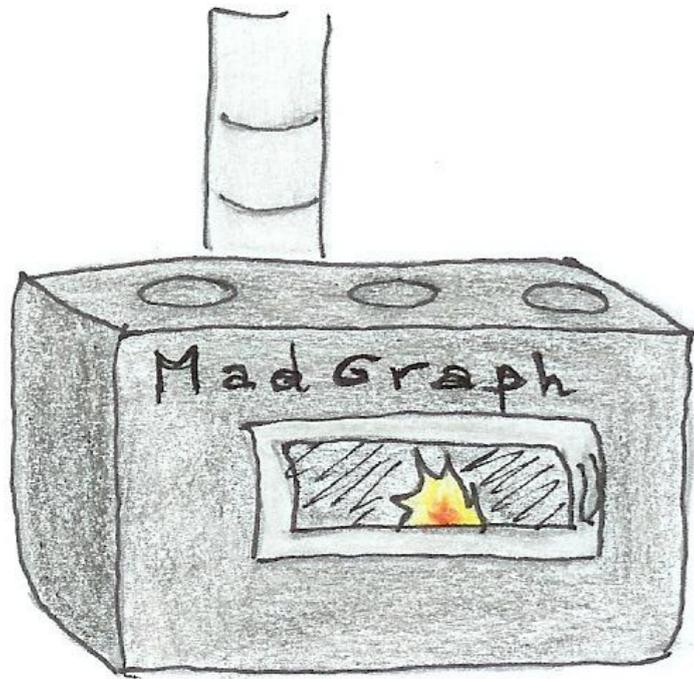
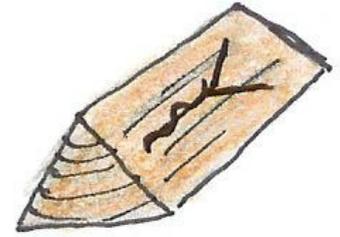
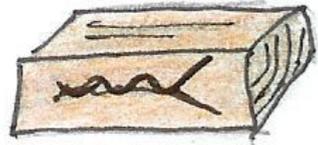
Implementing a model was often tedious and error prone.

```
#####  
# QFD Interactions  
# 2 heavy fermions - 1 light weak gauge boson  
#####  
  
# FFV (qqZ)  
dp dp z GZDp QED-HF  
up up z GZUp QED-HF  
sp sp z GZDp QED-HF  
cp cp z GZUp QED-HF  
bp bp z GZDp QED-HF  
tp tp z GZTp QED-HF  
  
# FFV (llZ)  
ep- ep- z GZLp QED-HF  
mup- mup- z GZLp QED-HF  
tap- tap- z GZLp QED-HF  
vep vep z GZNp QED-HF  
vmp vmp z GZNp QED-HF  
vtp vtp z GZNp QED-HF  
  
# FFV (qq'W) - diagonal CKM  
dp up w- GWFp QED-HF  
sp cp w- GWFp QED-HF  
bp tp w- GWTp QED-HF  
up dp w+ GWFp QED-HF  
cp sp w+ GWFp QED-HF  
tp bp w+ GWTp QED-HF  
  
# FFV (ll'W)  
vep ep- w+ GWFp QED-HF  
vmp mup- w+ GWFp QED-HF  
vtp tap- w+ GWFp QED-HF  
ep- vep w- GWFp QED-HF  
mup- vmp w- GWFp QED-HF  
tap- vtp w- GWFp QED-HF  
:  
█
```

```
c-----  
c   V-light   F-heavy   F-heavy  
c-----  
      GZDpL =  
- -1d0/2d0*gf(-ee,WMASS,ZMASS,MWP)  
- *vZ0f(WMASS,ZMASS,MWP)*vLP0f(WMASS,MWP)**2  
- -1d0/2d0*gtf(-ee,WMASS,ZMASS,MWP)  
- *VZ1f(WMASS,ZMASS,MWP)*vLP1f(WMASS,MWP)**2  
- +1d0/6d0*gpf(-ee,WMASS,ZMASS,MWP)  
- *vZ2f(WMASS,ZMASS,MWP)  
      GZDpR =  
- -1d0/2d0*gtf(-ee,WMASS,ZMASS,MWP)  
- *VZ1f(WMASS,ZMASS,MWP)  
- +1d0/6d0*gpf(-ee,WMASS,ZMASS,MWP)  
- *vZ2f(WMASS,ZMASS,MWP)  
      GZDp(1)=dcplx(GZDpL,Zero)  
      GZDp(2)=dcplx(GZDpR,Zero)  
      write(*,10) 'GZDpL = ',GZDpL  
      write(*,10) 'GZDpR = ',GZDpR  
  
      GZUpL =  
- 1d0/2d0*gf(-ee,WMASS,ZMASS,MWP)  
- *vZ0f(WMASS,ZMASS,MWP)*vLP0f(WMASS,MWP)**2  
- +1d0/2d0*gtf(-ee,WMASS,ZMASS,MWP)  
- *VZ1f(WMASS,ZMASS,MWP)*vLP1f(WMASS,MWP)**2  
- +1d0/6d0*gpf(-ee,WMASS,ZMASS,MWP)  
- *vZ2f(WMASS,ZMASS,MWP)  
      GZUpR =  
- 1d0/2d0*gtf(-ee,WMASS,ZMASS,MWP)  
- *VZ1f(WMASS,ZMASS,MWP)  
- +1d0/6d0*gpf(-ee,WMASS,ZMASS,MWP)  
- *vZ2f(WMASS,ZMASS,MWP)  
      GZUp(1)=dcplx(GZUpL,Zero)  
      GZUp(2)=dcplx(GZUpR,Zero)  
      write(*,10) 'GZUpL = ',GZUpL  
      write(*,10) 'GZUpR = ',GZUpR
```

Problem 2:

Each matrix element generator has its strengths. What if you need more than one? In the past you had to start over.



Problem 3:

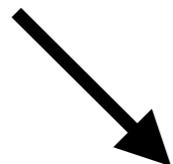
Implementations often did not transfer well to experimentalists.

Problem 3:

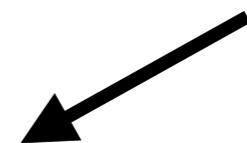
Implementations often did not transfer well to experimentalists.

It often required modifying the code of the matrix element generator.

Little Higgs



CalcHEP



SUSY

- MSSM
- pMSSM
- NMSSM
- RPVMSSM
- ...

MadGraph

Sherpa

Whizard

Extra



dimensions

FeynArts



...others



Higgsless
Technicolor

SUSY

MSSM

pMSSM

NMSSM

RPVMSSM

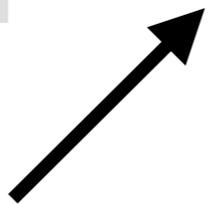
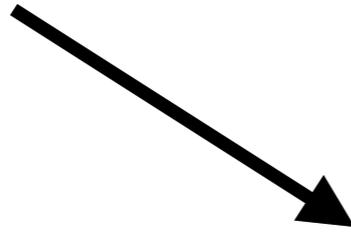
Little Higgs →

Extra dimensions →

Higgsless →

Technicolor

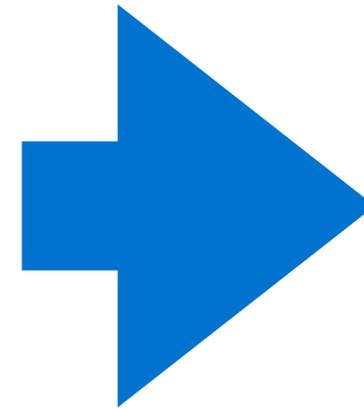
...others →



FeynRules

LanHEP

SARAH



CalcHEP

MadGraph

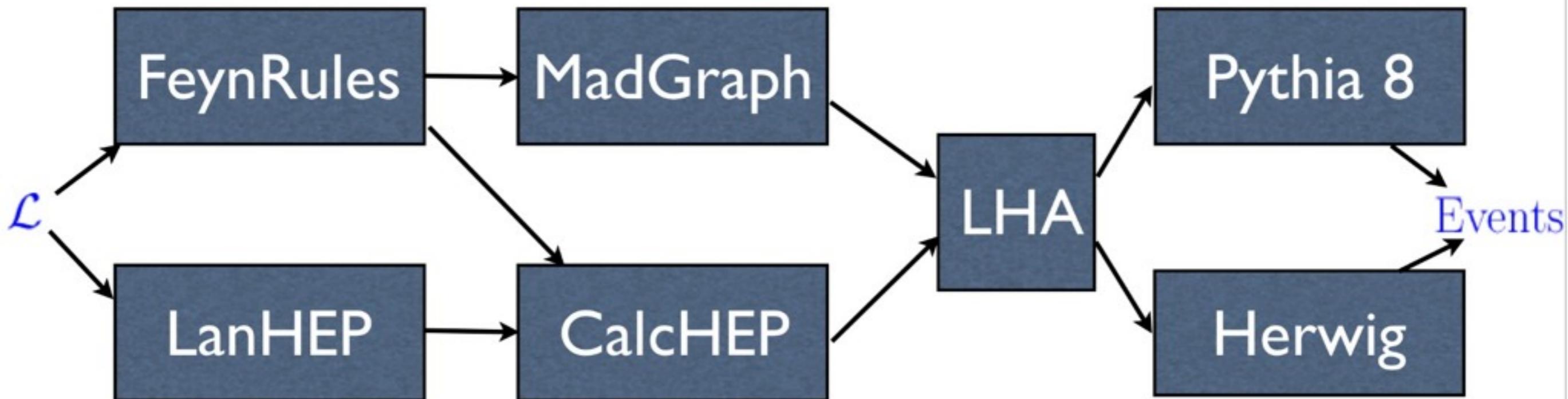
Sherpa

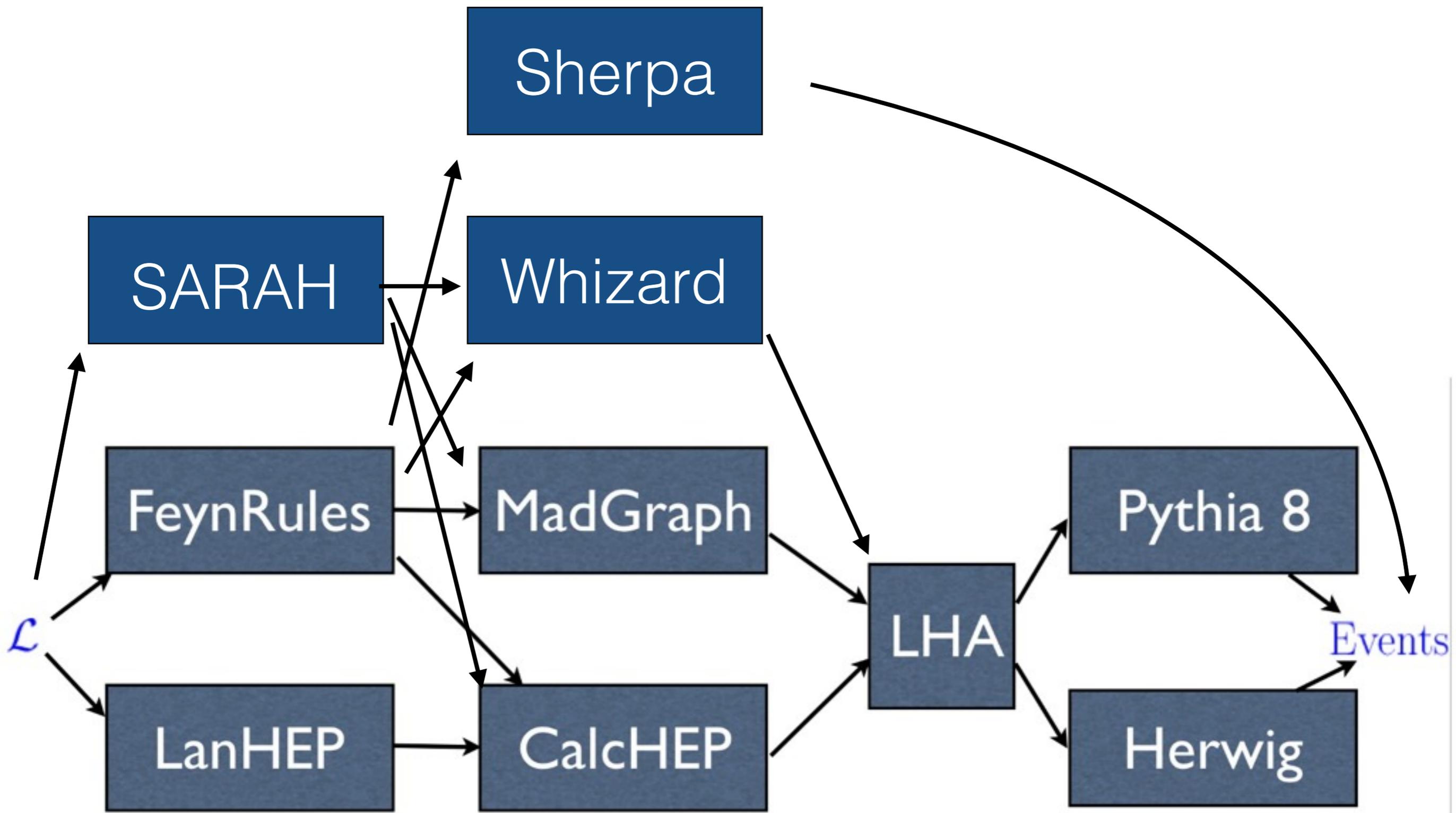
Whizard

FeynArts

MC4BSM 2012 Tutorial

[arXiv:1209.0297](https://arxiv.org/abs/1209.0297)





	LanHEP	FeynRules	SARAH
First Released	1996	2008	2008
Programming Language	C	Mathematica	Mathematica
General Lagrangian	Yes	Yes	SUSY Only
Superfields	No	Yes	Yes
Parameter Running	No	In Progress	Yes
Aut. Mass Diagonalization	Yes	Yes	Yes
Spin	0, 1/2, 1, 3/2, 2	0, 1/2, 1, 3/2, 2	-
Superfields	-	Chiral, Vector	Chiral, Vector

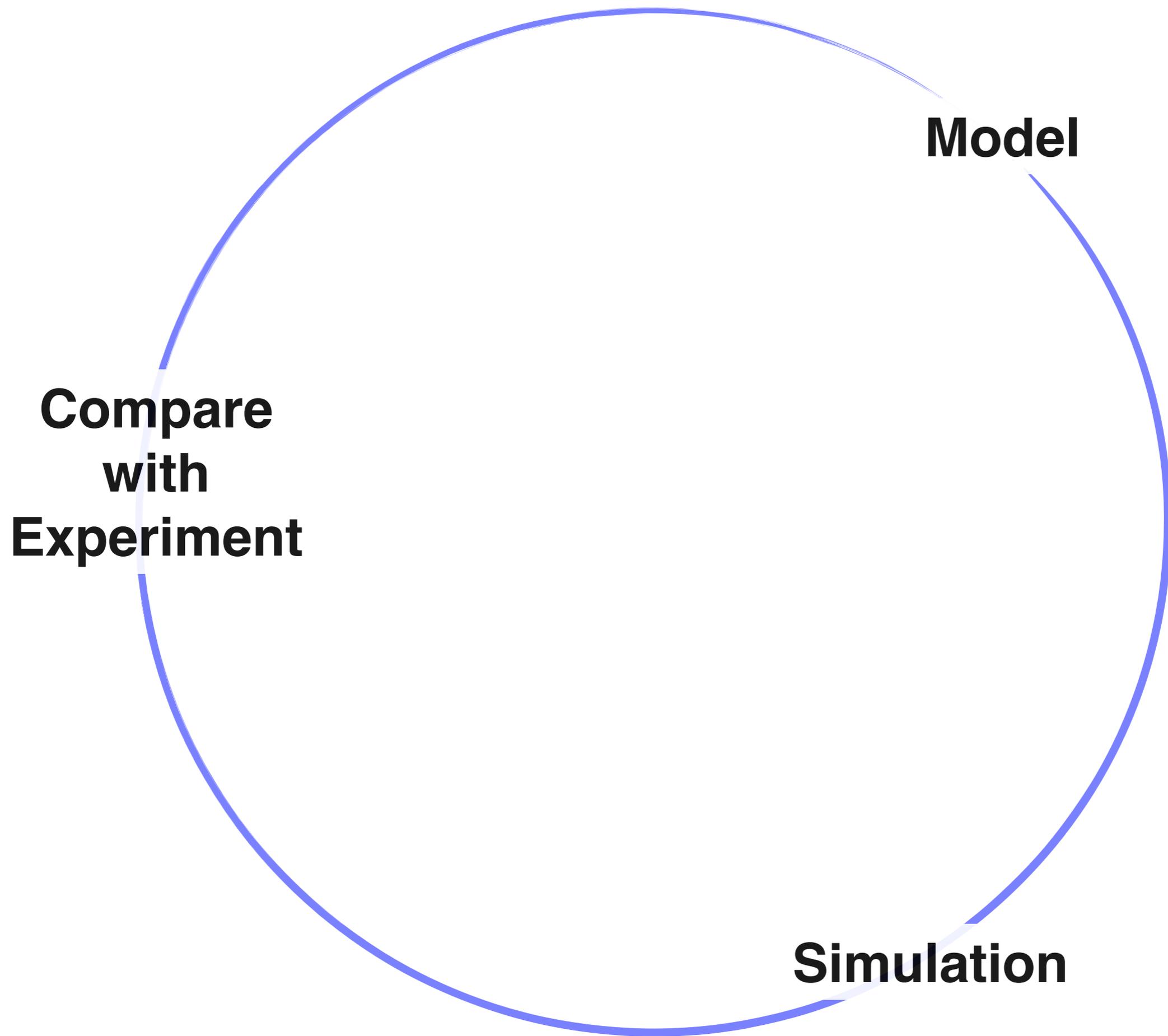
	LanHEP	FeynRules	SARAH
CalcHEP	Yes	Yes	Yes
FeynArts	Yes	Yes	Yes
MadGraph	In Progress	Yes	Yes
Sherpa	No	Yes	No
Whizard	No	Yes	Yes

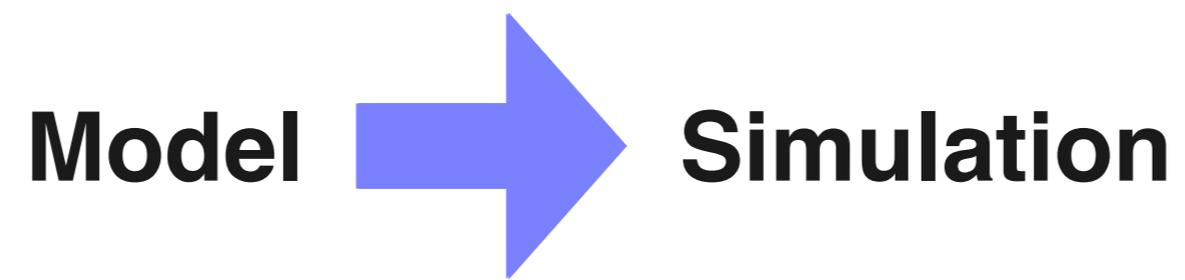
FeynRules 2.0

Coming soon!

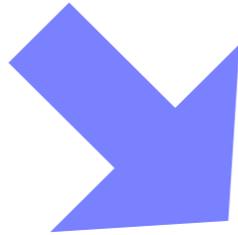
Beyond 1.0 (CPC 180, 1614):

- 2-Component Weyl Notation (CPC 182, 2404)
- Spin-3/2 (arXiv:1308.1668)
- Superspace Notation (CPC 182, 2404)
- Automatic Mass Diagonalization (EPJC 73, 2325)
- “.gen” files in FA interface
- Universal FeynRules Output (UFO) (CPC 183, 1201)
- Whizard Interface (EPJC 72, 1990)
- Automatic $1 \rightarrow 2$ widths (in preparation)
- Speed & Efficiency Improvements
- Web Validation (arXiv:1003.1643)

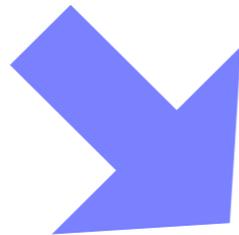




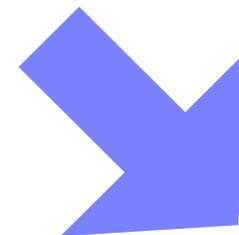
Model



FeynRules



MadGraph



Simulation

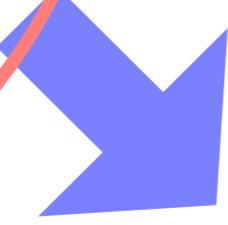
Model



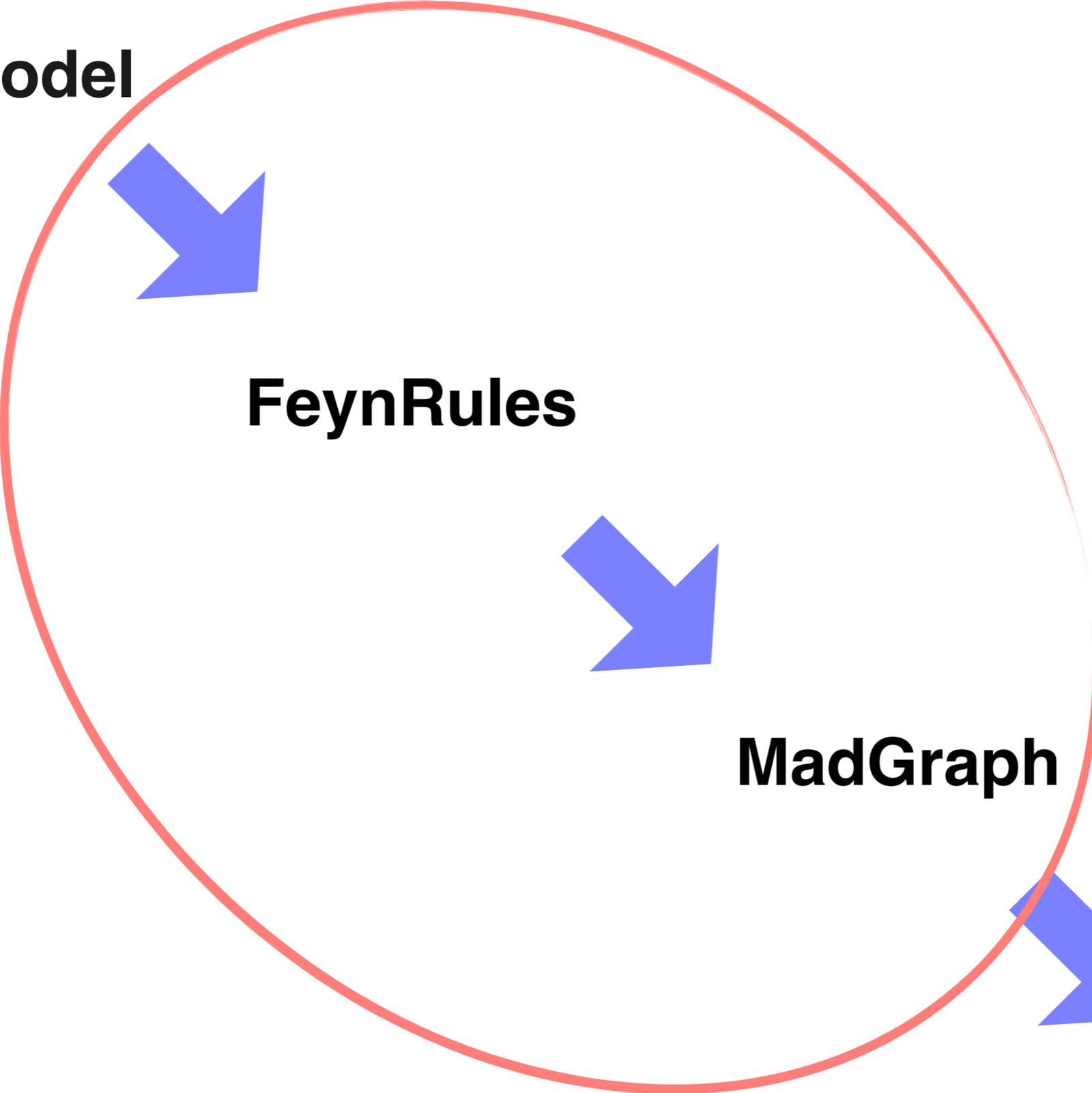
FeynRules



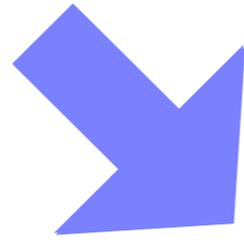
MadGraph



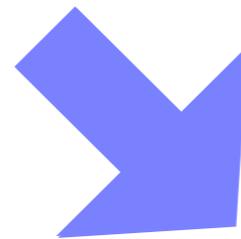
Simulation



Model



FeynRules

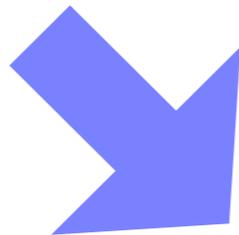


MadGraph

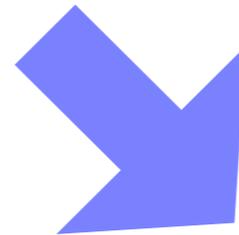
Model



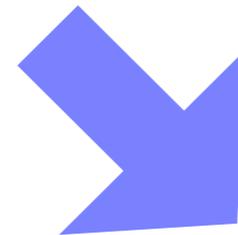
FR Model File



FeynRules

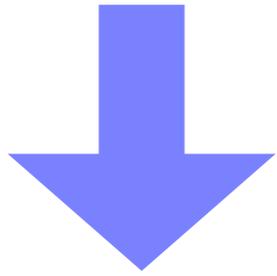


Validation

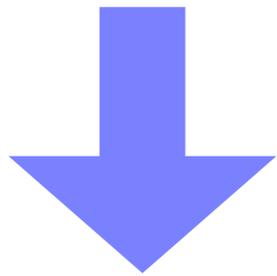


MadGraph

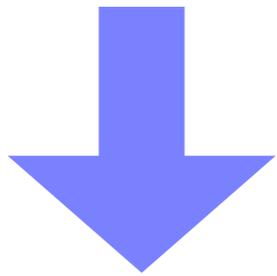
Model



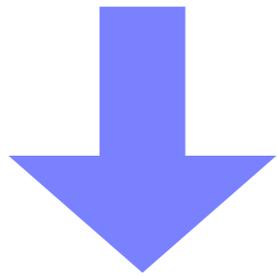
FR Model File



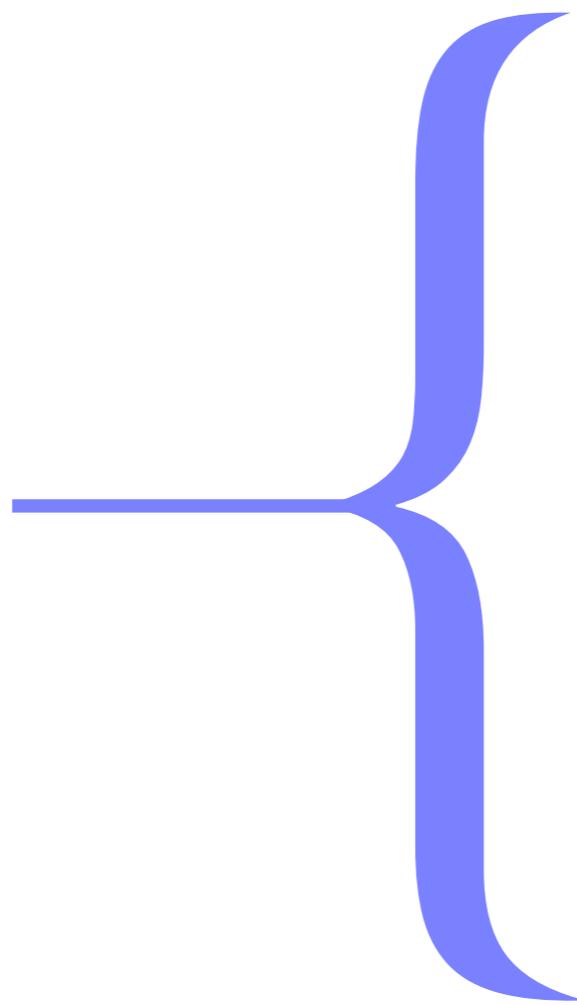
FeynRules



Validation

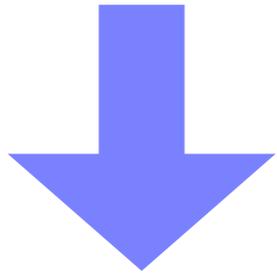


MadGraph

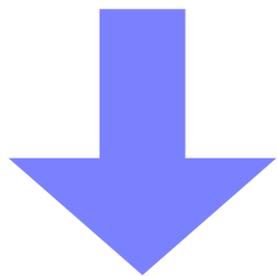


- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

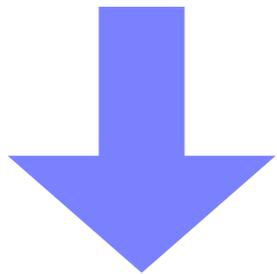
Model



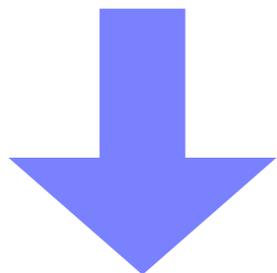
FR Model File



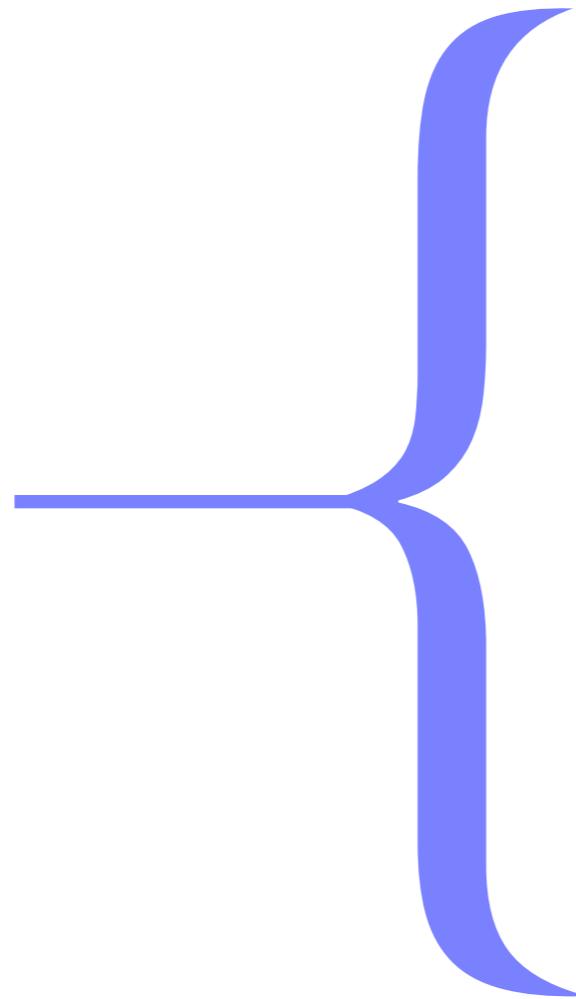
FeynRules



Validation

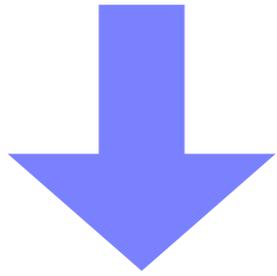


MadGraph

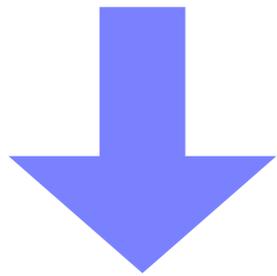


- Load FeynRules
- Load Model
- Update Parameters
- Check Hermiticity, Mass Diagonalization, etc.
- Check Feynman Rules
- Update Widths
- Export to Simulation Tool (UFO)

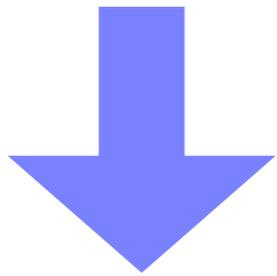
Model



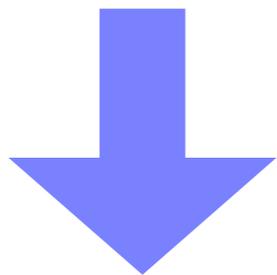
FR Model File



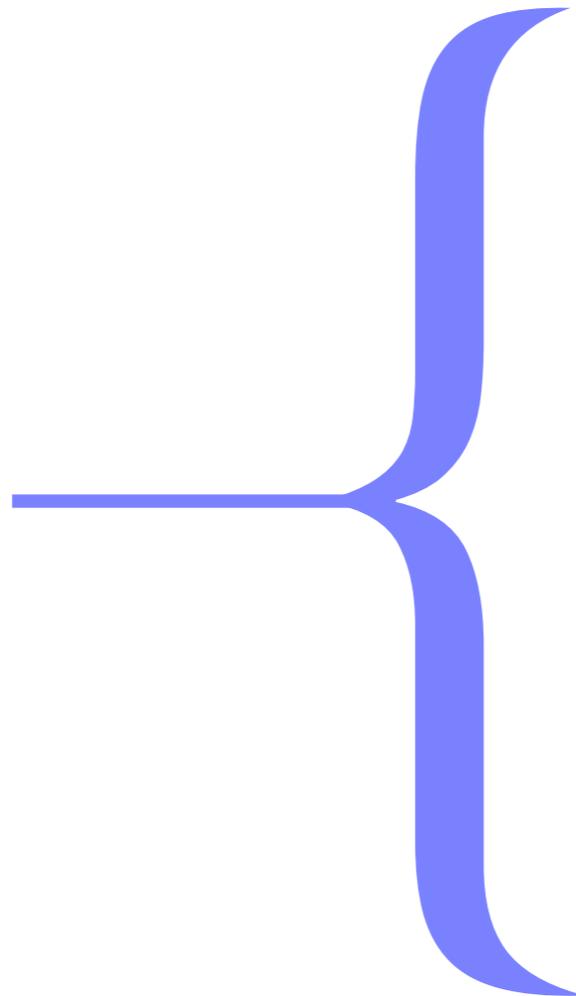
FeynRules



Validation

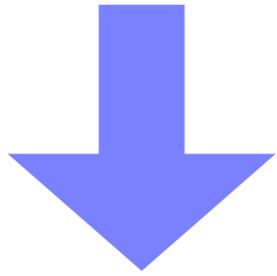


MadGraph

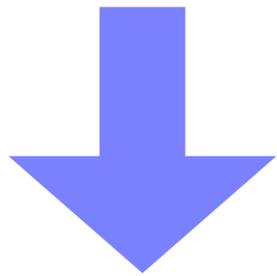


- Documentation
- Sanity Checks
- Test 1 Generator
- Test Several Generators
- Web Validation
- Debugging

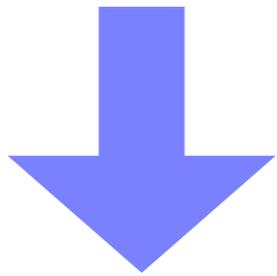
Model



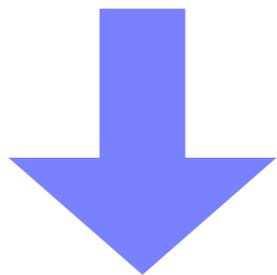
FR Model File



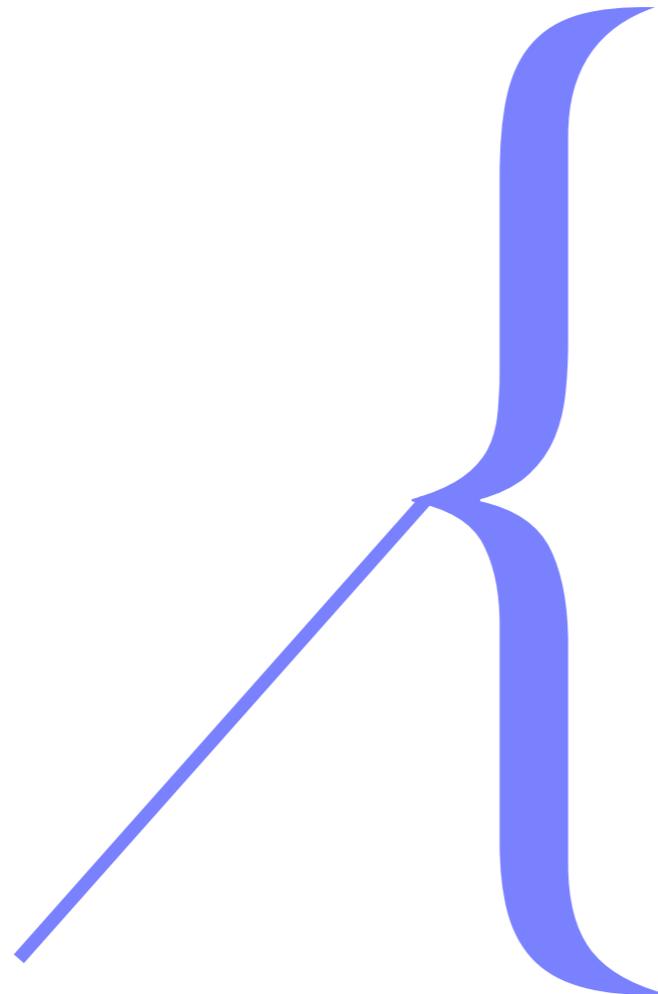
FeynRules



Validation

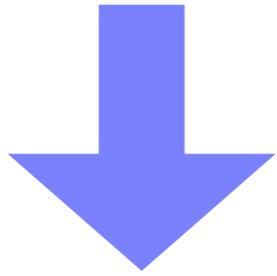


MadGraph

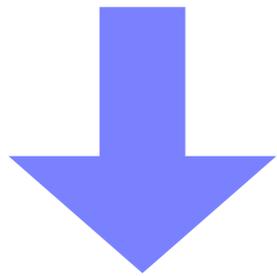


- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

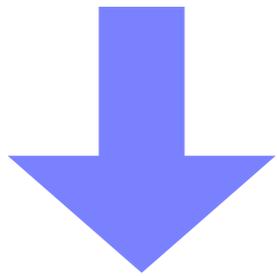
Model



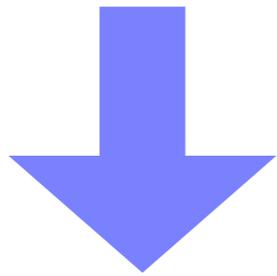
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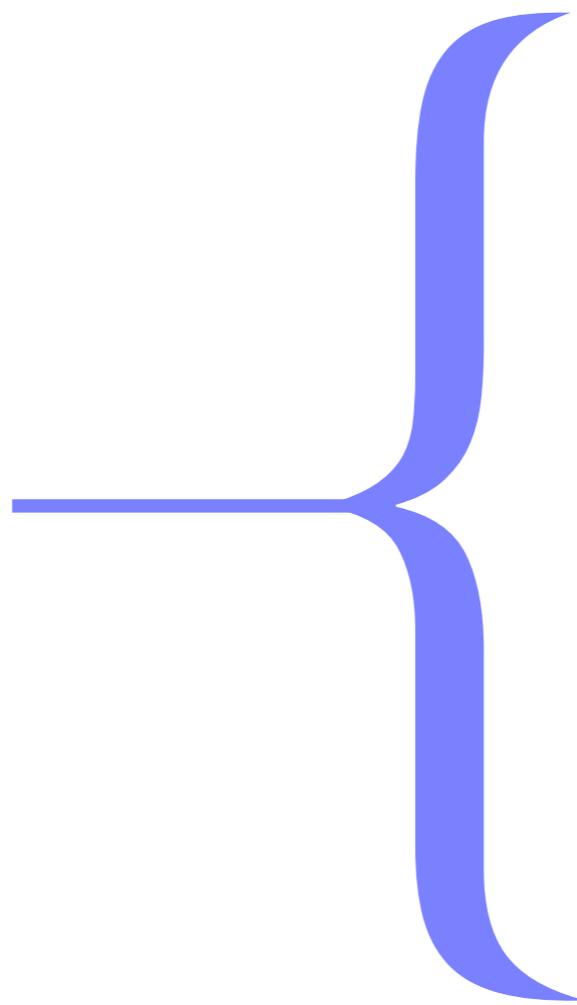
FeynRules



Validation

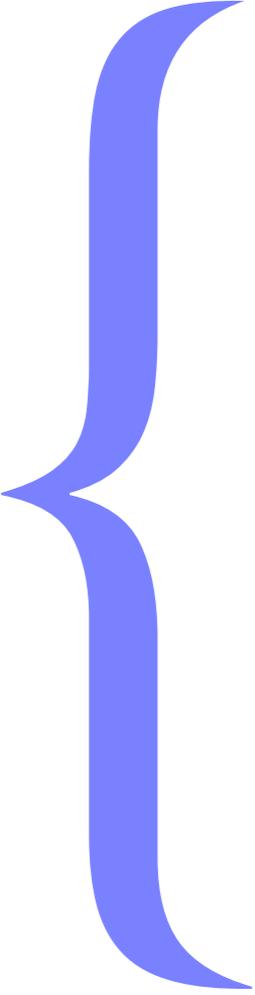


MadGraph



- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

FR Model File

- 
- Model Info
 - Indices
 - Parameters
 - Fields
 - Superfields
 - Gauge Groups
 - Restrictions
 - Mixings
 - Lagrangian

- Pure Text Files
 - Ending in “.fr”
- Mathematica Syntax

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Model Name
- Authors
- Institutions
- Emails
- Date
- References
- URLs
- Version

Model Info

```
M$ModelName = "my_new_model";
```

```
M$Information = {  
  Authors      -> {"Mr. X", "Ms. Y"},  
  Institutions -> {"UC Louvain"},  
  Emails       -> {"X@uclouvain.be", "Y@uclouvain.be"},  
  Date         -> "01.03.2013",  
  References   -> {"reference 1", "reference 2"},  
  URLs        -> {"http://feynrules.irmp.ucl.ac.be"},  
  Version      -> "1.0"  
};
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Lorentz/Spin Indices Automatic
- Symmetry and Flavor Indices
- Index Range
- Index Style
- Unfold/NoUnfold
 - Unfold must be used for any index that expands the field into non-mass eigenstates.

Indices

```
IndexRange[ Index[Colour] ] = Range[3];  
IndexRange[ Index[SU2W] ]   = Unfold[ Range[3] ];  
IndexRange[ Index[Gluon] ]  = NoUnfold[ Range[8] ];
```

```
IndexStyle[ Colour, i ];  
IndexStyle[ Gluon, a ];
```

$$G[\mu, a] \longrightarrow G[\text{Index}[\text{Lorentz}, \mu], \text{Index}[\text{Gluon}, a]]$$

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- External Parameters:
 - Independent
- Internal Parameters:
 - Dependent
 - Must only depend on parameters above it.

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- External Parameters:
 - Independent
- Internal Parameters:
 - Dependent
 - Must only depend on parameters above it.

ParameterType -> External

or

ParameterType -> Internal

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Value
 - Numerical (External)
 - Analytic (Internal)

Value

-> 0.1184

or

Value

-> Sqrt[4 Pi aS]

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Definitions
 - Numerical (External)
 - Analytic (Internal)
 - Replacement during Feynman rule calculation

Definitions -> { gs -> Sqrt[4 Pi aS] }

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Indices
 - Tensorial parameters

Indices

-> {Index[Generation], Index[Generation]}

Parameters

```
M$Parameters = {  
  param1 == { options1 },  
  param2 == { options2 },  
  ...  
};
```

Parameters

```
aS == {  
  TeX          -> Subscript[\[Alpha],s],  
  ParameterType -> External,  
  InteractionOrder -> {QCD, 2},  
  Value        -> 0.1184,  
  BlockName    -> SMINPUTS,  
  OrderBlock   -> 3,  
  Description  -> "Strong coupling constant at the Z pole"  
}
```

```
gs == {  
  TeX          -> Subscript[g,s],  
  ParameterType -> Internal,  
  ComplexParameter -> False,  
  InteractionOrder -> {QCD, 1},  
  Value        -> Sqrt[4 Pi aS],  
  ParameterName -> G,  
  Description  -> "Strong coupling constant at the Z pole"  
}
```

Parameters

```
CKM == {  
  ParameterType      -> Internal,  
  Indices            -> {Index[Generation], Index[Generation]},  
  Unitary            -> True,  
  ComplexParameter  -> True,  
  Definitions        -> {  
    CKM[i_,3]  :> 0 /; i!=3,  
    CKM[3,i_]  :> 0 /; i!=3,  
    CKM[3,3]   -> 1 },  
  Value              -> {  
    CKM[1,1] -> Cos[cabi],  
    CKM[1,2] -> Sin[cabi],  
    CKM[2,1] -> -Sin[cabi],  
    CKM[2,2] -> Cos[cabi] },  
  Description        -> "CKM-Matrix"  
}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- S[...] : Spin-0 Scalar
- F[...] : Spin-1/2 Fermion
 - 4-component
 - Dirac & Majorana
- W[...] : Spin-1/2 Fermions
 - 2-component
 - Left & Right Chiral
- V[...] : Spin-1 Vectors
- R[...] : Spin-3/2 Fermion
 - 4-component
 - Dirac & Majorana
- RW[...] : Spin-3/2 Fermion
 - 2-component
 - Left & Right Chiral
- T[...] : Spin-2 Tensor
- U[...] : Spin-0 Ghost

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- SelfConjugate
 - Whether the particle has an antiparticle

SelfConjugate -> False

or

SelfConjugate -> True

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

● ClassName

- Name of Particle Class
- Each class can have multiple members

ClassName -> uq,

ClassMembers -> {u, c, t}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- ClassName
 - Name of Particle Class
 - Each class can have multiple members
 - If not self-conjugate, FeynRules automatically generates antiparticles:
uqbar
{ubar, cbar, tbar}

ClassName -> uq,

ClassMembers -> {u, c, t}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Indices
 - Symmetry & Flavor Indices
 - Spin & Lorentz Indices automatic: Do Not Add Them!
- FlavorIndex
 - Index for Class Members

```
Indices -> {Index[ Colour ]}
```

```
Indices -> {Index[ Colour ], Index[ SU2D ]}
```

```
Indices -> { Index[ Colour ], Index[ Flavour ] },
```

```
FlavorIndex -> Flavour
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Quantum Numbers
 - Discrete Charges
 - Abelian Charges
 - Conservation checked during Feynman rule calculation

```
QuantumNumbers -> {Q -> -1, LeptonNumber -> 1}  
QuantumNumbers -> {Q -> 2/3}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

● Mass

- Class
- Class Members
- Numerical Value or Internal

Mass -> {MW, Internal}

Mass -> {MZ, 91.188}

Mass -> {{MU,0}, {MC,0}, {MT, 174.3}}

Mass -> {Mu, {MU, 0}, {MC, 0}, {MT, 174.3}}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Mass
 - Class
 - Class Members
 - Numerical Value or Internal
- Width is analogous

Mass -> {MW, Internal}

Mass -> {MZ, 91.188}

Mass -> {{MU,0}, {MC,0}, {MT, 174.3}}

Mass -> {Mu, {MU, 0}, {MC, 0}, {MT, 174.3}}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Unphysical
 - Not Mass Eigenstates

Unphysical -> True

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Unphysical
 - Not Mass Eigenstates
- Definitions
 - Replacements before calculation of Feynman rules

Unphysical -> True

Definitions -> {B[mu_] -> -sw Z[mu] + cw A[mu]}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Majorana Fermions
 - Charge Conjugation Phase
 - Chirality

MajoranaPhase -> Phi

Chirality -> Left

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Majorana Fermions
 - Charge Conjugation Phase
 - Chirality
 - WeylComponents (inside 4-component fermion)

MajoranaPhase -> Phi

Chirality -> Left

WeylComponents -> {chi, xibar}

Fields

```
M$ClassesDescription = {  
  spin1[1] == { options1 },  
  spin1[2] == { options2 },  
  spin2[1] == { options3 },  
  ... }
```

Fields

```
F[3] == {
  ClassName      -> uq,
  ClassMembers  -> {u, c, t},
  Indices        -> {Index[Generation], Index[Colour]},
  FlavorIndex    -> Generation,
  SelfConjugate  -> False,
  Mass           -> {Mu, {MU, 2.55*^-3}, {MC,1.27}, {MT,172}},
  Width         -> {0, 0, {WT,1.50833649}},
  QuantumNumbers -> {Q -> 2/3},
  PropagatorLabel -> {"uq", "u", "c", "t"},
  PropagatorType -> Straight,
  PropagatorArrow -> Forward,
  PDG           -> {2, 4, 6},
  ParticleName  -> {"u", "c", "t" },
  AntiParticleName -> {"u~", "c~", "t~"},
  FullName      -> {"u-quark", "c-quark", "t-quark"}
},
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- CSF[...] : Chiral Superfields
- VSF[...] : Vector Superfields
 - Wess-Zumino Gauge

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Shared Features
 - ClassName
 - Indices
 - QuantumNumbers

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Chiral Superfields
 - Chirality
 - Weyl
 - Scalar
 - Auxiliary field optional

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Vector Superfields
 - Gauge Boson
 - Gaugino
 - Auxiliary field optional

Superfields

```
M$Superfields = {  
  superfield1[1] == { options1 },  
  superfield2[2] == { options2 },  
  ...  
}
```

Superfields

```
CSF[1] == {  
  ClassName -> PHI,  
  Chirality -> Left,  
  Weyl      -> psi,  
  Scalar    -> z,  
  Auxiliary -> FF  
}  
CSF[2] == {  
  ClassName -> XI,  
  Chirality -> Right,  
  Weyl      -> psibar,  
  Scalar    -> zbar  
}
```

Superfields

```
VSF[1] == {  
  ClassName    -> VWZ,  
  GaugeBoson  -> V,  
  Gaugino     -> lambda,  
  Indices     -> {Index[SU2W]}  
}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Abelian
 - True or False
- CouplingConstant
 - Symbol
- GaugeBoson
 - ClassName
 - (Superfield can also be consistently specified)
- StructureConstant
 - Symbol

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Representation
 - {{Symbol,Index},
{Symbol,Index},...}

Representations → {{T,Colour}}

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Definitions
 - Applied before Feynman rule calculation

Representations

-> {{Ta, SU2D}},

Definitions

-> {Ta[a_] -> PauliSigma[a]/2, ep -> Eps}

Gauge Groups

```
M$GaugeGroups = {
  U1Y == {
    Abelian          -> True,
    CouplingConstant -> gp,
    GaugeBoson       -> B,
    Charge           -> Y
  },
  SU2L == {
    Abelian          -> False,
    CouplingConstant -> gw,
    GaugeBoson       -> Wi,
    StructureConstant -> ep,
    Representations   -> {{Ta,SU2D}},
    Definitions       -> {Ta[a_]->PauliSigma[a]/2, ep->Eps}
  },
  SU3C == {
    Abelian          -> False,
    CouplingConstant -> gs,
    GaugeBoson       -> G,
    StructureConstant -> f,
    Representations   -> {{T,Colour}},
    SymmetricTensor  -> dSUN
  }
}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Covariant Derivative
- Field Strength
Tensor
- Superfield Strength
Tensor

Gauge Groups

FS[A, mu, nu]

FS[A, mu, nu, a]

SuperfieldStrengthL[V, sp]

SuperfieldStrengthR[V, spdot]

SuperfieldStrengthL[V, sp , a]

SuperfieldStrengthR[V, spdot, a]

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^a_{bc} A_\mu^b A_\nu^c ,$$

$$W_\alpha = -\frac{1}{4} \bar{D} \cdot \bar{D} e^{2gV} D_\alpha e^{-2gV} ,$$

$$\bar{W}_{\dot{\alpha}} = -\frac{1}{4} D \cdot D e^{-2gV} \bar{D}_{\dot{\alpha}} e^{2gV} ,$$

Gauge Groups

`D_C [phi, mu]`

$$D_\mu \phi = \partial_\mu \phi - ig A_\mu^a T_a \phi$$

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Restrict models
 - Simpler form appropriate for a particular pheno study
 - E.G. CKM matrix can be replaced by a delta function
 - Applied before calculating Feynman rules

Restrictions

```
M$Restrictions = {  
    CKM[i_,i_] -> 1,  
    CKM[i_?NumericQ, j_?NumericQ] :> 0 /; (i != j)  
}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Mass Basis
 - Physical or Unphysical Basis
- Gauge Basis
 - Unphysical Basis

MassBasis \rightarrow {W, Wbar},

GaugeBasis \rightarrow {Wi[1], Wi[2]},

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Mass Basis
 - Physical or Unphysical Basis
- Gauge Basis
 - Unphysical Basis
- Value
 - Numerical Transformation Matrix

MassBasis $\rightarrow \{W, Wbar\},$

GaugeBasis $\rightarrow \{Wi[1], Wi[2]\},$

Value $\rightarrow \{\{1/Sqrt[2], -I/Sqrt[2]\}, \{1/Sqrt[2], I/Sqrt[2]\}\}$

Mixings

$$W_{\mu}^{+} = \frac{W_{\mu}^1 - iW_{\mu}^2}{\sqrt{2}} \quad \text{and} \quad W_{\mu}^{-} = \frac{W_{\mu}^1 + iW_{\mu}^2}{\sqrt{2}}$$

```
Mix["11"] == {  
  MassBasis   -> {W, Wbar},  
  GaugeBasis  -> {Wi[1], Wi[2]},  
  Value       -> {{1/Sqrt[2], -I/Sqrt[2]}, {1/Sqrt[2], I/Sqrt[2]}}  
}
```

MassBasis = Value . GaugeBasis

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Mass Basis
 - Physical or Unphysical Basis
- Gauge Basis
 - Unphysical Basis
- Mixing Matrix
 - Defines Transformation Matrix

MassBasis -> {A, Z},
GaugeBasis -> {B, Wi[3]},
MixingMatrix -> UW,

Mixings

$$\begin{pmatrix} A_\mu \\ Z_\mu \end{pmatrix} = U_w \begin{pmatrix} B_\mu \\ W_\mu^3 \end{pmatrix}$$

```
Mix["13"] == {  
  MassBasis      -> {A, Z},  
  GaugeBasis     -> {B, Wi[3]},  
  MixingMatrix   -> UW,  
  BlockName      -> WEAKMIX  
}
```

Mixings

```
Mix["dq"] == {  
  MassBasis      -> {dq[1, _], dq[2, _], dq[3, _]},  
  GaugeBasis     -> {  
    {QL[2, 1, _], QL[2, 2, _], QL[2, 3, _]},  
    {dR[1, _], dR[2, _], dR[3, _]}  
  },  
  MixingMatrix  -> {CKM, _},  
  Value         -> {_, {{1,0,0}, {0,1,0}, {0,0,1}} },  
  Inverse       -> {True, _}  
}
```

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Vacuum Expectation Values

$M\$vevs = \{ \{ \text{phi1}, \text{vev1} \}, \{ \text{phi2}, \text{vev2} \} \}$

Mixings

`M$vevs = { { phi1, vev1 }, { phi2, vev2 } }`

```
Mix["phi"] == {  
  MassBasis      -> { {h1, h2}, {a1, a2} },  
  GaugeBasis     -> { phi1, phi2 },  
  MixingMatrix  -> { US, UP }  
}
```

$$\begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix} = \frac{1}{\sqrt{2}} \left[\begin{pmatrix} v_1 \\ v_2 \end{pmatrix} + U_s^\dagger \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} + iU_p^\dagger \begin{pmatrix} a_1 \\ a_2 \end{pmatrix} \right]$$

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Built from the Fields, Parameters, etc.

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Built from the Fields, Parameters, etc.
 - Use `ClassName` or `ClassMembers`
 - Antiparticle automatic `psi` → `psibar` or `anti[psi]`
 - Includes γ^0 for fermions
 - Dummy Indices can be used
 - Lorentz/Spin Indices come first
 - Dot/Inner used for anticommuting objects

`gs Ga[mu, s, r] T[a, i, j] dqbar[s, f, i].dq[r, f, j] G[mu, a]`

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Field Strength Tensor
 - FS[G, mu, nu, a]
- Covariant Derivative
 - DC[psi, mu]

$$L = -1/4 \text{ FS}[G, \mu, \nu, a] \text{ FS}[G, \mu, \nu, a] + \int d\bar{q} \text{ Ga}[\mu] \cdot \text{DC}[dq, \mu]$$

Lagrangian

$$\begin{aligned} L = & -1/4 \text{FS}[G, \mu, \nu, a] \text{FS}[G, \mu, \nu, a] \\ & + \int d\bar{q} \text{Ga}[\mu] \text{DC}[dq, \mu] \end{aligned}$$

$$\mathcal{L}^{QCD} \equiv -\frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a + i\bar{d}\not{D}d,$$

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- SUSY
 - Kinetic & Gauge Interactions for Chiral Superfields

```
Theta2Thetabar2Component[ CSFKineticTerms[ ] ]
```

Lagrangian

$$\begin{aligned}\mathcal{L}_{\text{chiral}} &= \left[\Phi_i^\dagger e^{-2g_j V^j} \Phi^i \right]_{\theta \cdot \theta \bar{\theta} \cdot \bar{\theta}} \\ &= D_\mu \phi_i^\dagger D^\mu \phi^i + F_i^\dagger F^i - \frac{i}{2} \left(D_\mu \bar{\psi}_i \bar{\sigma}^\mu \psi^i - \bar{\psi}_i \bar{\sigma}^\mu D_\mu \psi^i \right) \\ &\quad + i\sqrt{2}g_j \bar{\lambda}^{ja} \cdot \bar{\psi}_i T_a \phi^i - i\sqrt{2}g_j \phi_i^\dagger T_a \psi^i \cdot \lambda^{ja} - g_j D^{ja} \phi_i^\dagger T_a \phi^i\end{aligned}$$

Theta2Thetabar2Component [CSFKineticTerms []]

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- SUSY
 - Kinetic & Gauge Interactions for Vector Superfields

```
Theta2Component [ VSFKineticTerms [ ] ] +  
Thetabar2Component [ VSFKineticTerms [ ] ]
```

Lagrangian

$$\begin{aligned}\mathcal{L}_V &= \frac{1}{16g^2} [W^{\alpha a} W_{\alpha a}]_{\theta \cdot \theta} + \text{h.c.} \\ &= -\frac{1}{4} F_a^{\mu\nu} F_{\mu\nu}^a + \frac{i}{2} (\lambda_a \sigma^\mu D_\mu \bar{\lambda}^a - D_\mu \lambda_a \sigma^\mu \bar{\lambda}^a) + \frac{1}{2} D^a D_a\end{aligned}$$

Theta2Component [VSFKineticTerms []] +
Thetabar2Component [VSFKineticTerms []]

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Superpotential
 - Represented here by SuperW

Theta2Component [SuperW] + Thetabar2Component [HC [SuperW]]

Lagrangian

$$\mathcal{L}_W = [W(\Phi)]_{\theta\cdot\theta} + \text{h.c.} = F^i \frac{\partial W(\phi)}{\partial \phi^i} + \frac{1}{2} \frac{\partial^2 W(\phi)}{\partial \phi^i \partial \phi^j} \psi^i \cdot \psi^j + \text{h.c.}$$

Theta2Component [SuperW] + Thetabar2Component [HC [SuperW]]

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Equations of Motion
 - Auxiliary Fields

`SolveEqMotionFD [Lag]`

`SolveEqMotionF [SolveEqMotionD [Lag]]`

FR Model File

- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

- Weyl \rightarrow Dirac Fields

WeylToDirac []

Lagrangian

```
LC=Theta2Thetabar2Component [CSFKineticTerms []];
```

```
LV=Theta2Component [VSFKineticTerms []] +
```

```
Thetabar2Component [VSFKineticTerms []];
```

```
LW=Theta2Component [SuperW] +Thetabar2Component [HC [SuperW]];
```

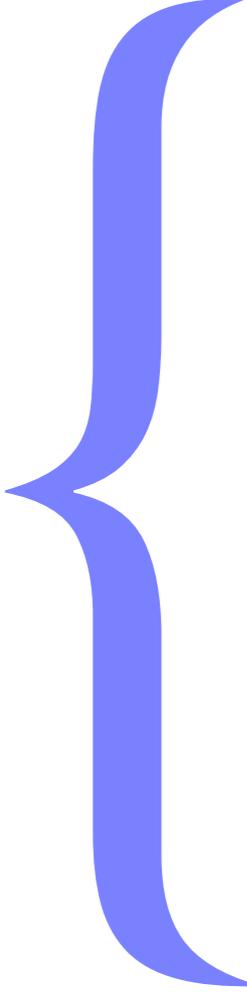
```
Lag = LC + LV + LW;
```

```
SolveEqMotionFD [Lag]
```

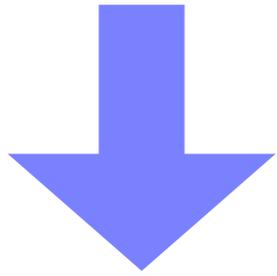
```
SolveEqMotionF [SolveEqMotionD [Lag]]
```

```
WeylToDirac []
```

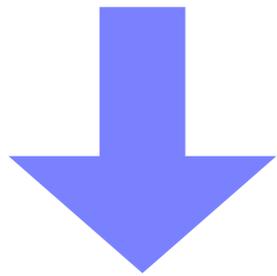
FR Model File

- 
- Model Info
 - Indices
 - Parameters
 - Fields
 - Superfields
 - Gauge Groups
 - Restrictions
 - Mixings
 - Lagrangian

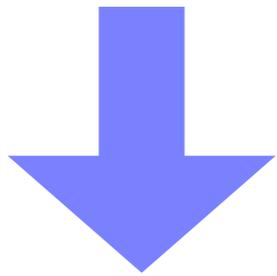
Model



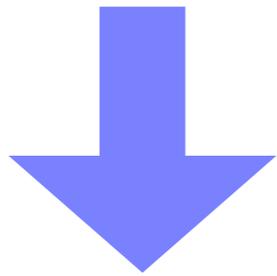
FR Model File



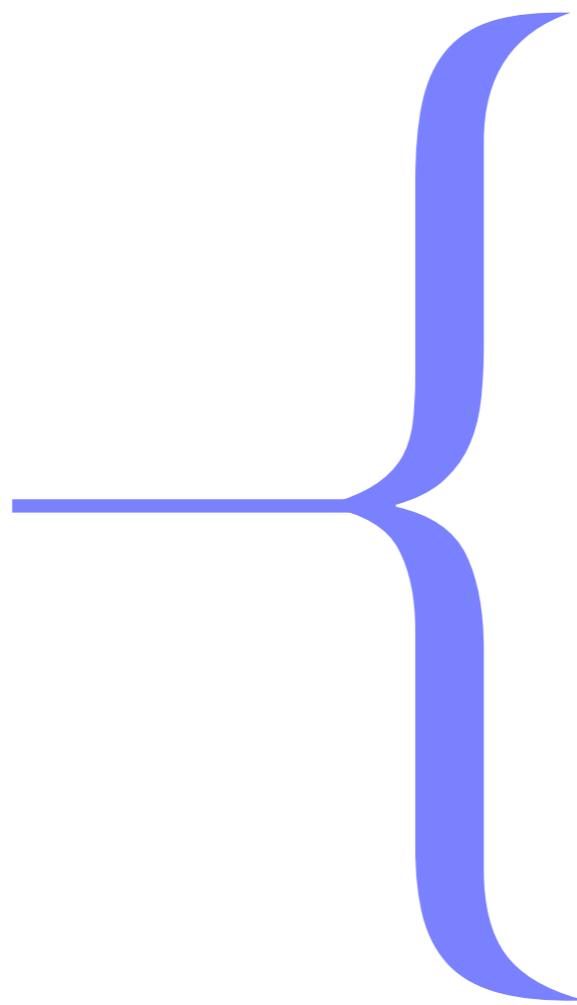
FeynRules



Validation

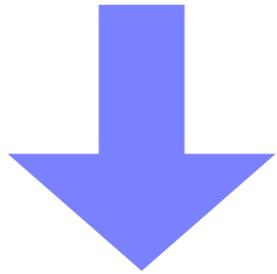


MadGraph

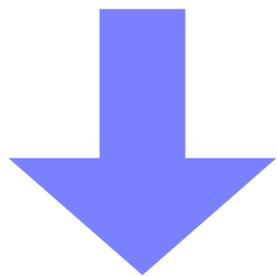


- Model Info
- Indices
- Parameters
- Fields
- Superfields
- Gauge Groups
- Restrictions
- Mixings
- Lagrangian

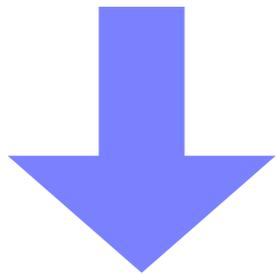
Model



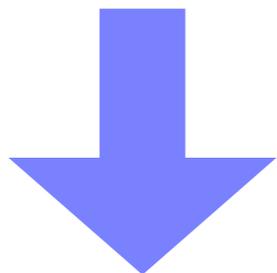
FR Model File



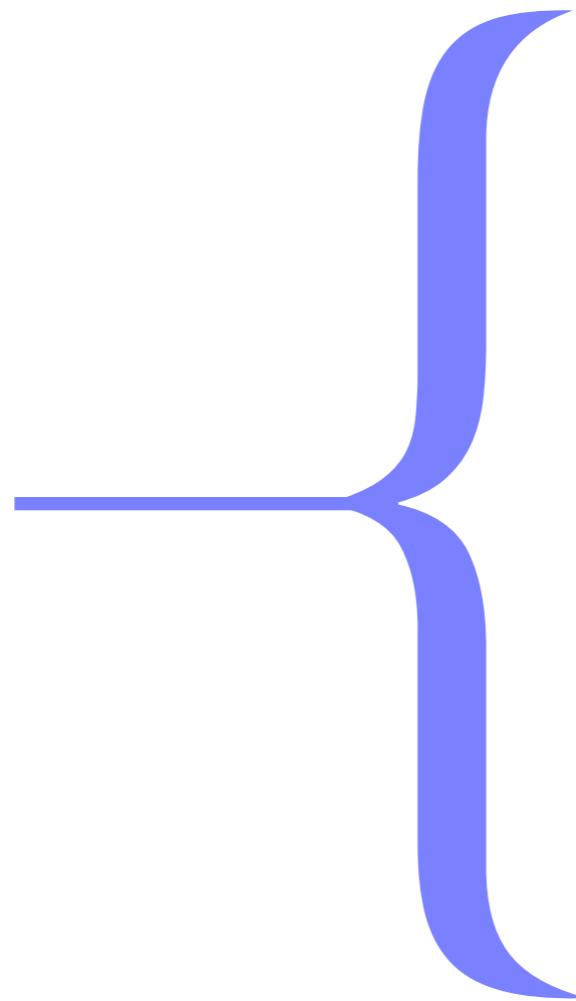
FeynRules



Validation

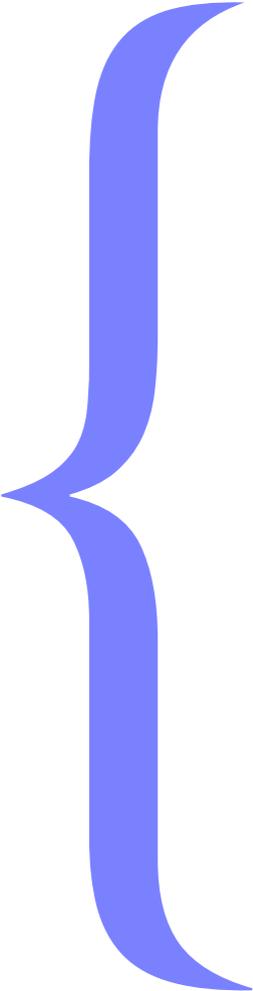


MadGraph

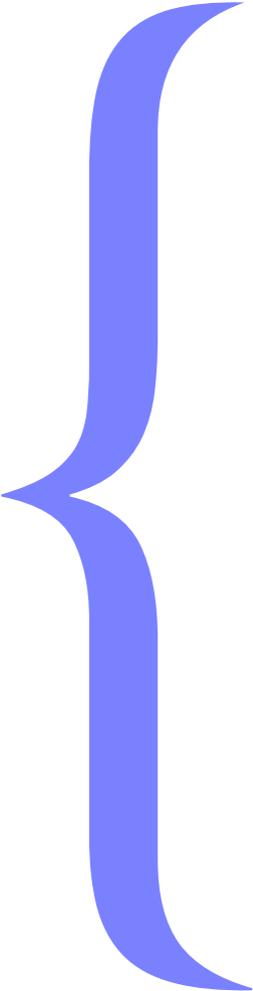


- Load FeynRules
- Load Model
- Update Parameters
- Check Hermiticity, Mass Diagonalization, etc.
- Check Feynman Rules
- Update Widths
- Export to Simulation Tool (UFO)

FeynRules

- 
- Load FeynRules
 - Load Model
 - Update Parameters
 - Check Hermiticity, Mass Diagonalization, etc.
 - Check Feynman Rules
 - Update Widths
 - Export to Simulation Tool (UFO)

FeynRules

- 
- Load FR
 - Load Model
 - Update Pars
 - Run Checks
 - Feyn. Rules
 - Widths
 - Export

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Set \$FeynRulesPath
- Set Directory
- <<FeynRules`

```
$FeynRulesPath = SetDirectory[ <the address of the package> ];  
<< FeynRules`
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Set Directory
 - Else output will be put in FR directory
- Load Model

```
LoadModel[ < file.fr >, < file2.fr >, ... ]
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Set Directory
 - Else output will be put in FR directory
- Load Model
- Load Restrictions

```
LoadModel[ < file.fr >, < file2.fr >, ... ]
```

```
LoadRestriction[ file1.rst, file2.rst, ... ]
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Update Parameters

```
UpdateParameters[ gs -> 0.118 , ee -> 0.33 ]
```

```
ReadLHAFile[ Input -> "LH-file" ]
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Check Hermiticity
- Check Mass Spectrum

```
CheckHermiticity[  $\mathcal{L}$  ];
```

```
CheckMassSpectrum[  $\mathcal{L}$ , options ]
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- FeynmanRules
 - ScreenOutput
 - FlavorExpand
 - MinParticles
 - MaxParticles
 - SelectParticles
 - Contains
 - Free

```
vertsQCD = FeynmanRules [ LQCD ] ;
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Many SUSY Commands

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

- Compute Widths
- Update Widths

```
vertices = FeynmanRules[ L ];  
decays = ComputeWidths[ vertices ];  
UpdateWidths[ decays ];
```

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- **Export**

Export

● Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

● Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

● FeynRules Core

- Does Not Require these Conventions

● Feynman Diagram Calculators

- Do Require these Conventions

● Export Interfaces

- Do Require these Conventions

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- Pure ASCII

- ParticleName
- AntiParticleName

```
ParticleName      -> {"ne", "nm", "nt"},  
AntiParticleName -> {"ne~", "nm~", "nt~"}
```

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- Particle Data Group ID

- Many particles already numbered
- New particles should be numbered starting from 9000001
- FR will automatically assign these

PDG \rightarrow {2,4,6}

Export

- Conventions
 - Name Restrictions
 - PDG ID
 - SM Restrictions
 - Gauge Choice
 - Interaction Order
- Interfaces
 - ASperGe
 - CalcHEP
 - FeynArts
 - Sherpa
 - TeX
 - UFO
 - Whizard

- Some SM parameters fixed:
 - α_s (Strong Coupling)
 - g_s (Strong Coupling)
 - α_{EW1} (EW Coupling)
 - G_f (Fermi Constant)
 - e_e (Electric Coupling)

SM Parameters

```
aS == {  
  ParameterType    -> External,  
  BlockName        -> SMINPUTS,  
  OrderBlock       -> 3,  
  Value            -> 0.1184,  
  InteractionOrder -> {QCD,2},  
  Description      -> "Strong coupling constant at the Z pole"  
},
```

```
gs == {  
  ParameterType    -> Internal,  
  Value            -> Sqrt[4 Pi aS],  
  InteractionOrder -> {QCD,1},  
  ParameterName    -> G,  
  Description      -> "Strong coupling constant at the Z pole"  
},
```

SM Parameters

```
Gf == {  
  ParameterType  -> External,  
  BlockName      -> SMINPUTS,  
  OrderBlock     -> 2,  
  Value          -> 1.16637*^-5,  
  InteractionOrder -> {QED,2},  
  Description    -> "Fermi constant"  
},
```

SM Parameters

```
aEWM1 == {
  ParameterType    -> External,
  BlockName        -> SMINPUTS,
  OrderBlock       -> 1,
  Value            -> 127.9,
  InteractionOrder -> {QED,-2},
  Description      -> "Inverse of the EW coupling constant at the Z pole"
},
aEW == {
  ParameterType    -> Internal,
  Value            -> 1/aEWM1,
  InteractionOrder -> {QED,2},
  Description      -> "Electroweak coupling constant"
},
ee == {
  ParameterType    -> Internal,
  Value            -> Sqrt[4 Pi aEW],
  InteractionOrder -> {QED,1},
  Description      -> "Electric coupling constant"
}
```

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- QCD Structure

- Gauge group declaration
- Indices

QCD

```
SU3C == {  
    Abelian          -> False,  
    CouplingConstant -> gs,  
    GaugeBoson      -> G,  
    StructureConstant -> f,  
    Representations  -> {{T, Colour},  
                        {T6, Sextet}},  
    SymmetricTensor  -> dSUN  
}
```

```
IndexRange[ Index[ Colour ] ] = Range[3];  
IndexRange[ Index[ Sextet ] ] = Range[6];  
IndexRange[ Index[ Gluon ] ] = Range[8];
```

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- InteractionOrder

- How many powers of a fundamental coupling

- Hierarchy

- The hierarchy of fundamental couplings

- OrderLimit

- The largest power of a fundamental coupling in a diagram

Interaction Order

InteractionOrder -> {QCD,2}

InteractionOrder -> {QED,1}

```
M$InteractionOrderHierarchy = {  
  {QCD,1},  
  {NP,1},  
  {QED,2}  
}
```

```
M$InteractionOrderLimit = {  
  {NP,2}  
}
```

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- Automatic Mass Diagonalization

- WriteASperGe[Lag, options]
- Requires Gnu Scientific Library (GSL)

```
WriteASperGe[ Lag, Output -> dirname ]
```

```
./ASperGe <inputfile> <outputfile>
```

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- CalcHEP Output

- WriteCHOutput[Lag, options]
- Options:
 - CHAutoWidths : Automatic width calculation
 - LHASupport : Support for reading LHA files

WriteCHOutput [$\mathcal{L}_1, \mathcal{L}_2, \dots, options$]

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- FeynArts Output

- WriteFeynArtsOutput[Lag, options]
- Completely general operators supported (.gen file)

WriteFeynArtsOutput [$\mathcal{L}_1, \mathcal{L}_2, \dots, options$]

Export

- Conventions
 - Name Restrictions
 - PDG ID
 - SM Restrictions
 - Gauge Choice
 - Interaction Order
- Interfaces
 - ASperGe
 - CalcHEP
 - FeynArts
 - Sherpa
 - TeX
 - UFO
 - Whizard

- Sherpa Output
 - WriteSHOutput[Lag, options]

WriteSHOutput [$\mathcal{L}_1, \mathcal{L}_2, \dots, options$]

Export

- Conventions
 - Name Restrictions
 - PDG ID
 - SM Restrictions
 - Gauge Choice
 - Interaction Order
- Interfaces
 - ASperGe
 - CalcHEP
 - FeynArts
 - Sherpa
 - TeX
 - UFO
 - Whizard

- TeX Output
 - WriteLaTeXOutput[Lag, Verts, options]

WriteLaTeXOutput [$\mathcal{L}_1, \mathcal{L}_2, \dots, V_1, V_2, \dots, options$]

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- Universal FeynRules Output

- WriteUFO[Lag, options]
- Options:
 - AddDecays : Automatic
1 → 2 Decays
- Supported by Aloha, MadGraph5, MadAnalysis5
- Planned support by GoSam and Herwig++

WriteUFO[$\mathcal{L}_1, \mathcal{L}_2, \dots, options$]

Export

- Conventions

- Name Restrictions
- PDG ID
- SM Restrictions
- Gauge Choice
- Interaction Order

- Interfaces

- ASperGe
- CalcHEP
- FeynArts
- Sherpa
- TeX
- UFO
- Whizard

- Whizard Output

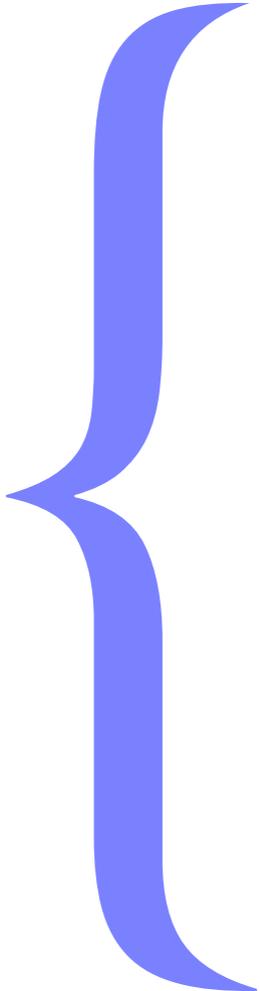
- WriteWOOutput[Lag, options]
- Options:
 - WOAutoGauge :
Automatically generate R_ξ gauge from Feynman gauge

`WriteWOOutput [$\mathcal{L}_1, \mathcal{L}_2, \dots, options$]`

FeynRules

- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- **Export**

FeynRules

- 
- Load FR
 - Load Model
 - Update Pars
 - Run Checks
 - Feyn. Rules
 - Widths
 - Export

Significantly Faster

Efficiency

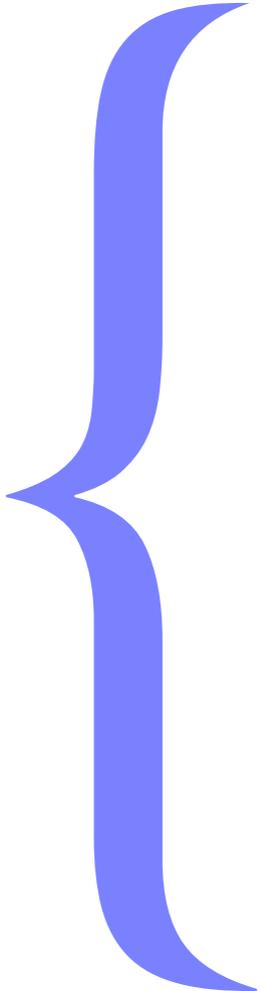
SM

Command	FR 1.6	FR 2.0 - 1	FR 2.0 - 2	FR 2.0 - 4	FR 2.0 - 8
FeynmanRules	5.84 s	4.98 s	3.09 s	2.32 s	1.93 s
WriteCHOutput	9.33 s	9.51 s	8.05 s	6.26 s	5.53 s
WriteUFO	9.05 s	8.82 s	7.89 s	6.51 s	6.05 s

MSSM

Command	FR 1.6	FR 2.0 - 1	FR 2.0 - 2	FR 2.0 - 4	FR 2.0 - 8
FeynmanRules	325.5 s	213.7 s	79.7 s	62.6 s	41.0 s
WriteCHOutput	853.4 s	618.9 s	350.8 s	283.9 s	204.4 s
WriteUFO	436.0 s	518.5 s	316.1 s	273.8 s	239.7 s

FeynRules

- 
- Load FR
 - Load Model
 - Update Pars
 - Run Checks
 - Feyn. Rules
 - Widths
 - Export

Model Database

ModelDatabaseMainPage - FeynRules

feynrules.irmp.ucl.ac.be/wiki/ModelDatabaseMainPage Reader

Home Apple Yahoo! Google News Jobs Social Finite Simple Groups Buses HTML

- ✉ fuks@cern.ch
- ✉ cdegrand@illinois.edu

Available models

Standard Model	The SM implementation of FeynRules, included into the distribution of the FeynRules package.
Simple extensions of the SM (15)	Several models based on the SM that include one or more additional particles, like a 4th generation, a second Higgs doublet or additional colored scalars.
Supersymmetric Models (5)	Various supersymmetric extensions of the SM, including the MSSM, the NMSSM and many more.
Extra-dimensional Models (4)	Extensions of the SM including KK excitations of the SM particles.
Strongly coupled and effective field theories (8)	Including Technicolor, Little Higgs, as well as SM higher-dimensional operators, vector-like quarks.
Miscellaneous (0)	

[Edit this page](#)
[Attach file](#)
[Rename page](#)
[Delete this version](#)
[Delete page](#)

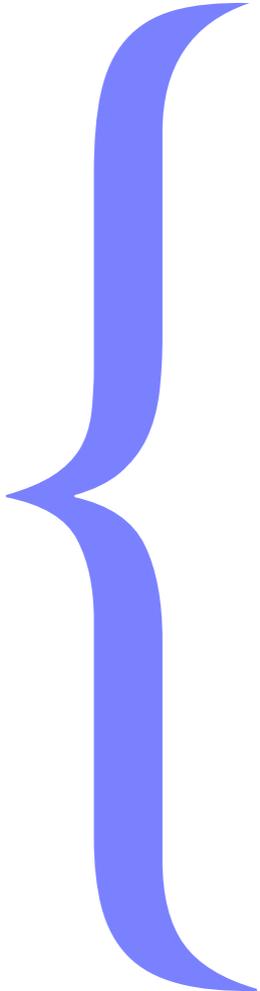
FeynRules model database: Supersymmetric models

This page contains a collection of supersymmetric models that are already implemented in FeynRules. For each model, a complete model-file is available, containing all the information that is needed, as well as the Lagrangian, as well as the references to the papers where this Lagrangian was taken from. All model-files can be freely downloaded and changed, serving like this as the starting point for building new models. A TeX-file for each model containing a summary of the Feynman Rules produced by FeynRules is also available.

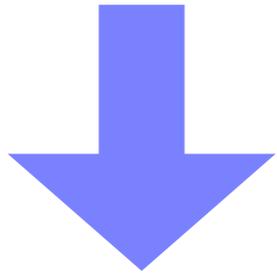
Model	Short Description	Contact	Status
MSSM	The Minimal Supersymmetric extension of the SM.	✉ B. Fuks	Available
NMSSM	The Next-to-Minimal Supersymmetric Standard Model.	✉ B. Fuks	Available
RPV-MSSM	The Minimal Supersymmetric extension of the SM including R-parity violation (trilinear RPV interactions only).	✉ B. Fuks	Available
R-MSSM	A R-symmetric supersymmetric extension of the SM.	✉ B. Fuks	Available
gld-grv	Extension of the MSSM containing goldstino and gravitino couplings to the supercurrent.	✉ B. Fuks	Available

Back to the [FeynRules model database](#).

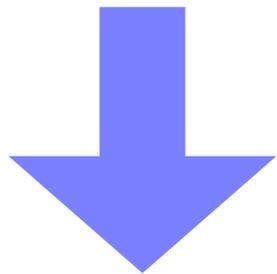
FeynRules

- 
- Load FR
 - Load Model
 - Update Pars
 - Run Checks
 - Feyn. Rules
 - Widths
 - Export

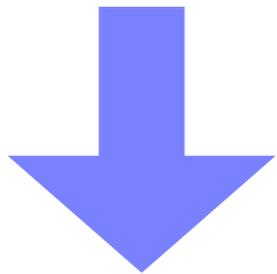
Model



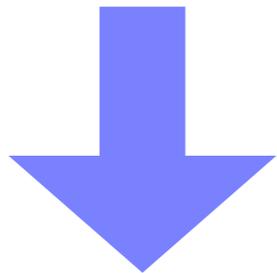
FR Model File



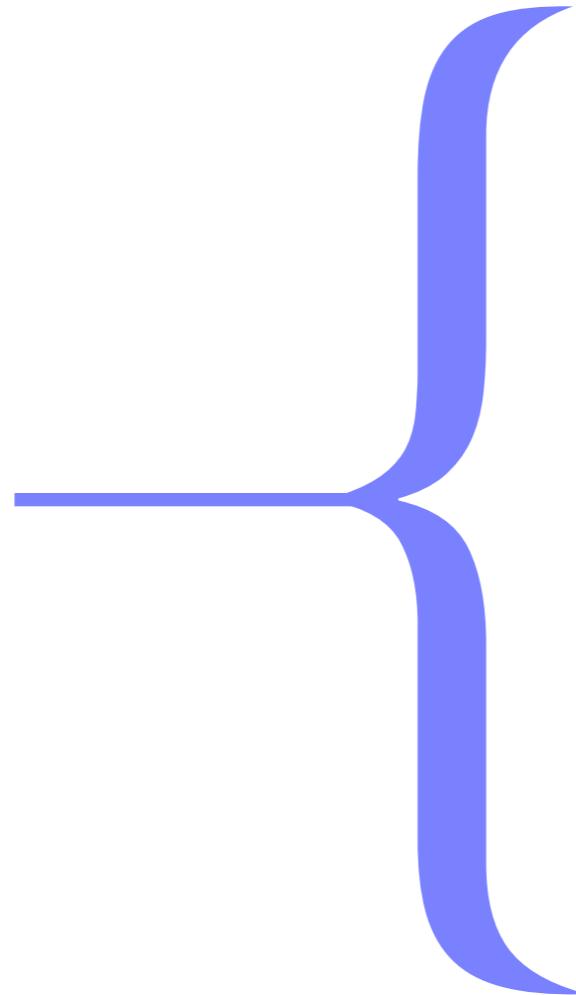
FeynRules



Validation

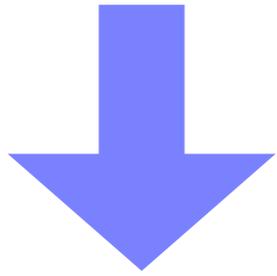


MadGraph

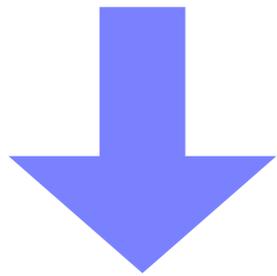


- Load FR
- Load Model
- Update Pars
- Run Checks
- Feyn. Rules
- Widths
- Export

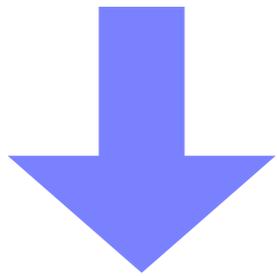
Model



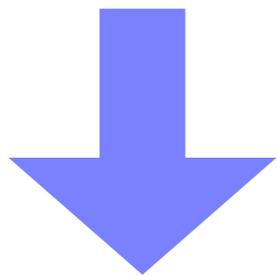
FR Model File



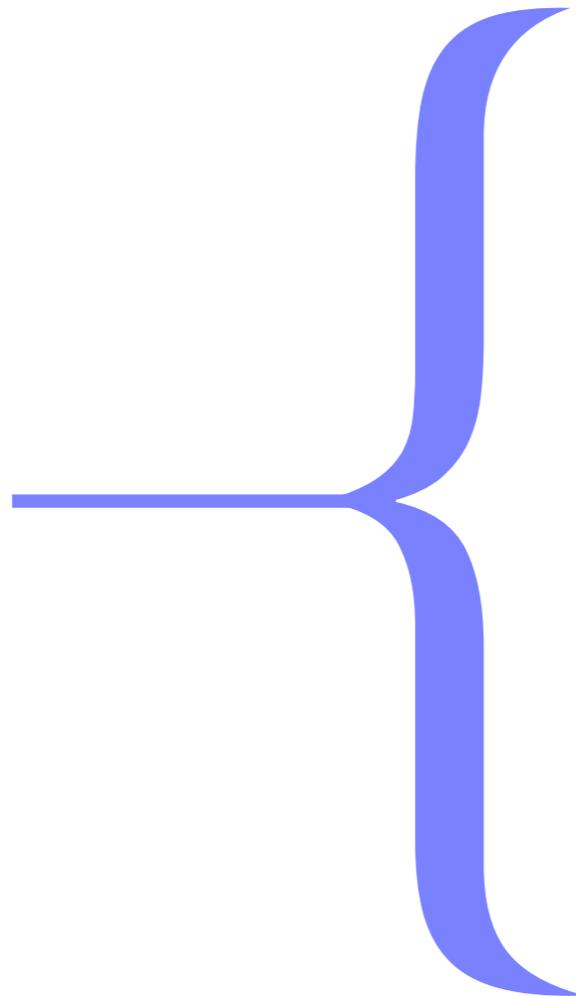
FeynRules



Validation



MadGraph



- Documentation
- Sanity Checks
- Test 1 Generator
- Test Several Generators
- Web Validation
- Debugging

Validation

- Documentation
- Sanity Checks
- 1 Generator
- >1 Generators
- Web Validation
- Debugging

Validation

- Documentation
- Sanity Checks
- 1 Generator
- >1 Generators
- Web Validation
- Debugging

● Tracibility & Reproducibility

- Model Theory References
- Model Implementation Details
- Validation Details
- Software Versions

Validation

- Documentation
- Sanity Checks
- 1 Generator
- > 1 Generators
- Web Validation
- Debugging

- Hermiticity
- Gauge Invariance
- Agreement with literature

Validation

- Documentation
- Sanity Checks
- 1 Generator
- >1 Generators
- Web Validation
- Debugging

- Numerical Cross Sections/Widths
 - Compared with literature
 - Gauge Invariance
 - Unitarity Cancellations
 - Comparison with SM results where appropriate

Validation

- Documentation
- Sanity Checks
- 1 Generator
- > 1 Generators
- Web Validation
- Debugging

- Between Generators
 - Large set of processes
 - Gauge invariance
 - With independent implementations if available

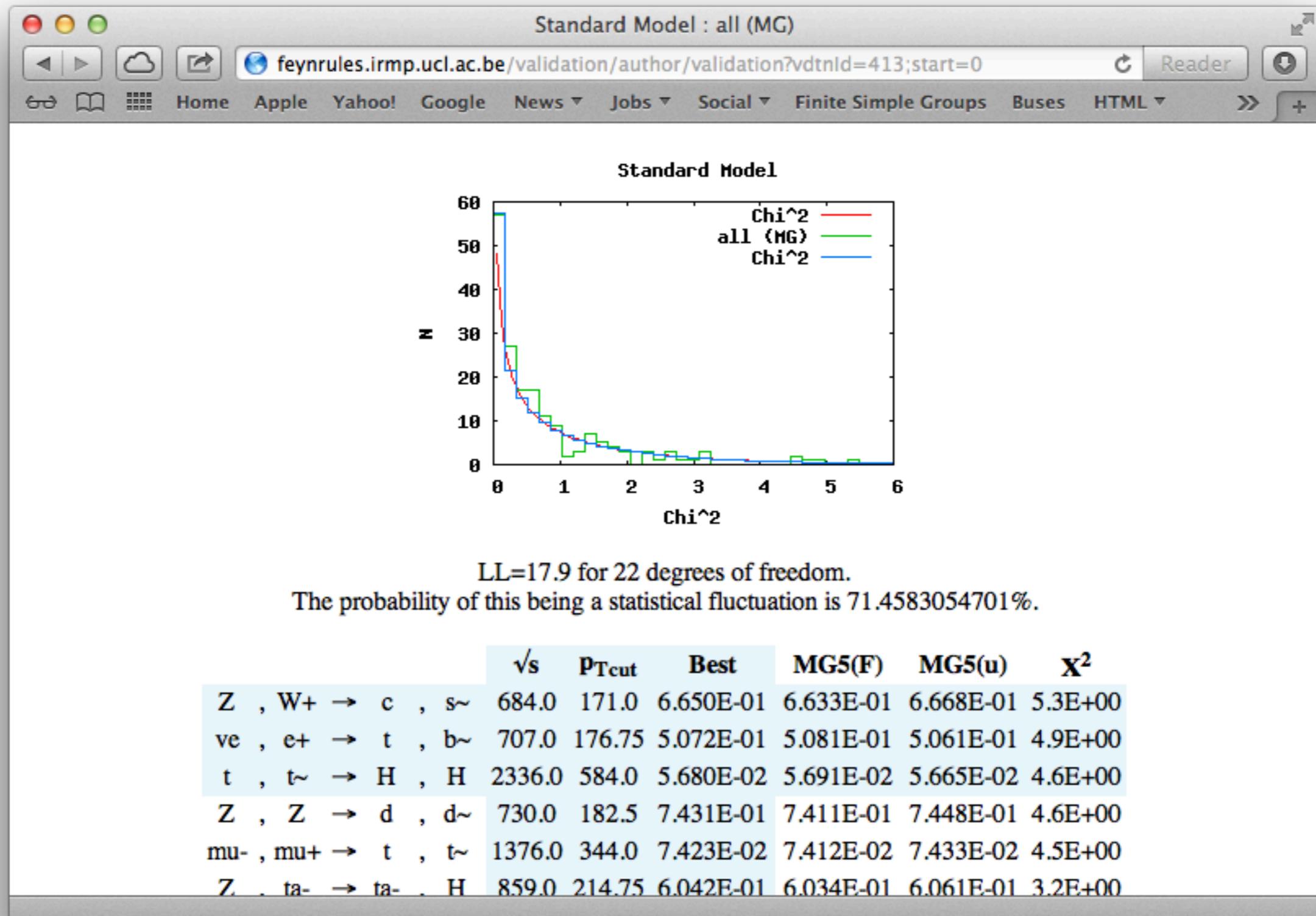
Validation

- Documentation
- Sanity Checks
- 1 Generator
- >1 Generators
- Web Validation
- Debugging

- Automated comparison
 - All $2 \rightarrow 2$ processes
 - Feynman & unitary gauges
 - CalcHEP
 - MadGraph
 - Whizard
 - Need username/password

<http://feynrules.phys.ucl.ac.be/validation>

Web Validation

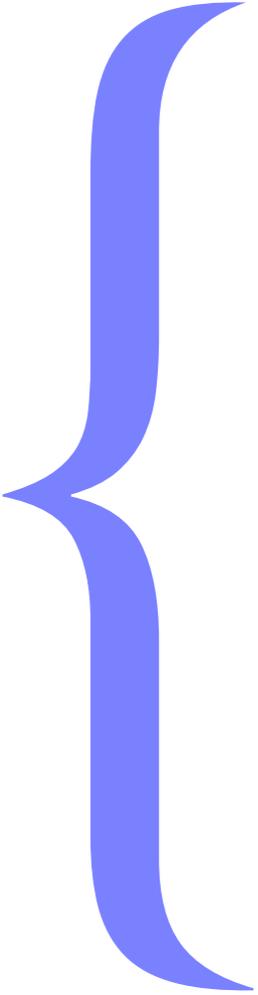


Validation

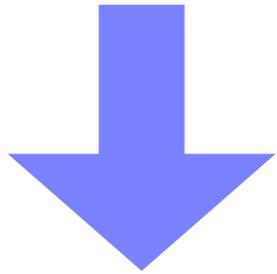
- Documentation
- Sanity Checks
- 1 Generator
- >1 Generators
- Web Validation
- Debugging

- Comment Out
 - Syntax errors can be found by commenting out until the error is found.
- Web validation
 - Help find problematic vertices

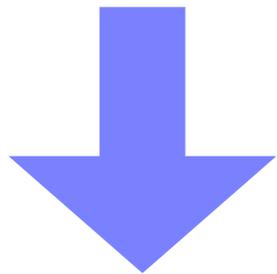
Validation

- 
- Documentation
 - Sanity Checks
 - 1 Generator
 - > 1 Generators
 - Web Validation
 - Debugging

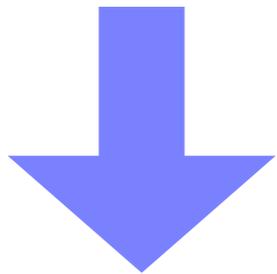
Model



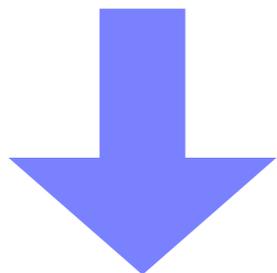
FR Model File



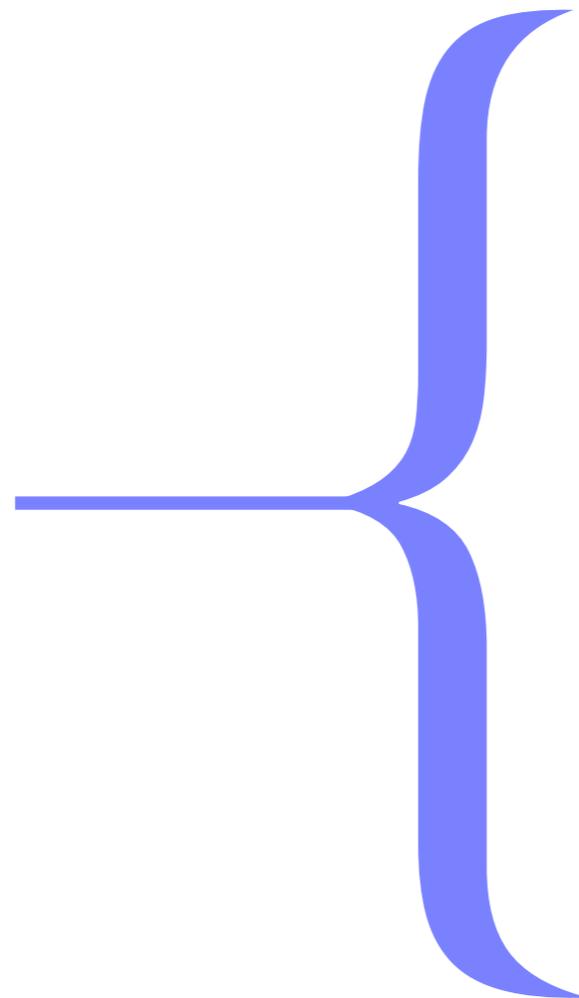
FeynRules



Validation

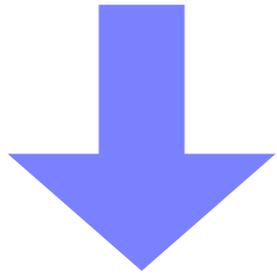


MadGraph

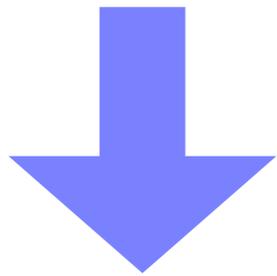


- Documentation
- Sanity Checks
- 1 Generator
- > 1 Generators
- Web Validation
- Debugging

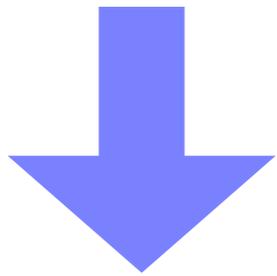
Model



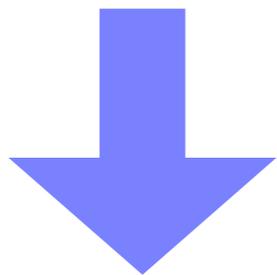
FR Model File



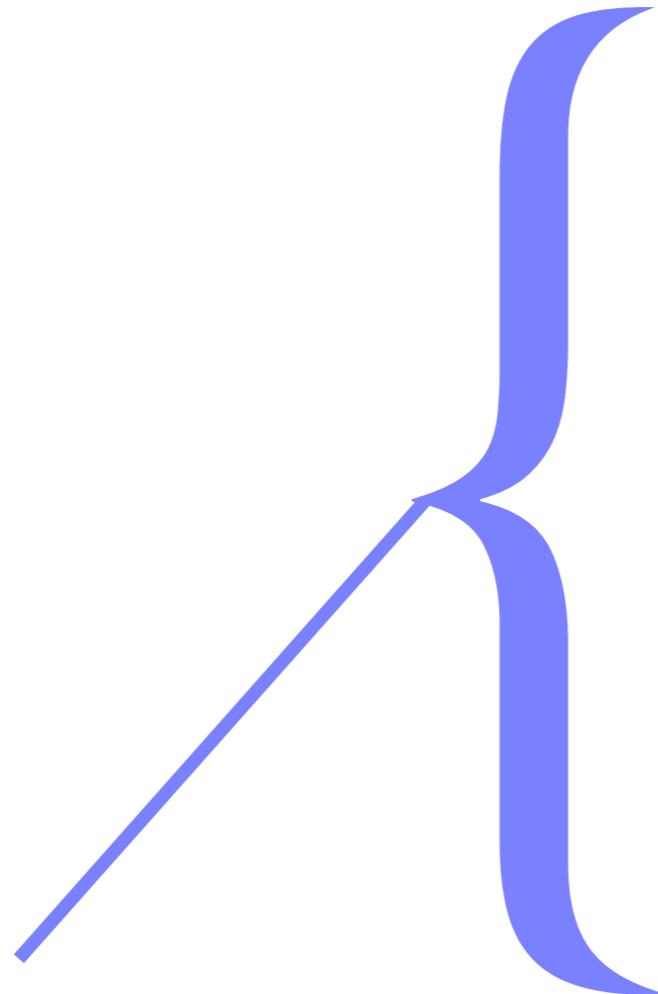
FeynRules



Validation



MadGraph



- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

- UFO Model Dir
 - Copy the UFO Model dir to the MadGraph5 models dir

```
cp -r ModelName_UFO ../MadGraph5_v1_5_12/models/.
```

MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

- Load UFO Model
 - During MG5 session

```
mg5>import model ModelName_UFO
```

MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

- Import UFO Model
 - During MG5 session
- Like Built-In Model
 - Everything from this point like a built-in model

```
mg5>import model ModelName_UFO
```

MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

- For example:
 - check process
 - Gauge invariance
 - Lorentz invariance
 - Permutation

```
mg5>check p p > uv uv~
```

MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- ...

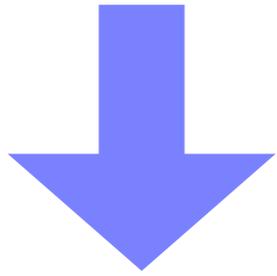
- Like Built-In Models
 - generate
 - output
 - launch
 - ...

```
mg5>generate p p > uv uv~  
mg5>output  
mg5>launch
```

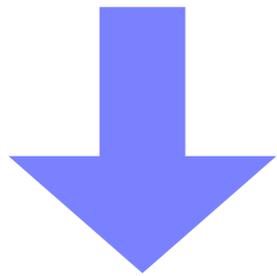
MadGraph

- Load UFO into MG5
- Run MG5 Tests
- Run Simulations
- Enjoy!

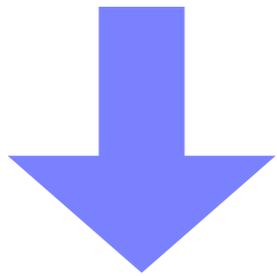
Model



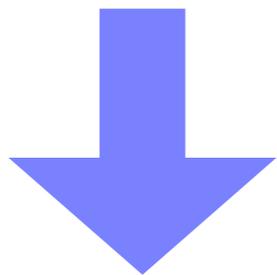
FR Model File



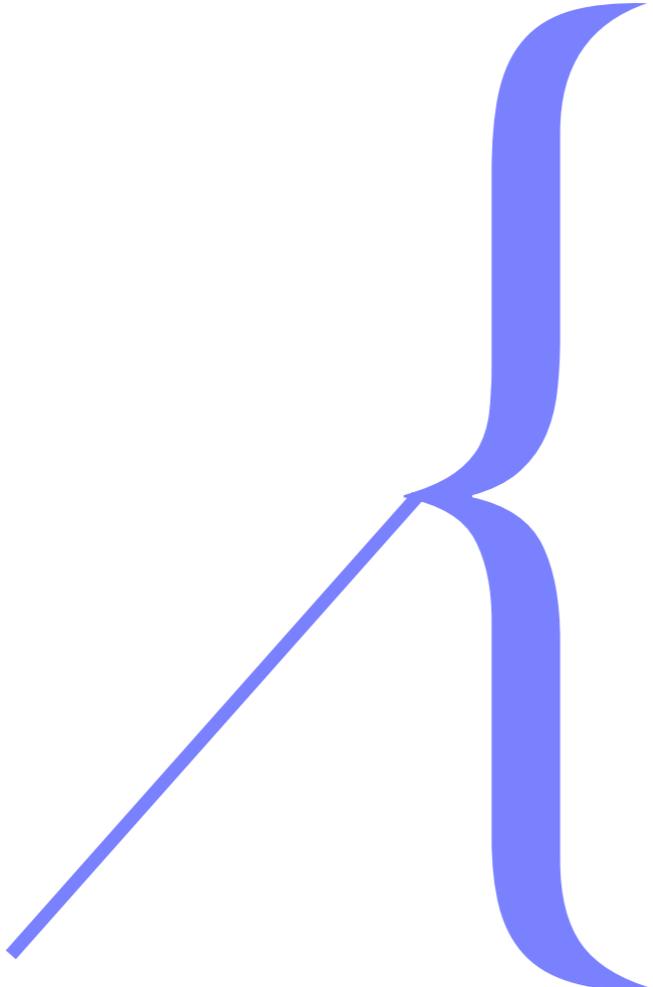
FeynRules



Validation



MadGraph

- 
- A large blue curly brace on the right side of the diagram, grouping the list of actions with the MadGraph step.
- Load **UFO** into MG5
 - Run MG5 Tests
 - Run Simulations
 - Enjoy!

UFO & ALOHA

- UFO
- ALOHA

- Universal FeynRules Output
 - DeGrande, Duhr, Fuks, Grellscheid, Mattelaer and Reiter (CPC 183, 1201 (2012))
 - Full FeynRules model info included

UFO & ALOHA

- UFO
- ALOHA

- Universal FeynRules Output
 - DeGrande, Duhr, Fuks, Grellscheid, Mattelaer and Reiter (CPC 183, 1201 (2012))
 - Full FeynRules model info included
- Not tied to specific matrix element generator (universal)
 - Default model format for MadGraph 5, GoSam and Herwig++(future)

UFO & ALOHA

- UFO
- ALOHA

- Universal FeynRules Output
 - DeGrande, Duhr, Fuks, Grellscheid, Mattelaer and Reiter (CPC 183, 1201 (2012))
 - Full FeynRules model info included
- Not tied to specific matrix element generator (universal)
 - Default model format for MadGraph 5, GoSam and Herwig++(future)
- General operators supported
 - Completely general Lorentz structures
 - 4-fermion operators
 - operators with >4 particles
 - 3, 6 and 8 color reps supported

UFO & ALOHA

- UFO
- ALOHA

- Automatic Language-Independent Output of Helicity Amplitudes
 - de Aquino, Link, Maltoni, Mattelaer and Steltzer (CPC 183, 2254 (2012))
 - Convert UFO Lorentz structure to Fortran/C++ code required to calculate helicity amplitudes



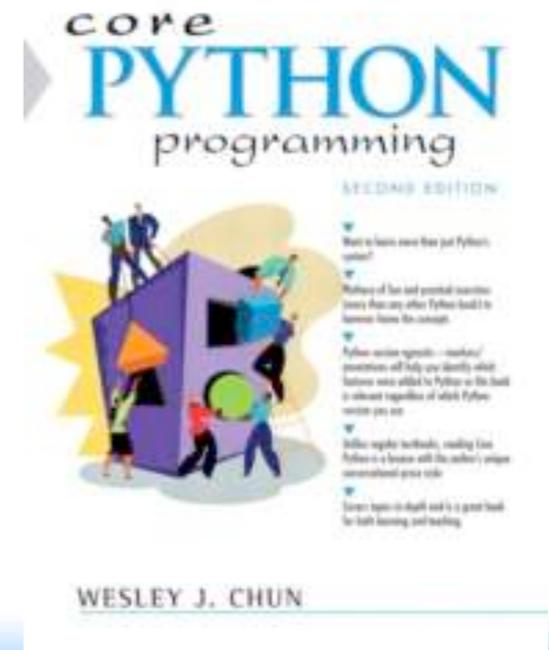
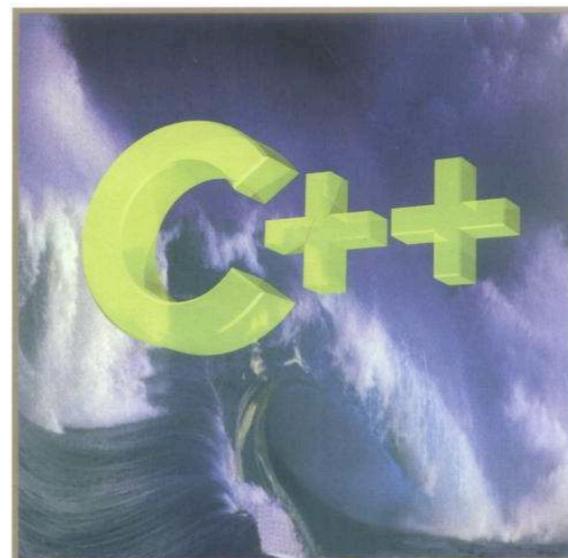
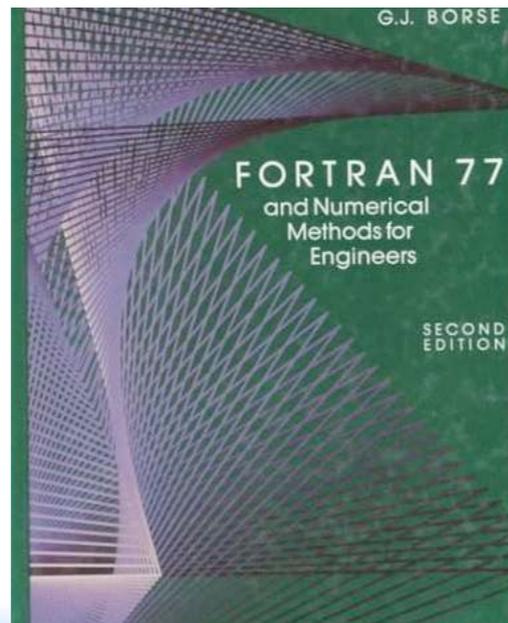
ALOHA

ALOHA
~~Google~~ translate

From: [UFO] To: Helicity [Translate]

```
VVVV6 = Lorentz(name = 'VVVV6',
                spins = [ 3, 3, 3, 3 ],
                structure = 'Metric(1,4)*Metric(2,3) -Metric(1,3)*Metric(2,4)')
```

Type text or a website address or translate a document.





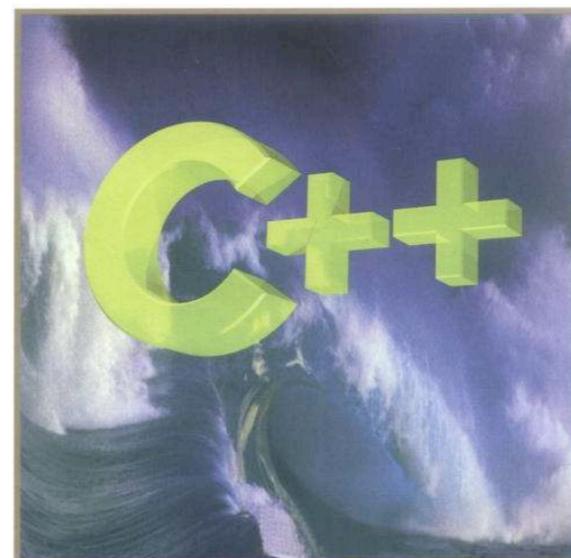
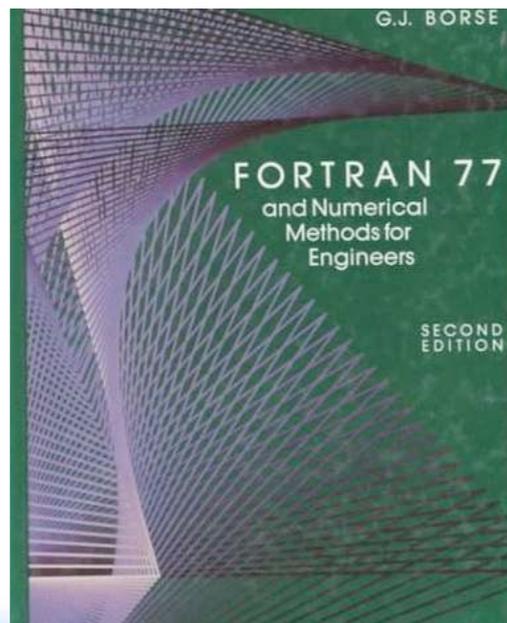
ALOHA

ALOHA
~~Google~~ translate

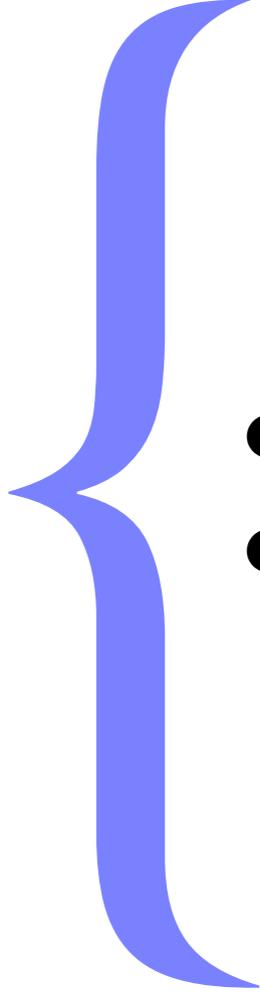
From: [UFO] To: Helicity [Translate]

```
VERTEX = COUP*( (V4(1)*( (V2(1)*( (0, -1)*(V3(2)*V1(2))
$ +(0, -1)*(V3(3)*V1(3))+0, -1)*(V3(4)*V1(4))))+(V1(1)*( (0, 1)
$ *(V3(2)*V2(2))+0, 1)*(V3(3)*V2(3))+0, 1)*(V3(4)*V2(4))))))
$ +( (V4(2)*( (V2(2)*( (0, -1)*(V3(1)*V1(1))+0, 1)*(V3(3)*V1(3))
$ +(0, 1)*(V3(4)*V1(4))))+(V1(2)*( (0, 1)*(V3(1)*V2(1))+0,
$ -1)*(V3(3)*V2(3))+0, -1)*(V3(4)*V2(4))))))+( (V4(3)*( (V2(3)
```

Type text or a website address or translate a document.

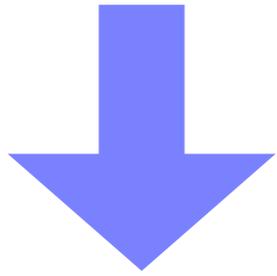


UFO & ALOHA

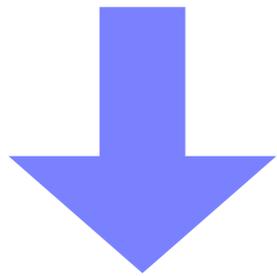


- UFO
- ALOHA

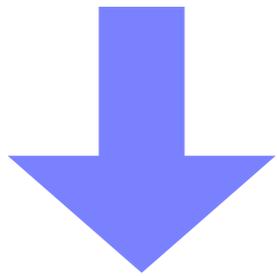
Model



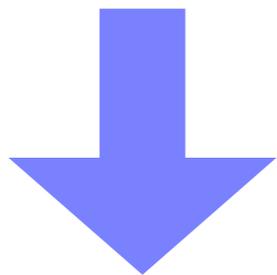
FR Model File



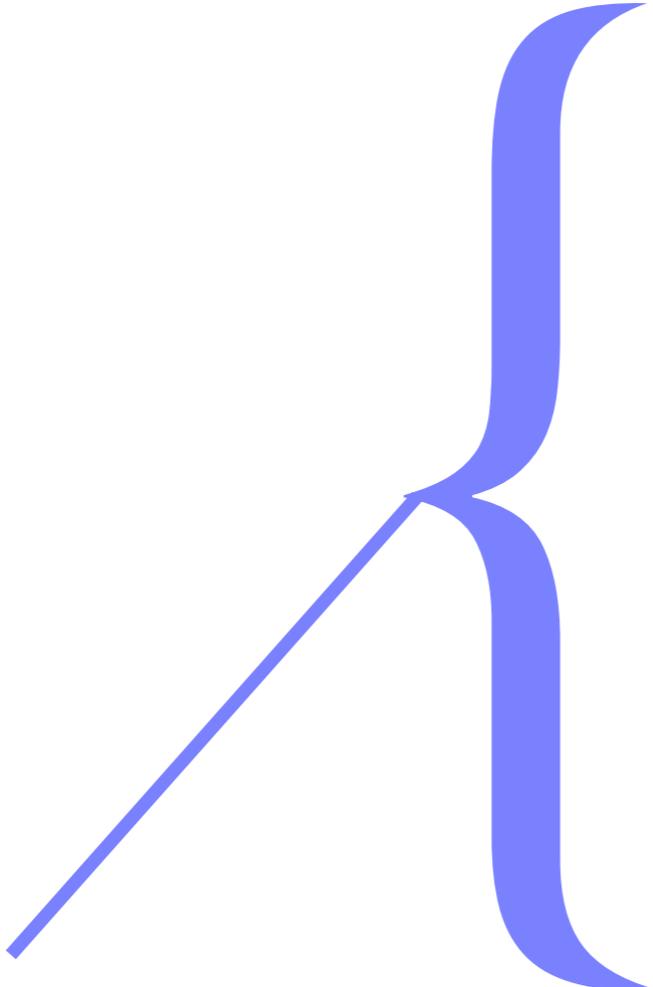
FeynRules



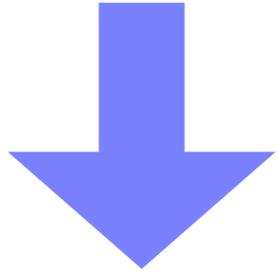
Validation



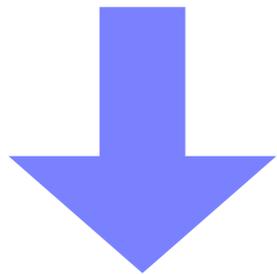
MadGraph

- 
- A large blue curly brace on the right side of the diagram, grouping the four steps: FeynRules, Validation, and MadGraph, and pointing to a list of actions.
- Load **UFO** into MG5
 - Run MG5 Tests
 - Run Simulations
 - Enjoy!

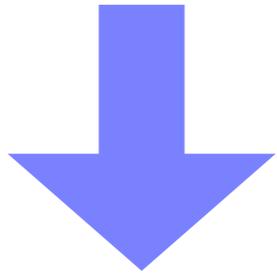
Model



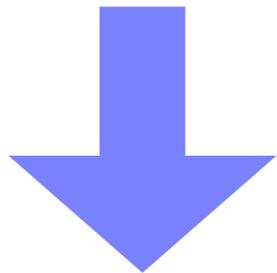
FR Model File



FeynRules



Validation



MadGraph

FeynRules Future

- InSurGe
- FR@NLO
- Galileo

- One-loop renormalization equations
 - Alloul, de Causmaecker and Fuks
 - Generic SUSY models

FeynRules Future

- InSurGe
- FR@NLO
- Galileo

- Automatic Counterterms
 - Degrande, Duhr, Fuks and Hahn

FeynRules Future

- InSurGe
- FR@NLO
- Galileo

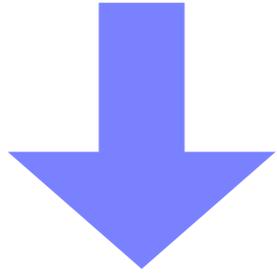
- Models from symmetry
 - Christensen, Salmon, Setzer, Stefanus

FeynRules Future

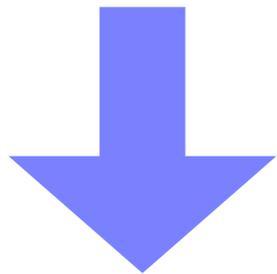
- InSurGe
- FR@NLO
- **Galileo**

- Models from symmetry
 - Christensen, Salmon, Setzer, Stefanus

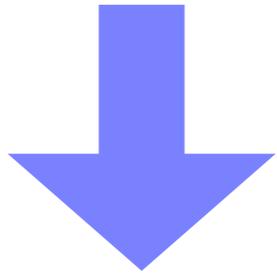
Model



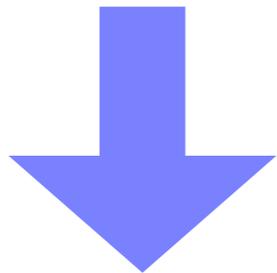
FR Model File



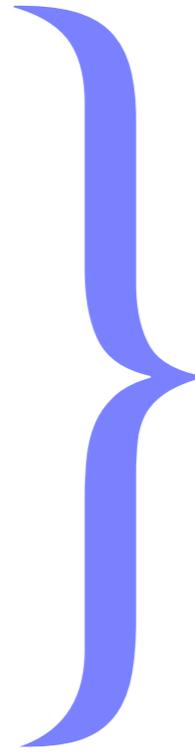
FeynRules



Validation



MadGraph



Galileo

- Models from symmetry
 - Christensen, Salmon, Setzer, Stefanus

$SU(3)_c \times SU(2)_W \times U(1)_Y$

Q_c	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_c	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
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Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu} F_c^{\mu\nu} - \frac{1}{4} F_{w,\mu\nu} F_w^{\mu\nu} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices
- Rotate fields to mass basis

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices
- Rotate fields to mass basis
- Calculate Feynman diagrams

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
\mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
& + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
& + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
& - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
\end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices
- Rotate fields to mass basis
- Calculate Feynman diagrams
- Implement Feynman rules into CH, FA, MG, SH, WO

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices
- Rotate fields to mass basis
- Calculate Feynman diagrams
- Implement Feynman rules into CH, FA, MG, SH, WO
- Implement Lagrangian into FR

	$SU(3)_c$	$SU(2)_W$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\begin{aligned}
 \mathcal{L} = & -\frac{1}{4} F_{c,\mu\nu} F_c^{\mu\nu} - \frac{1}{4} F_{w,\mu\nu} F_w^{\mu\nu} - \frac{1}{4} F_{y,\mu\nu} F_y^{\mu\nu} \\
 & + i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R \\
 & + \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 \\
 & - \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.
 \end{aligned}$$

- Insert vevs
- Expand Lagrangian
- Collect quadratic terms
- Diagonalize mass matrices
- Rotate fields to mass basis
- Calculate Feynman diagrams
- Implement Feynman rules into CH, FA, MG, SH, WO
- Implement Lagrangian into FR
- Do calculations

	$SU(3)_c$	$SU(2)_w$	$U(1)_Y$
Q_L	3	2	$1/6$
U_R	3	1	$2/3$
d_R	3	1	$-1/3$
L_L	1	2	$-1/2$
e_R	1	1	-1
Φ	1	2	$1/2$

$$\mathcal{L} = -\frac{1}{4} F_{c,\mu\nu}^a F_c^{\mu\nu a} - \frac{1}{4} F_{w,\mu\nu}^a F_w^{\mu\nu a} - \frac{1}{4} F_{Y,\mu\nu} F_Y^{\mu\nu}$$

$$+ i \bar{Q}_L \not{D} Q_L + i \bar{U}_R \not{D} U_R + i \bar{d}_R \not{D} d_R + i \bar{L}_L \not{D} L_L + i \bar{e}_R \not{D} e_R$$

$$+ \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$$- \lambda_u \Phi \bar{U}_R Q_L - \lambda_d \Phi \bar{d}_R Q_L - \lambda_e \Phi \bar{e}_R L_L + h.c.$$

Algorithmic!

- Insert vevs **Algorithmic!**
- Expand Lagrangian **Algorithmic!**
- Collect quadratic terms **Algorithmic!**
- Diagonalize mass matrices **Algorithmic!**
- Rotate fields to mass basis **Algorithmic!**
- Calculate Feynman diagrams **Algorithmic!**
- Implement Feynman rules into CH, FA, MG, SH, WD **Algorithmic!**
- Implement Lagrangian into FR **Algorithmic!**
- Do calculations **Some algorithmic!**

Introducing

Galileo

Do more!

I	G	F	Config
	U(1)		+G
e_L	-1		
e_R	-1		
+F			

Lagrangian

$$\begin{aligned}
 &-\frac{1}{4} A_{\mu\nu} A^{\mu\nu} + i\bar{e}_L \gamma_\mu D^\mu e_L + \\
 &i\bar{e}_R \gamma_\mu D^\mu e_R \\
 &m_0 \bar{e}_R e_L + \\
 &m_0^* \bar{e}_L e_R
 \end{aligned}$$

U(1)

Galileo

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Google

I G F Config

	SU(3)	SU(2)	U(1)	+G
Q_L	3	2	$\frac{1}{6}$	
u_R	3	1	$\frac{2}{3}$	
d_R	3	1	$-\frac{1}{3}$	
L_L	1	2	$-\frac{1}{2}$	
e_R	1	1	-1	
Φ	1	2	$\frac{1}{2}$	
+F				

Lagrangian

$$-\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + \theta_0 G_{\mu\nu} \tilde{G}^{\mu\nu} - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} + \theta_1 W_{\mu\nu} \tilde{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i \bar{Q}_L \gamma_\mu D^\mu Q_L + i \bar{u}_R \gamma_\mu D^\mu u_R + i \bar{d}_R \gamma_\mu D^\mu d_R + i \bar{L}_L \gamma_\mu D^\mu L_L + i \bar{e}_R \gamma_\mu D^\mu e_R + D_\mu \Phi D^\mu \Phi^*$$

$$\mu_{r2} \Phi \Phi^*$$

$$\lambda_{r3} \Phi \Phi \Phi^* \Phi^* +$$

$$\lambda_{r4} \Phi \Phi \Phi^* \Phi^*$$

$$y_5 \Phi \bar{u}_R Q_L + y_5^* \Phi^* \bar{Q}_L u_R + y_6 \Phi^* \bar{d}_R Q_L + y_6^* \Phi \bar{Q}_L d_R + y_7 \Phi^* \bar{e}_R L_L +$$

$$y_7^* \Phi \bar{L}_L e_R$$

Galileo

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	SU(3)	SU(2)	U(1)	+G
Q_L	3	2	$\frac{1}{6}$	
u_R	3	1	$\frac{2}{3}$	
d_R	3	1	$-\frac{1}{3}$	
L_L	1	2	$-\frac{1}{2}$	
e_R	1	1	-1	
Φ	1	2	$\frac{1}{2}$	
+F				

Lagrangian

$$-\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + \theta_0 G_{\mu\nu} \tilde{G}^{\mu\nu} - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} + \theta_1 W_{\mu\nu} \tilde{W}^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i \bar{Q}_L \gamma_\mu D^\mu Q_L + i \bar{u}_R \gamma_\mu D^\mu u_R + i \bar{d}_R \gamma_\mu D^\mu d_R + i \bar{L}_L \gamma_\mu D^\mu L_L + i \bar{e}_R \gamma_\mu D^\mu e_R + D_\mu \Phi D^\mu \Phi^*$$

$$\mu_{r2} \Phi \Phi^*$$

$$\lambda_{r3} \Phi \Phi \Phi^* \Phi^* +$$

$$\lambda_{r4} \Phi \Phi \Phi^* \Phi^*$$

$$y_5 \Phi \bar{u}_R Q_L + y_5^* \Phi^* \bar{Q}_L u_R + y_6 \Phi^* \bar{d}_R Q_L + y_6^* \Phi \bar{Q}_L d_R + y_7 \Phi^* \bar{e}_R L_L + y_7^* \Phi \bar{L}_L e_R + y_8 \Phi \Phi \bar{L}_L^c L_L + y_8^* \Phi^* \Phi^* \bar{L}_L L_L^c + y_9 \Phi \Phi \bar{L}_L^c L_L + y_9^* \Phi^* \Phi^* \bar{L}_L L_L^c$$

Galileo

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Google

I G F Config

	SU(3)	SU(2)	U(1)	Z ₂	+G
Q _L	3	2	$\frac{1}{6}$	1	
u _R	3	1	$\frac{2}{3}$	1	
d _R	3	1	$-\frac{1}{3}$	1	
L _L	1	2	$-\frac{1}{2}$	1	
e _R	1	1	-1	1	
Φ	1	2	$\frac{1}{2}$	1	
H ₂	1	2	$\frac{1}{2}$	-1	
+F					

Lagrangian

$$-\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + \theta_0 G_{\mu\nu} \tilde{G}^{\mu\nu} + -\frac{1}{4} W_{\mu\nu} W^{\mu\nu} + \theta_1 W_{\mu\nu} \tilde{W}^{\mu\nu} + -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i \bar{Q}_L \gamma_\mu D^\mu Q_L + i \bar{u}_R \gamma_\mu D^\mu u_R + i \bar{d}_R \gamma_\mu D^\mu d_R + i \bar{L}_L \gamma_\mu D^\mu L_L + i \bar{e}_R \gamma_\mu D^\mu e_R + D_\mu \Phi D^\mu \Phi^* + D_\mu H_2 D^\mu H_2^*$$

$$\mu_{r2} \Phi \Phi^* +$$

$$\mu_{r3} H_2 H_2^*$$

$$\lambda_{r4} \Phi \Phi \Phi^* \Phi^* + \lambda_{r5} \Phi \Phi \Phi^* \Phi^* + \lambda_{r6} \Phi \Phi^* H_2 H_2^* + \lambda_{r7} \Phi \Phi^* H_2 H_2^* + \lambda_8 \Phi \Phi H_2^* H_2^* + \lambda_8^* \Phi^* \Phi^* H_2 H_2 + \lambda_9 \Phi \Phi H_2^* H_2^* + \lambda_9^* \Phi^* \Phi^* H_2 H_2 + \lambda_{r10} H_2 H_2 H_2^* H_2^* + \lambda_{r11} H_2 H_2 H_2^* H_2^*$$

$$y_{12} \Phi \bar{u}_R Q_L + y_{12}^* \Phi^* \bar{Q}_L u_R + y_{13} \Phi^* \bar{d}_R Q_L + y_{13}^* \Phi \bar{Q}_L d_R + y_{14} \Phi^* \bar{e}_R L_L +$$

$$y_{14}^* \Phi \bar{L}_L e_R$$

Galileo

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Google

	SU(3)	SU(2)	U(1)	+G
Q	3	2	$\frac{1}{6}$	
u_c	3	1	$-\frac{2}{3}$	
d_c	3	1	$\frac{1}{3}$	
L	1	2	$-\frac{1}{2}$	
e_c	1	1	1	
H_u	1	2	$\frac{1}{2}$	
H_d	1	2	$-\frac{1}{2}$	
+F				

Lagrangian

$$\begin{aligned}
& \int d^2\theta d^2\bar{\theta} Q^\dagger \exp[g_0 G + g_1 W + g_2 B] Q + \int d^2\theta d^2\bar{\theta} u_c^\dagger \exp[g_0 G + g_2 B] u_c + \int d^2\theta d^2\bar{\theta} d_c^\dagger \exp[g_0 G + g_2 B] d_c + \\
& \int d^2\theta d^2\bar{\theta} L^\dagger \exp[g_1 W + g_2 B] L + \int d^2\theta d^2\bar{\theta} e_c^\dagger \exp[g_2 B] e_c + \int d^2\theta d^2\bar{\theta} H_u^\dagger \exp[g_1 W + g_2 B] H_u + \\
& \int d^2\theta d^2\bar{\theta} H_d^\dagger \exp[g_1 W + g_2 B] H_d - \frac{1}{4} \int d^2\theta G G - \frac{1}{4} \int d^2\bar{\theta} G^\dagger G^\dagger - \frac{1}{4} \int d^2\theta W W - \frac{1}{4} \int d^2\bar{\theta} W^\dagger W^\dagger + \\
& - \frac{1}{4} \int d^2\theta B B - \frac{1}{4} \int d^2\bar{\theta} B^\dagger B^\dagger \\
& \mu_0 \int d^2\bar{\theta} H_u^\dagger L^\dagger + \mu_0^* \int d^2\theta L H_u + \mu_1 \int d^2\bar{\theta} H_d^\dagger H_u^\dagger + \\
& \mu_1^* \int d^2\theta H_u H_d \\
& y_2 \int d^2\bar{\theta} H_u^\dagger u_c^\dagger Q^\dagger + y_2^* \int d^2\theta Q u_c H_u + y_3 \int d^2\bar{\theta} L^\dagger d_c^\dagger Q^\dagger + y_3^* \int d^2\theta Q d_c L + y_4 \int d^2\bar{\theta} H_d^\dagger d_c^\dagger Q^\dagger + y_4^* \int d^2\theta Q d_c H_d + \\
& y_5 \int d^2\bar{\theta} d_c^\dagger d_c^\dagger u_c^\dagger + y_5^* \int d^2\theta u_c d_c d_c + y_6 \int d^2\bar{\theta} e_c^\dagger L^\dagger L^\dagger + y_6^* \int d^2\theta L L e_c + y_7 \int d^2\bar{\theta} H_d^\dagger e_c^\dagger L^\dagger + y_7^* \int d^2\theta L e_c H_d + y_8 \int d^2\bar{\theta} H_d^\dagger H_d^\dagger e_c^\dagger \\
& + y_8^* \int d^2\theta e_c H_d H_d
\end{aligned}$$

Galileo

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Google

	SU(3)	SU(2)	U(1)	Z ₂	+G
Q	3	2	$\frac{1}{6}$	-1	
u _c	3	1	$-\frac{2}{3}$	-1	
d _c	3	1	$\frac{1}{3}$	-1	
L	1	2	$-\frac{1}{2}$	-1	
e _c	1	1	1	-1	
H _u	1	2	$\frac{1}{2}$	1	
H _d	1	2	$-\frac{1}{2}$	1	
+F					

Lagrangian

$$\begin{aligned}
& \int d^2\theta d^2\bar{\theta} Q^\dagger \exp[g_0 G + g_1 W + g_2 B] Q + \int d^2\theta d^2\bar{\theta} u_c^\dagger \exp[g_0 G + g_2 B] u_c + \int d^2\theta d^2\bar{\theta} d_c^\dagger \exp[g_0 G + g_2 B] d_c + \\
& \int d^2\theta d^2\bar{\theta} L^\dagger \exp[g_1 W + g_2 B] L + \int d^2\theta d^2\bar{\theta} e_c^\dagger \exp[g_2 B] e_c + \int d^2\theta d^2\bar{\theta} H_u^\dagger \exp[g_1 W + g_2 B] H_u + \\
& \int d^2\theta d^2\bar{\theta} H_d^\dagger \exp[g_1 W + g_2 B] H_d - \frac{1}{4} \int d^2\theta G G - \frac{1}{4} \int d^2\bar{\theta} G^\dagger G^\dagger - \frac{1}{4} \int d^2\theta W W - \frac{1}{4} \int d^2\bar{\theta} W^\dagger W^\dagger + \\
& - \frac{1}{4} \int d^2\theta B B - \frac{1}{4} \int d^2\bar{\theta} B^\dagger B^\dagger \\
& \mu_0 \int d^2\bar{\theta} H_d^\dagger H_u^\dagger + \\
& \mu_0^* \int d^2\theta H_u H_d \\
& y_1 \int d^2\bar{\theta} H_u^\dagger u_c^\dagger Q^\dagger + y_1^* \int d^2\theta Q u_c H_u + y_2 \int d^2\bar{\theta} H_d^\dagger d_c^\dagger Q^\dagger + y_2^* \int d^2\theta Q d_c H_d + y_3 \int d^2\bar{\theta} H_d^\dagger e_c^\dagger L^\dagger + \\
& y_3^* \int d^2\theta L e_c H_d
\end{aligned}$$

Dash home

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Google

	SU(3)	SU(2)	U(1)	Z ₂	Z ₃	+G
Q	3	2	$\frac{1}{6}$	-1	$e^{\frac{4\pi i}{3}}$	
u _c	3	1	$\frac{2}{3}$	-1	$e^{\frac{4\pi i}{3}}$	
d _c	3	1	$\frac{1}{3}$	-1	$e^{\frac{4\pi i}{3}}$	
L	1	2	$-\frac{1}{2}$	-1	$e^{\frac{4\pi i}{3}}$	
e _c	1	1	1	-1	$e^{\frac{4\pi i}{3}}$	
H _u	1	2	$\frac{1}{2}$	1	$e^{\frac{4\pi i}{3}}$	
H _d	1	2	$-\frac{1}{2}$	1	$e^{\frac{4\pi i}{3}}$	
S	1	1	0	1	$e^{\frac{4\pi i}{3}}$	
+F						

Lagrangian

$$\begin{aligned}
& \int d^2\theta d^2\bar{\theta} Q^\dagger \exp[g_0 G + g_1 W + g_2 B_3] Q + \int d^2\theta d^2\bar{\theta} u_c^\dagger \exp[g_0 G + g_2 B_3] u_c + \int d^2\theta d^2\bar{\theta} d_c^\dagger \exp[g_0 G + g_2 B_3] d_c + \\
& \int d^2\theta d^2\bar{\theta} L^\dagger \exp[g_1 W + g_2 B_3] L + \int d^2\theta d^2\bar{\theta} e_c^\dagger \exp[g_2 B_3] e_c + \int d^2\theta d^2\bar{\theta} H_u^\dagger \exp[g_1 W + g_2 B_3] H_u + \\
& \int d^2\theta d^2\bar{\theta} H_d^\dagger \exp[g_1 W + g_2 B_3] H_d + \int d^2\theta d^2\bar{\theta} S^\dagger \exp[g_2 B_3] S - \frac{1}{4} \int d^2\theta G G - \frac{1}{4} \int d^2\bar{\theta} G^\dagger G^\dagger - \frac{1}{4} \int d^2\theta W W - \frac{1}{4} \int d^2\bar{\theta} W^\dagger W^\dagger + \\
& -\frac{1}{4} \int d^2\theta B_3 B_3 - \frac{1}{4} \int d^2\bar{\theta} B_3^\dagger B_3^\dagger \\
& y_0 \int d^2\bar{\theta} H_u^\dagger u_c^\dagger Q^\dagger + y_0^* \int d^2\theta Q u_c H_u + y_1 \int d^2\bar{\theta} H_d^\dagger d_c^\dagger Q^\dagger + y_1^* \int d^2\theta Q d_c H_d + y_2 \int d^2\bar{\theta} H_d^\dagger e_c^\dagger L^\dagger + y_2^* \int d^2\theta L e_c H_d + \\
& y_3 \int d^2\bar{\theta} S^\dagger H_d^\dagger H_u^\dagger + y_3^* \int d^2\theta H_u H_d S + y_4 \int d^2\bar{\theta} S^\dagger S^\dagger S^\dagger + y_4^* \int d^2\theta S S S
\end{aligned}$$

Dash home

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Google

	SU(3)	SU(2)	SU(2)	U(1)	+G
Q_{L0}	3	2	1	$\frac{1}{6}$	
Q_{L1}	3	1	2	$\frac{1}{6}$	
Q_{R1}	3	1	2	$\frac{1}{6}$	
u_{R2}	3	1	1	$\frac{2}{3}$	
d_{R2}	3	1	1	$-\frac{1}{3}$	
L_{L0}	1	2	1	$-\frac{1}{2}$	
L_{L1}	1	1	2	$-\frac{1}{2}$	
L_{R1}	1	1	2	$-\frac{1}{2}$	
e_{R2}	1	1	1	-1	
Φ_{01}	1	2	2	0	
Φ_{12}	1	1	2	$\frac{1}{2}$	
+F					

Lagrangian

$$-\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + \theta_0 G_{\mu\nu} \tilde{G}^{\mu\nu} + -\frac{1}{4} W_{0\mu\nu} W_0^{\mu\nu} + \theta_1 W_{0\mu\nu} \tilde{W}_0^{\mu\nu} + -\frac{1}{4} W_{1\mu\nu} W_1^{\mu\nu} + \theta_2 W_{1\mu\nu} \tilde{W}_1^{\mu\nu} + -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i \bar{Q}_{L0} \gamma_\mu D^\mu Q_{L0} +$$

$$i \bar{Q}_{L1} \gamma_\mu D^\mu Q_{L1} + i \bar{Q}_{R1} \gamma_\mu D^\mu Q_{R1} + i \bar{u}_{R2} \gamma_\mu D^\mu u_{R2} + i \bar{d}_{R2} \gamma_\mu D^\mu d_{R2} + i \bar{L}_{L0} \gamma_\mu D^\mu L_{L0} + i \bar{L}_{L1} \gamma_\mu D^\mu L_{L1} + i \bar{L}_{R1} \gamma_\mu D^\mu L_{R1} +$$

$$i \bar{e}_{R2} \gamma_\mu D^\mu e_{R2} + D_\mu \Phi_{01} D^\mu \Phi_{01}^* + D_\mu \Phi_{01} D^\mu \Phi_{01}^* + D_\mu \Phi_{01}^* D^\mu \Phi_{01}^* + D_\mu \Phi_{12} D^\mu \Phi_{12}^*$$

$$\mu_{r3} \Phi_{01} \Phi_{01}^* + \mu_4 \Phi_{01} \Phi_{01} + \mu_4^* \Phi_{01}^* \Phi_{01}^* +$$

$$\mu_{r5} \Phi_{12} \Phi_{12}^*$$

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L_{L1}	1	1	2	$\frac{-1}{2}$	
L_{R1}	1	1	2	$\frac{-1}{2}$	
e_{R2}	1	1	1	-1	
Φ_{01}	1	2	2	0	
Φ_{12}	1	1	2	$\frac{1}{2}$	
+F					

Lagrangian

$$-\frac{1}{4} G_{\mu\nu} G^{\mu\nu} + \theta_0 G_{\mu\nu} \tilde{G}^{\mu\nu} + -\frac{1}{4} W_{0\mu\nu} W_0^{\mu\nu} + \theta_1 W_{0\mu\nu} \tilde{W}_0^{\mu\nu} + -\frac{1}{4} W_{1\mu\nu} W_1^{\mu\nu} + \theta_2 W_{1\mu\nu} \tilde{W}_1^{\mu\nu} + -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} + i \overline{Q_{L0}} \gamma_\mu D^\mu Q_{L0} +$$

$$i \overline{Q_{L1}} \gamma_\mu D^\mu Q_{L1} + i \overline{Q_{R1}} \gamma_\mu D^\mu Q_{R1} + i \overline{u_{R2}} \gamma_\mu D^\mu u_{R2} + i \overline{d_{R2}} \gamma_\mu D^\mu d_{R2} + i \overline{L_{L0}} \gamma_\mu D^\mu L_{L0} + i \overline{L_{L1}} \gamma_\mu D^\mu L_{L1} + i \overline{L_{R1}} \gamma_\mu D^\mu L_{R1} +$$

$$i \overline{e_{R2}} \gamma_\mu D^\mu e_{R2} + D_\mu \Phi_{01} D^\mu \Phi_{01}^* + D_\mu \Phi_{01} D^\mu \Phi_{01} + D_\mu \Phi_{01}^* D^\mu \Phi_{01}^* + D_\mu \Phi_{12} D^\mu \Phi_{12}^*$$

$$\mu_{r3} \Phi_{01} \Phi_{01}^* + \mu_4 \Phi_{01} \Phi_{01} + \mu_4^* \Phi_{01}^* \Phi_{01}^* +$$

$$\mu_{r5} \Phi_{12} \Phi_{12}^*$$

$$\lambda_{r6} \Phi_{01} \Phi_{01} \Phi_{01}^* \Phi_{01}^* + \lambda_{r7} \Phi_{01} \Phi_{01} \Phi_{01}^* \Phi_{01}^* + \lambda_{r8} \Phi_{01} \Phi_{01} \Phi_{01}^* \Phi_{01}^* + \lambda_{r9} \Phi_{01} \Phi_{01} \Phi_{01}^* \Phi_{01}^* + \lambda_{10} \Phi_{01}^* \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{10}^* \Phi_{01} \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* +$$

$$\lambda_{11} \Phi_{01}^* \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{11}^* \Phi_{01} \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* + \lambda_{12} \Phi_{01}^* \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{12}^* \Phi_{01} \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* + \lambda_{13} \Phi_{01}^* \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{13}^* \Phi_{01} \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* +$$

$$\lambda_{r14} \Phi_{01} \Phi_{01}^* \Phi_{12} \Phi_{12}^* + \lambda_{r15} \Phi_{01} \Phi_{01}^* \Phi_{12} \Phi_{12}^* + \lambda_{16} \Phi_{01} \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{16}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* + \lambda_{17} \Phi_{01} \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{17}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* +$$

$$\lambda_{18} \Phi_{01} \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{18}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* + \lambda_{19} \Phi_{01} \Phi_{01} \Phi_{01} \Phi_{01} + \lambda_{19}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* \Phi_{01}^* + \lambda_{20} \Phi_{01} \Phi_{01} \Phi_{12} \Phi_{12} + \lambda_{20}^* \Phi_{01}^* \Phi_{01}^* \Phi_{12} \Phi_{12}^* +$$

$$\lambda_{21} \Phi_{01} \Phi_{01} \Phi_{12} \Phi_{12} + \lambda_{21}^* \Phi_{01}^* \Phi_{01}^* \Phi_{12} \Phi_{12}^* + \lambda_{r22} \Phi_{12} \Phi_{12} \Phi_{12}^* \Phi_{12}^* + \lambda_{r23} \Phi_{12} \Phi_{12} \Phi_{12}^* \Phi_{12}^*$$

$$y_{24} \Phi_{01}^* \overline{Q_{R1}} Q_{L0} + y_{24}^* \Phi_{01} \overline{Q_{L0}} Q_{R1} + y_{25} \Phi_{01}^* \overline{Q_{R1}} Q_{L0} + y_{25}^* \Phi_{01} \overline{Q_{L0}} Q_{R1} + y_{26} \Phi_{12} \overline{u_{R2}} Q_{L1} + y_{26}^* \Phi_{12}^* \overline{Q_{L1}} u_{R2} + y_{27} \Phi_{12}^* \overline{d_{R2}} Q_{L1} + y_{27}^* \Phi_{12} \overline{Q_{L1}} d_{R2}$$

$$+ y_{28} \Phi_{01}^* \overline{L_{R1}} L_{L0} + y_{28}^* \Phi_{01} \overline{L_{L0}} L_{R1} + y_{29} \Phi_{01}^* \overline{L_{R1}} L_{L0} + y_{29}^* \Phi_{01} \overline{L_{L0}} L_{R1} + y_{30} \Phi_{12}^* \overline{e_{R2}} L_{L1} + y_{30}^* \Phi_{12} \overline{L_{L1}} e_{R2}$$

$$m_{31} \overline{Q_{R1}} Q_{L1} + m_{31}^* \overline{Q_{L1}} Q_{R1} + m_{32} \overline{L_{R1}} L_{L1} +$$

$$m_{32}^* \overline{L_{L1}} L_{R1}$$

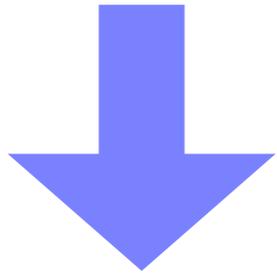
Galileo

- Core library with thin GUI wrapper
 - C++ library linkable to other codes
 - Thorough API documentation
- Any rep of any semisimple compact Lie algebra
 - Including finding singlets
 - Many, many automated tests
- Rewriting Lorentz part of core to be more general
 - Want solid foundation for later development

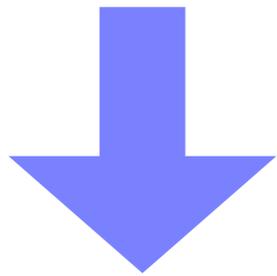
Galileo

- Under construction
 - Lorentz symmetry
 - Symmetry breaking
 - Expansion of Lagrangian
 - Save/Read
 - Output to FeynRules
 - ...

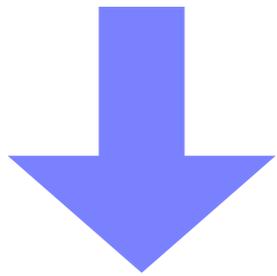
Model



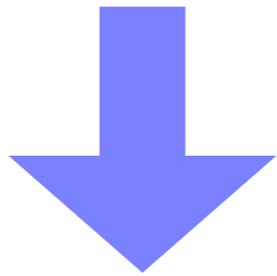
FR Model File



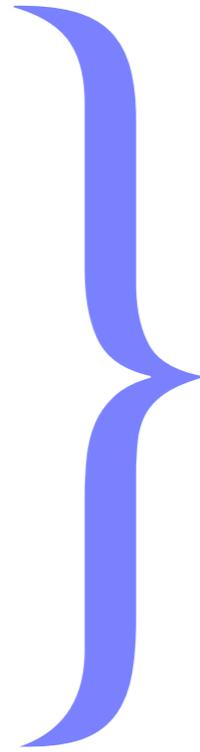
FeynRules



Validation

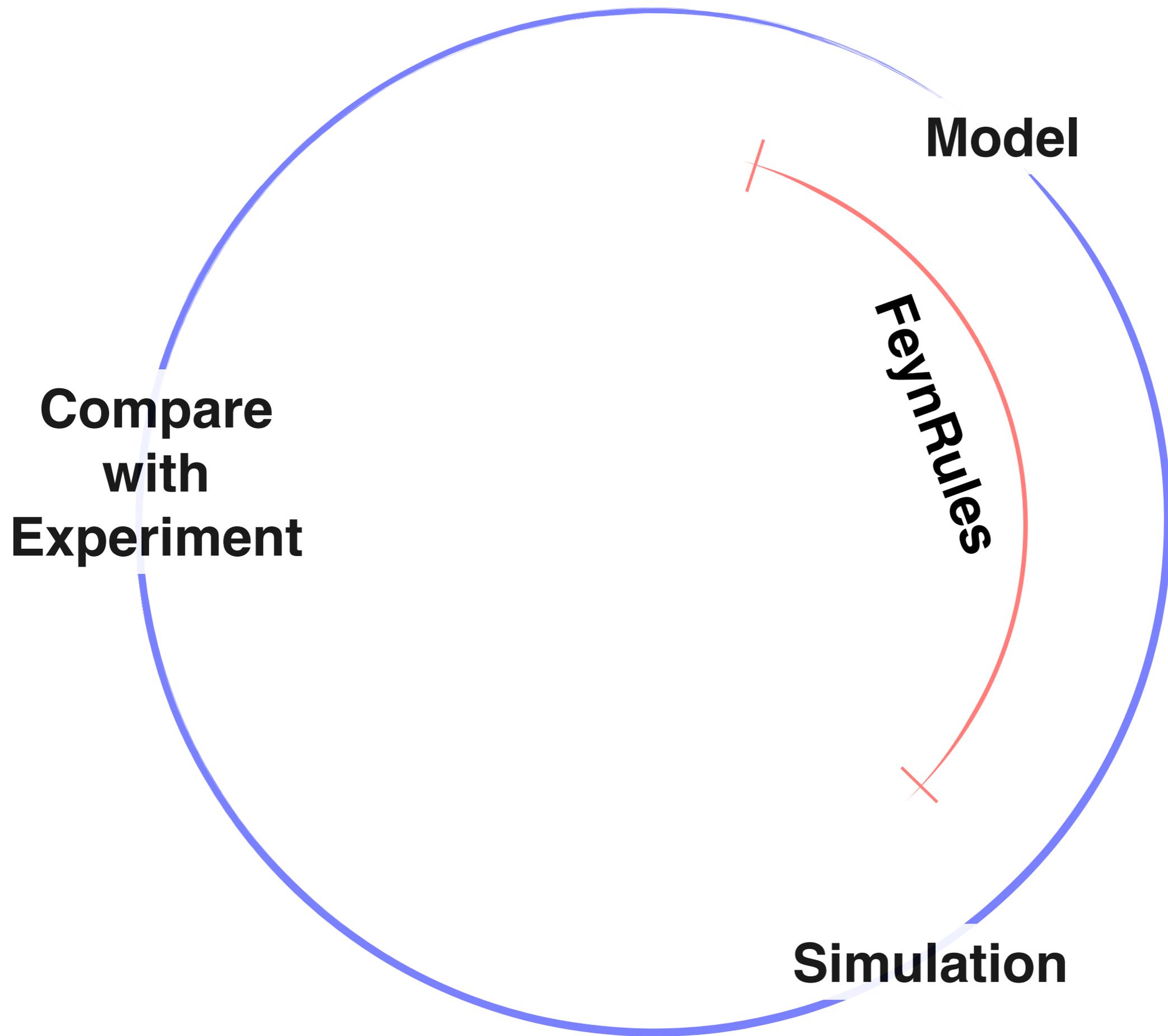


MadGraph



Galileo

- Models from symmetry
 - Christensen, Salmon, Setzer, Stefanus



Model

Feynman Rules

Simulation

**Compare
with
Experiment**