

MadGraph 5

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University of Illinois at Urbana Champaign

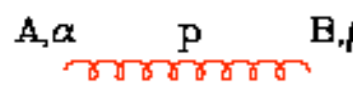
Aims for these lectures

- Get you **acquainted** with the concepts and techniques used in event generation
- Give you hands-on experience with matrix element generation, event generation and analysis
- **Answer as many of your questions as I can (so please ask questions!)**

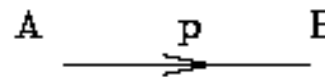
Topic of this lecture

- How to compute the matrix element
→ HELAS / ALOHA
- Features of MG5
- Life demonstration
- MadSpin ?

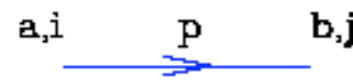
The Matrix Element



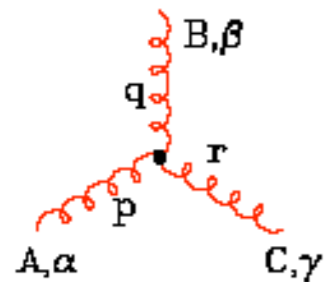
$$\delta^{AB} \left[-g^{\alpha\beta} + (1-\lambda) \frac{p^\alpha p^\beta}{p^2 + i\epsilon} \right] \frac{i}{p^2 + i\epsilon}$$



$$\delta^{AB} \frac{i}{(p^2 + i\epsilon)}$$

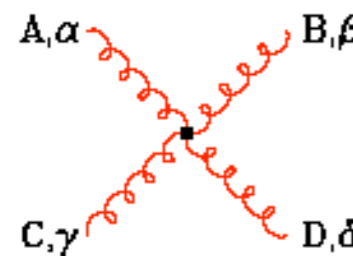


$$\delta^{ab} \frac{i}{(\not{p} - m + i\epsilon)_{ij}}$$

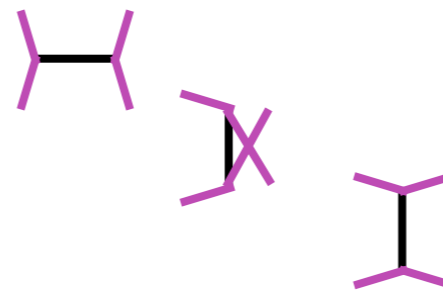


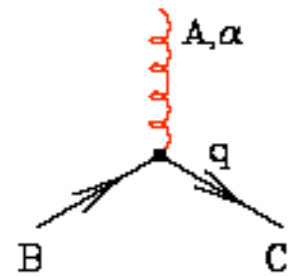
$$-g f^{ABC} [(p-q)^\gamma g^{\alpha\beta} + (q-r)^\alpha g^{\beta\gamma} + (r-p)^\beta g^{\gamma\alpha}]$$

(all momenta incoming)

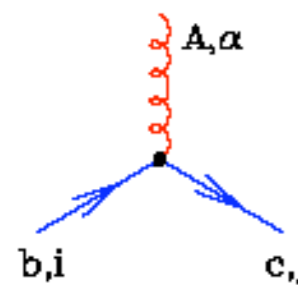


$$\begin{aligned} & -ig^2 f^{XAC} f^{XBD} [g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\delta} g^{\beta\gamma}] \\ & -ig^2 f^{XAD} f^{XBC} [g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\gamma} g^{\beta\delta}] \\ & -ig^2 f^{XAB} f^{XCD} [g^{\alpha\gamma} g^{\beta\delta} - g^{\alpha\delta} g^{\beta\gamma}] \end{aligned}$$



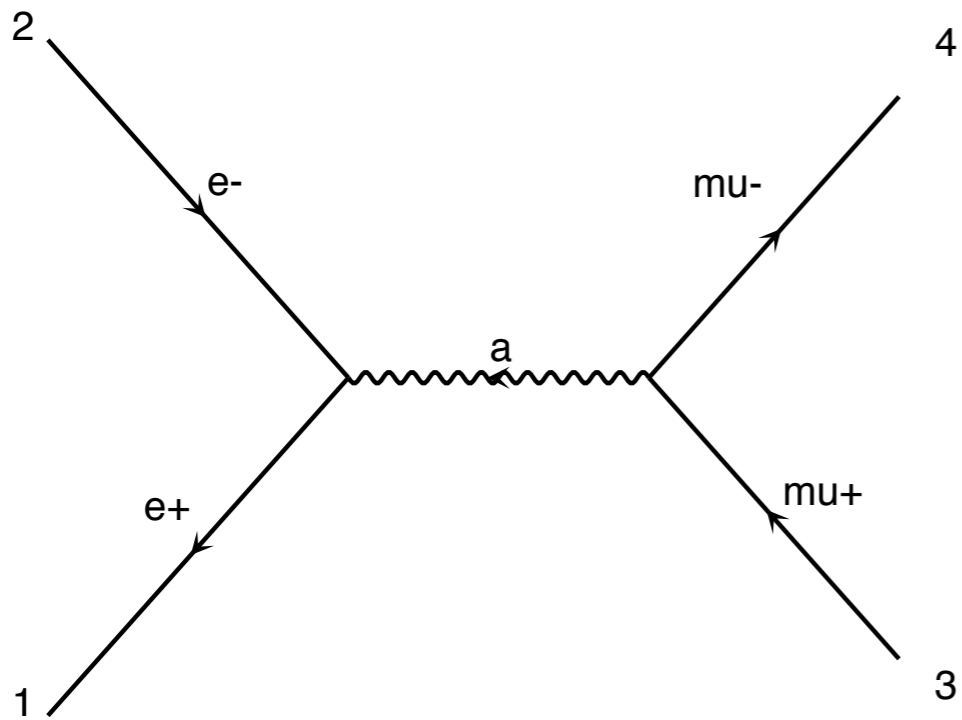


$$g f^{ABC} q^\alpha$$

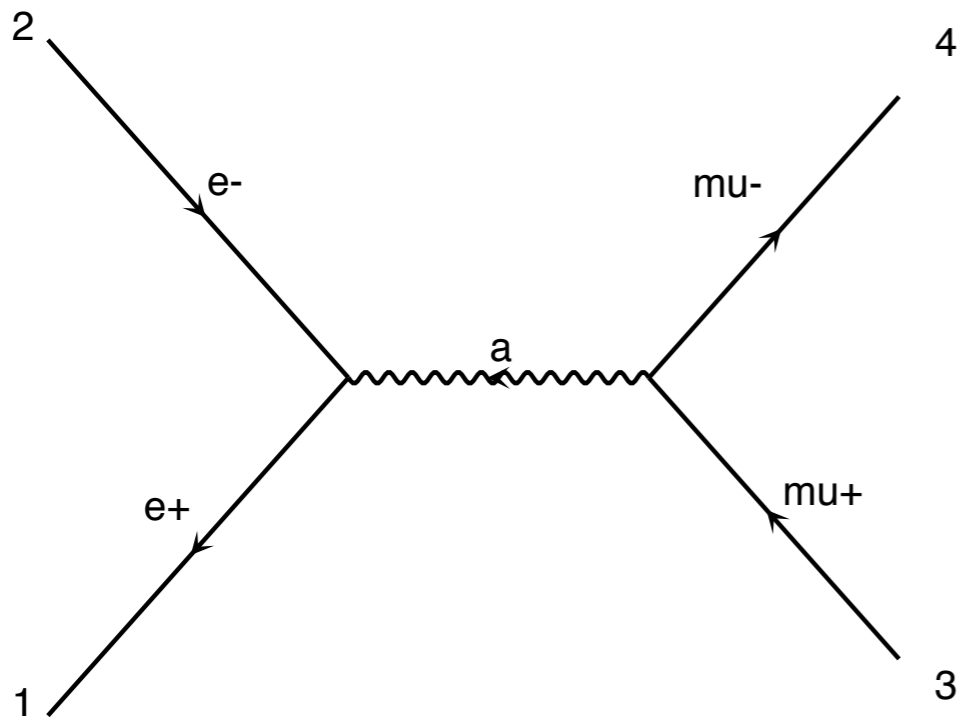


$$-ig (t^A)_{cb} (\gamma^\alpha)_{ij}$$

Evaluate a square Matrix Element

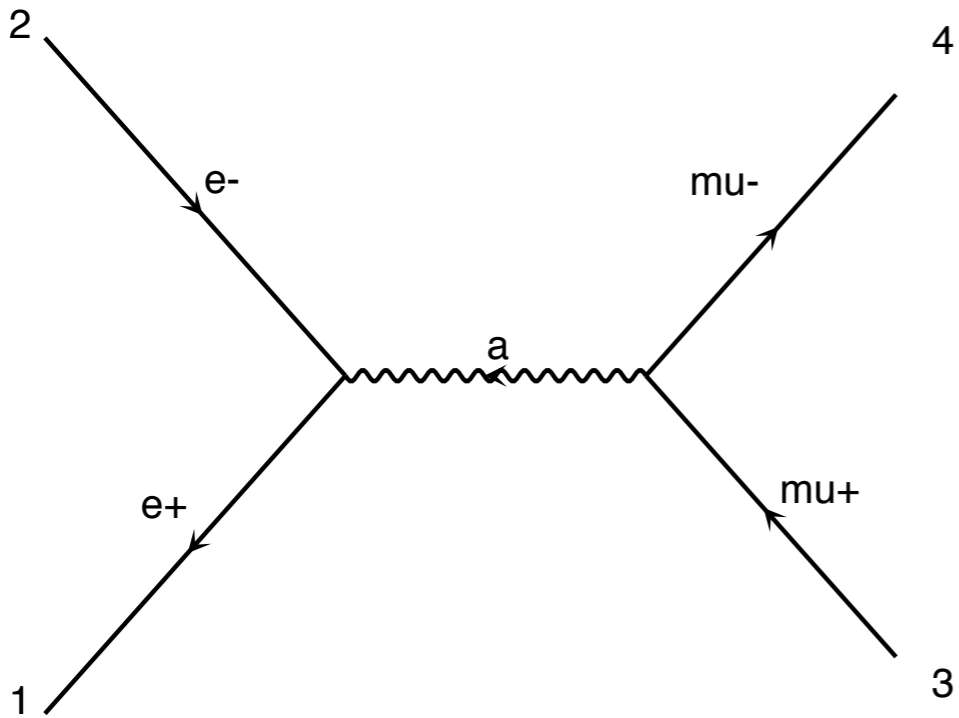


Evaluate a square Matrix Element



$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

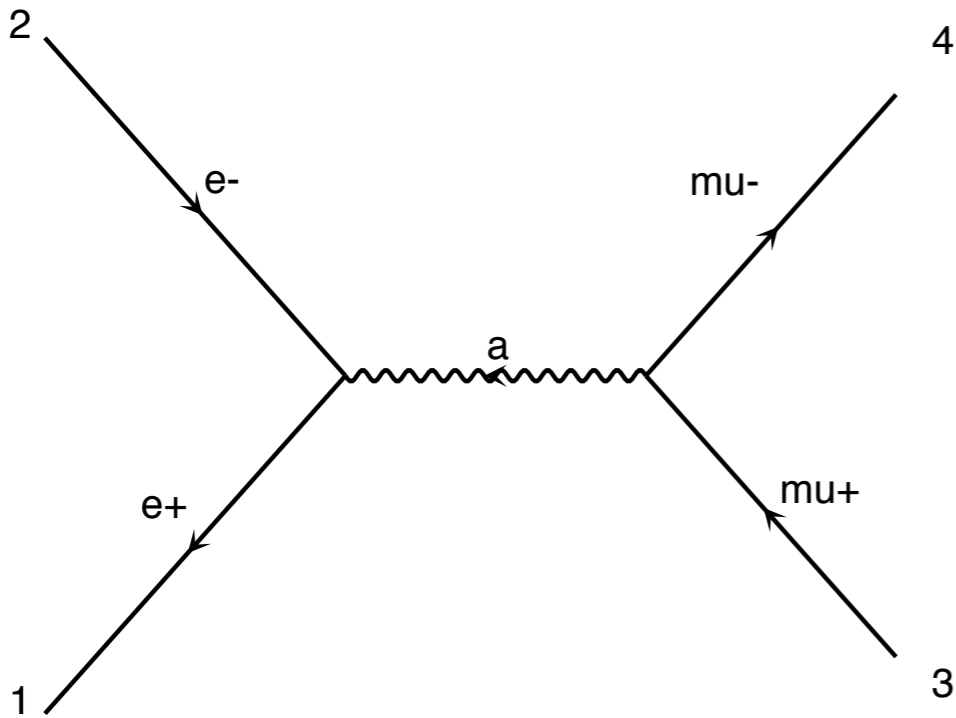
Evaluate a square Matrix Element



$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

Evaluate a square Matrix Element

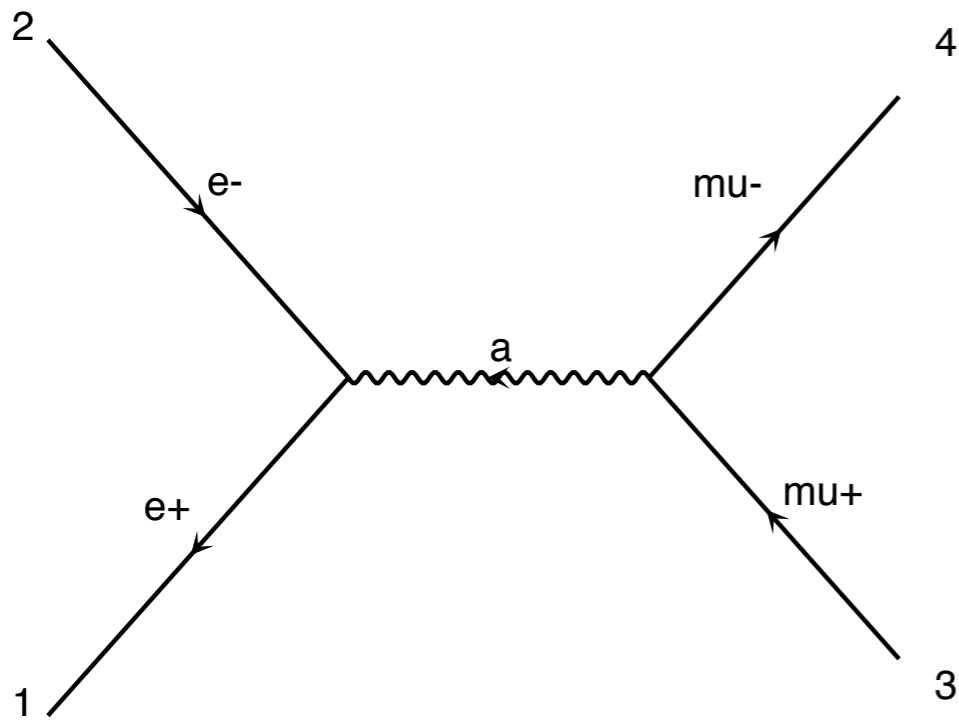


$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

$$\sum_{pol} \bar{u} u = \not{p} + m$$

Evaluate a square Matrix Element



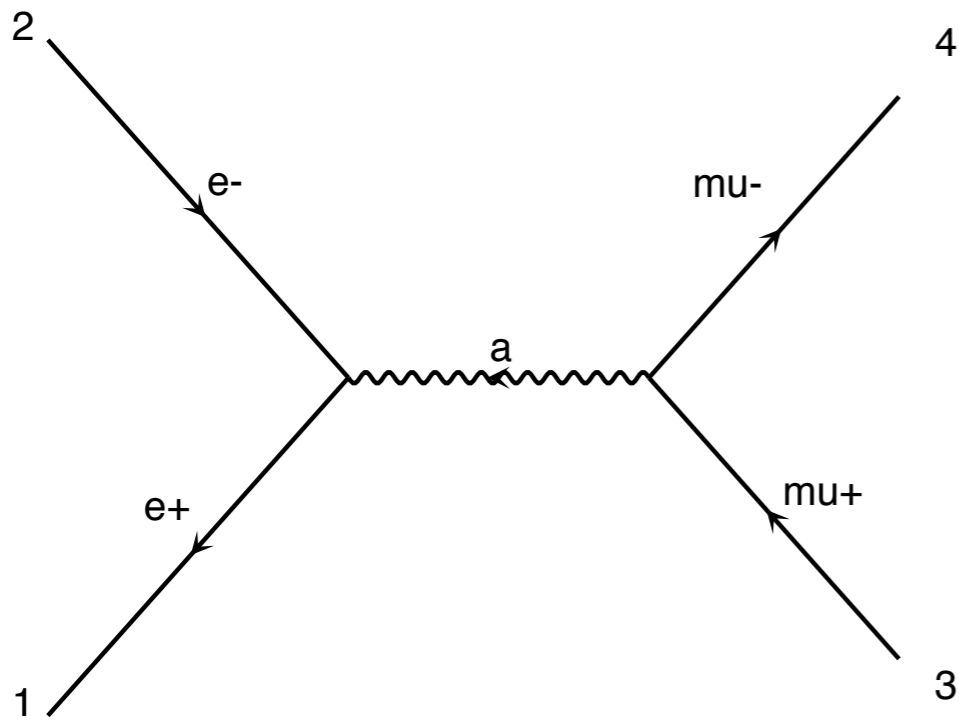
$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

$$\sum_{pol} \bar{u} u = \not{p} + m$$

$$\rightarrow \frac{e^4}{4q^4} \text{Tr}[\not{p}_1 \gamma^\mu \not{p}_2 \gamma^\nu] \text{Tr}[\not{p}_3 \gamma_\mu \not{p}_4 \gamma_\nu]$$

Evaluate a square Matrix Element



$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

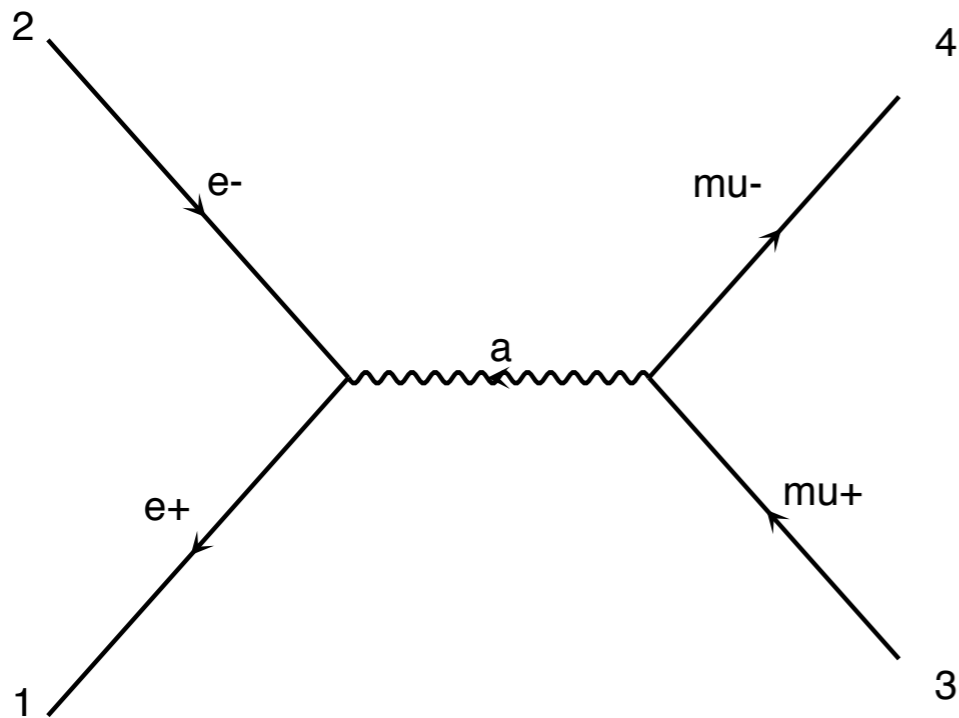
$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

$$\sum_{pol} \bar{u} u = \not{p} + m$$

$$\rightarrow \frac{e^4}{4q^4} \text{Tr}[\not{p}_1 \gamma^\mu \not{p}_2 \gamma^\nu] \text{Tr}[\not{p}_3 \gamma_\mu \not{p}_4 \gamma_\nu]$$

Very Efficient !!!

Evaluate a square Matrix Element



$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

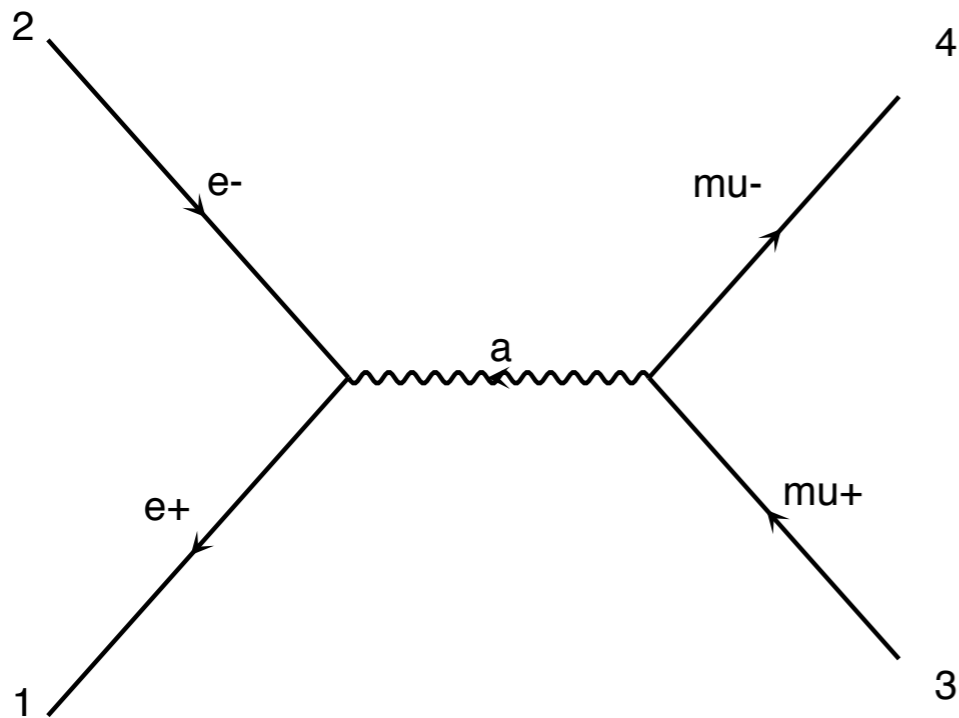
$$\sum_{pol} \bar{u} u = \not{p} + m$$

$$\rightarrow \frac{e^4}{4q^4} \text{Tr}[\not{p}_1 \gamma^\mu \not{p}_2 \gamma^\nu] \text{Tr}[\not{p}_3 \gamma_\mu \not{p}_4 \gamma_\nu]$$

Very Efficient !!!

But The number of term raises as N^2

Evaluate a square Matrix Element



$$\mathcal{M} = e^2 (\bar{u} \gamma^\mu v) \frac{g_{\mu\nu}}{q^2} (\bar{u} \gamma^\nu v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

$$\sum_{pol} \bar{u} u = \not{p} + m$$

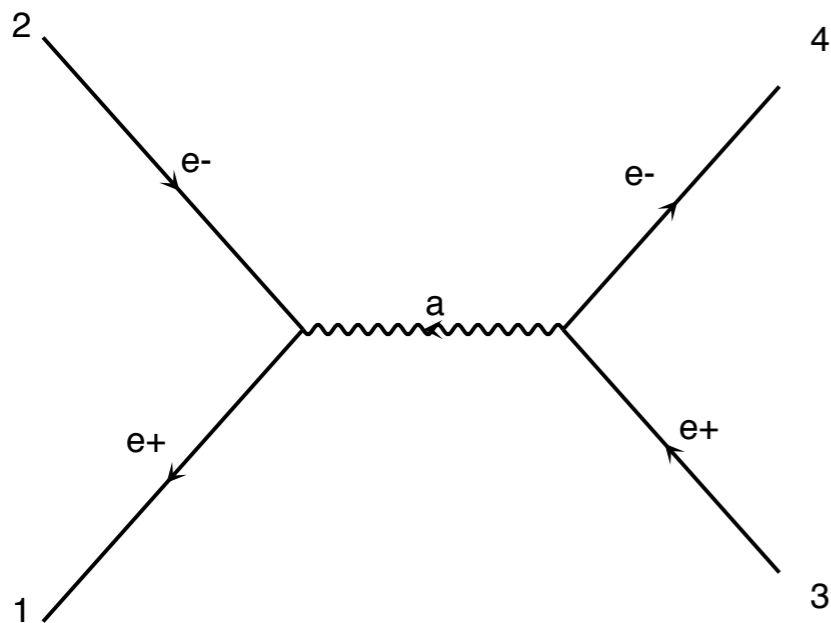
$$\rightarrow \frac{e^4}{4q^4} \text{Tr}[\not{p}_1 \gamma^\mu \not{p}_2 \gamma^\nu] \text{Tr}[\not{p}_3 \gamma_\mu \not{p}_4 \gamma_\nu]$$

Very Efficient !!!

But The number of term raises as N^2

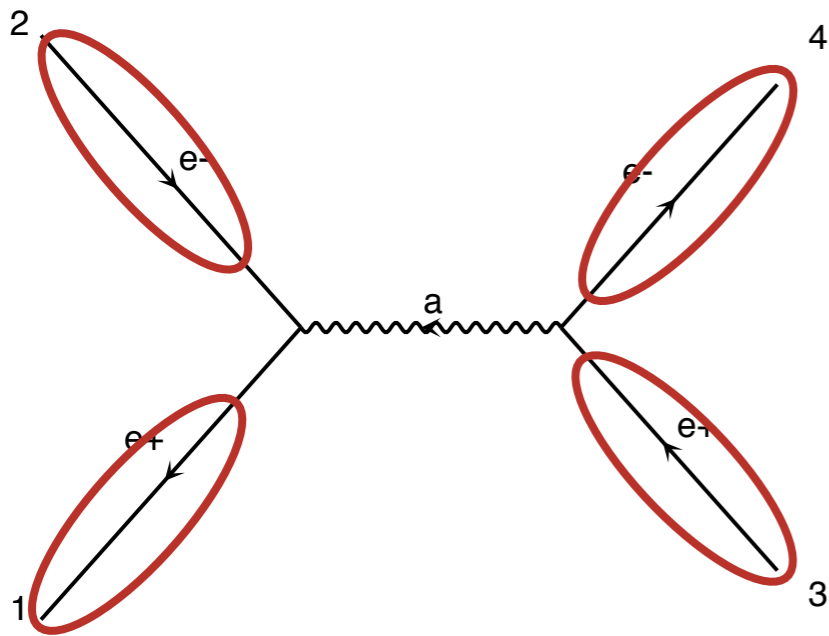
Only for $2 > 2$ and $2 > 3$

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results



$$\mathcal{M} = \bar{u}\gamma^\mu v P_{\mu\nu} \bar{u}\gamma^\nu v$$

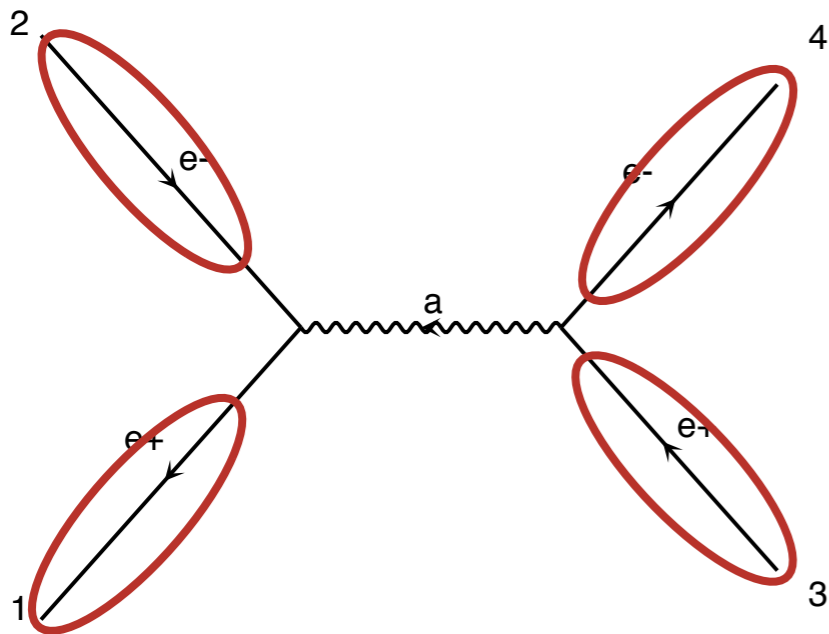
- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
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$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results

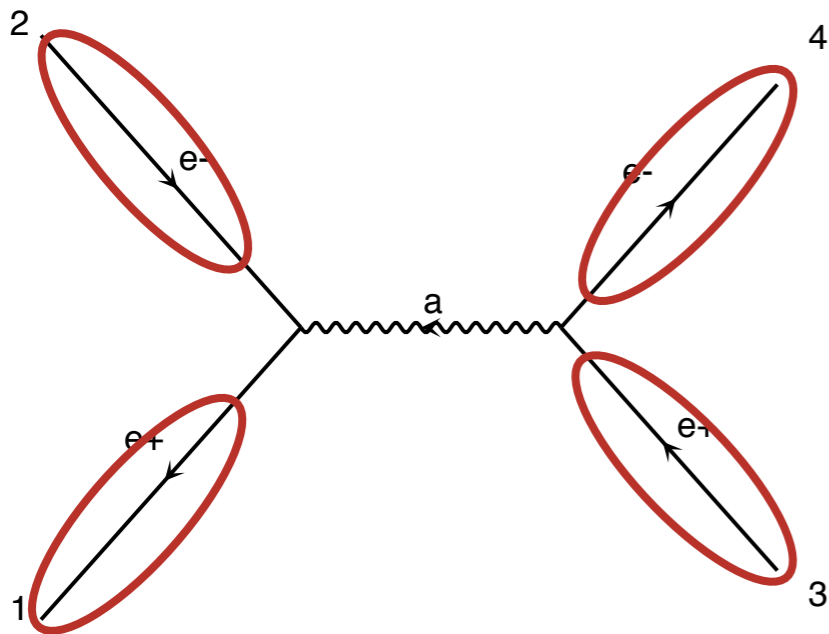


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta

```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
```


- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results



$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

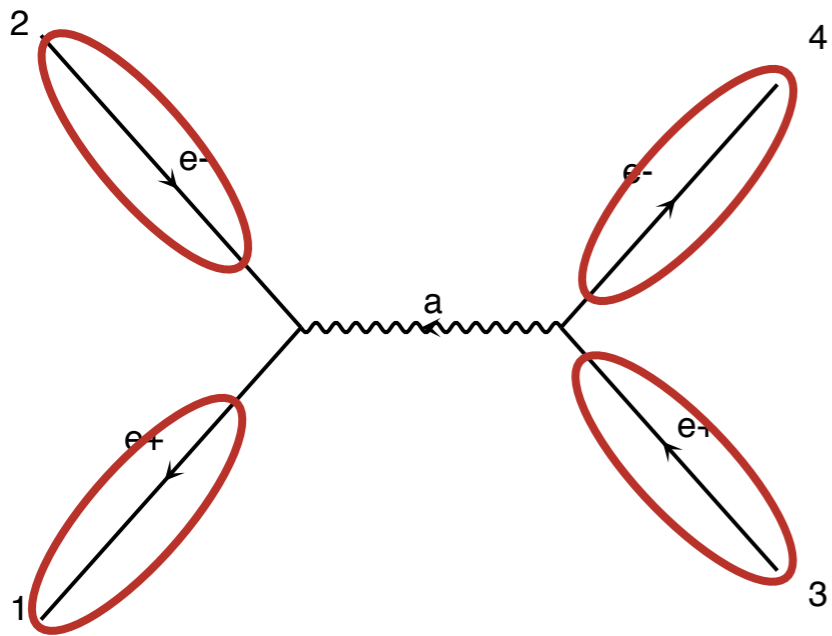
Numbers for given helicity and momenta

`CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1))`

Input: momenta, mass, helicity

Output: Wavefunction (given by an analytical formula)

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with $\mathcal{M}^* \rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results

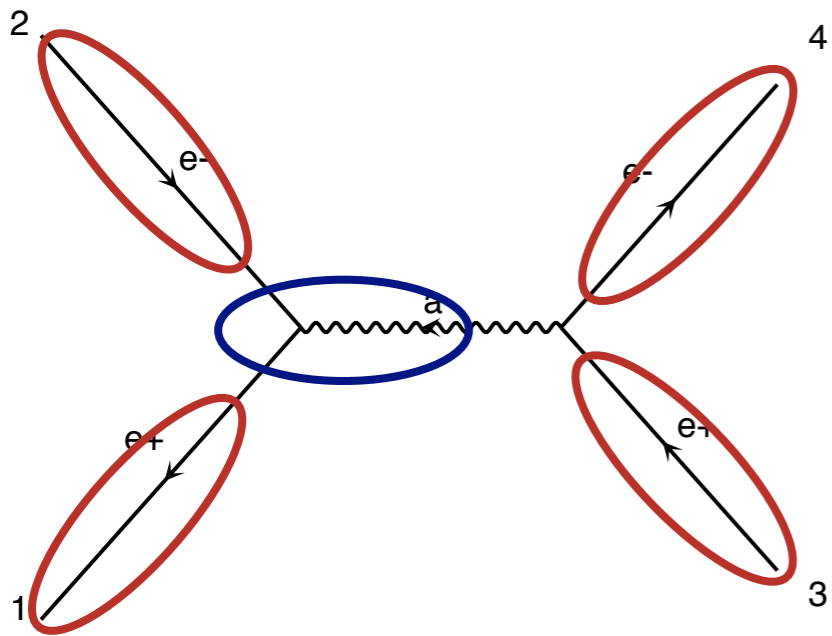


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta

```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
```

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results

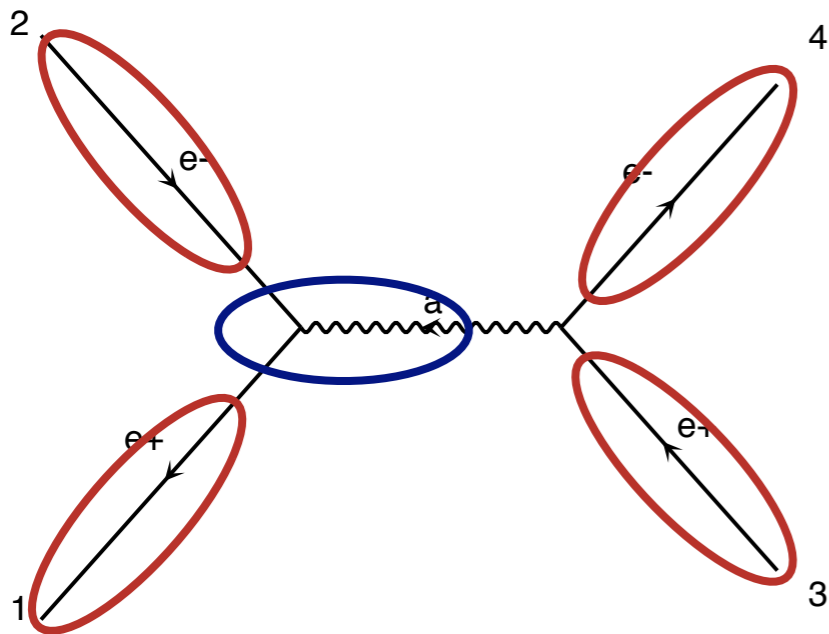


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
Calculate propagator wavefunctions

```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
CALL JIOXXX (W (1 , 2) , W (1 , 1) , GAL , ZERO , ZERO , W (1 , 5) )
```

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results



$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
Calculate propagator wavefunctions

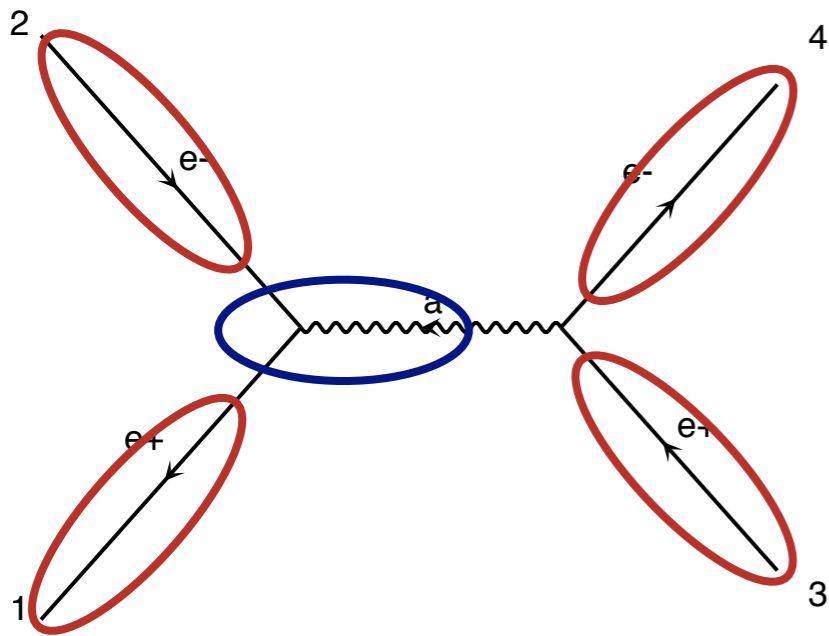
```
CALL OXXXXX (P (0, 1), ZERO, NHEL (1), -1*IC (1), W (1, 1))
CALL IXXXXX (P (0, 2), ZERO, NHEL (2), +1*IC (2), W (1, 2))
```

Input: Wavefunctions, mass, width, coupling

```
CALL JIOXXX (W (1, 2), W (1, 1), GAL, ZERO, ZERO, W (1, 5))
```

Output: Wavefunction (given by an analytical formula)

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results

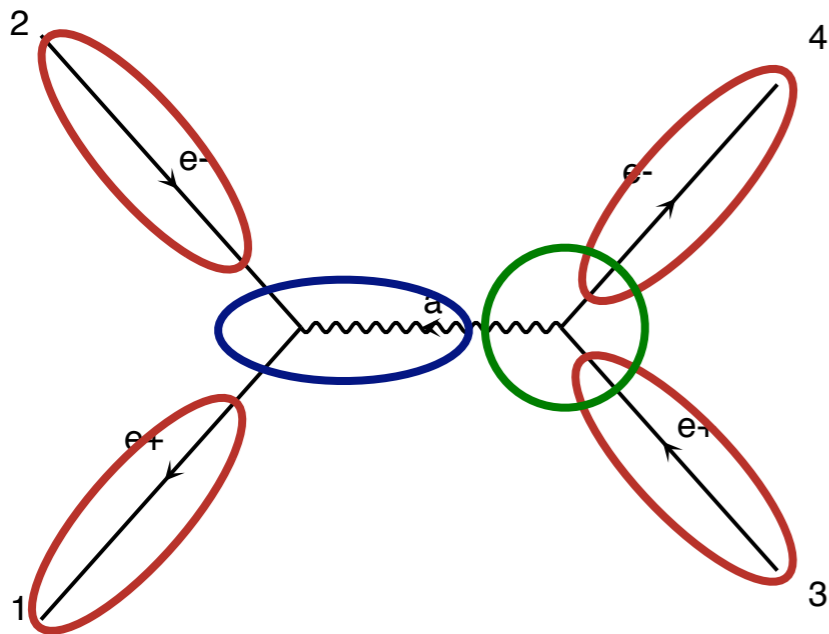


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
 Calculate propagator wavefunctions

```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
CALL JIOXXX (W (1 , 2) , W (1 , 1) , GAL , ZERO , ZERO , W (1 , 5) )
```

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
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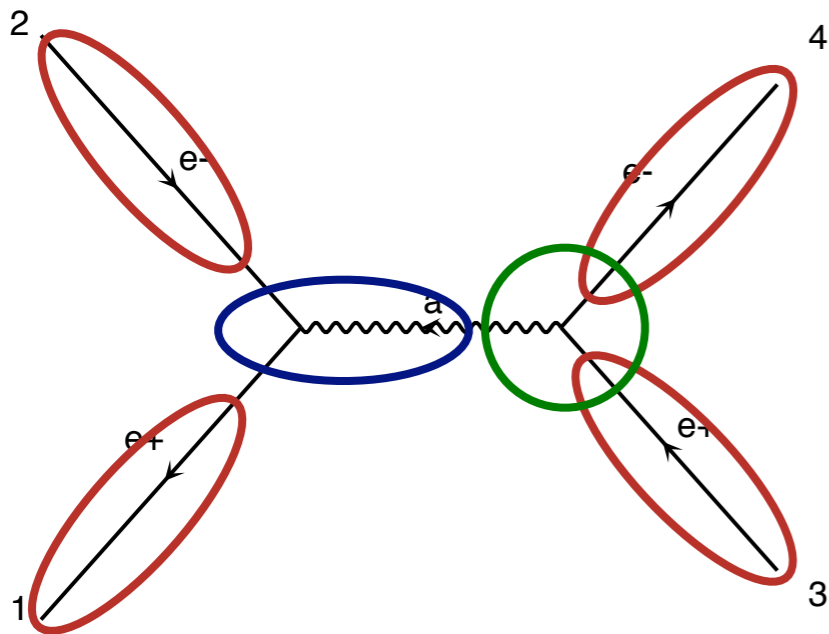


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
 Calculate propagator wavefunctions
 Finally evaluate amplitude (c-number)

```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
CALL JIOXXX (W (1 , 2) , W (1 , 1) , GAL , ZERO , ZERO , W (1 , 5) )
CALL IOVXXX (W (1 , 3) , W (1 , 4) , W (1 , 5) , GAL , AMP (1) )
```

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results



$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
 Calculate propagator wavefunctions
 Finally evaluate amplitude (c-number)

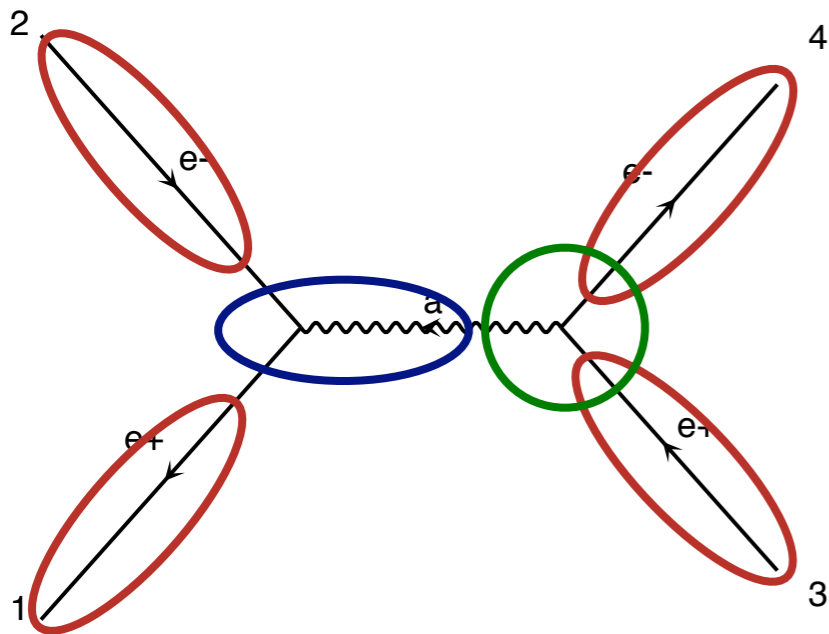
```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
```

Input: Wavefunctions, coupling

```
CALL IOVXXX (W (1 , 3) , W (1 , 4) , W (1 , 5) , GAL , AMP (1) )
```

Output: Amplitude

- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with \mathcal{M}^* $\rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results

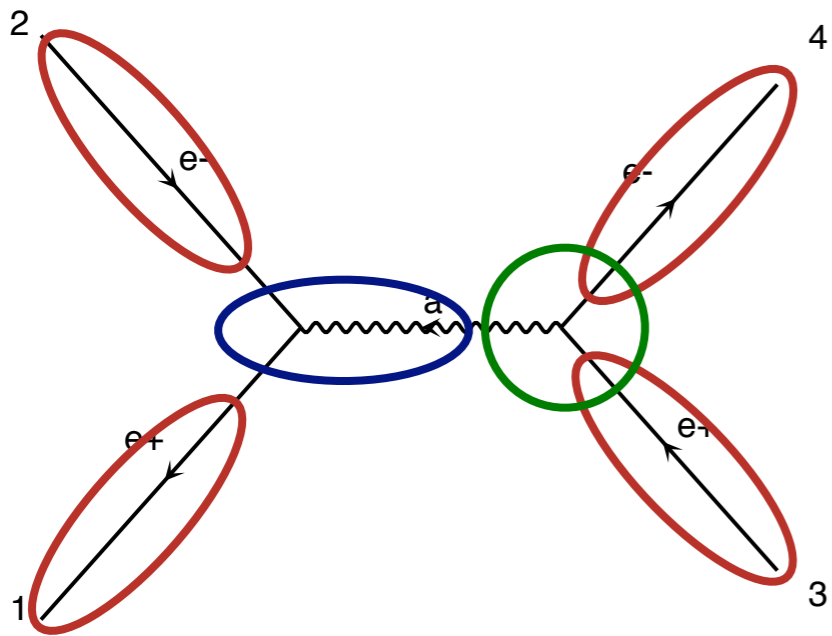


$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
 Calculate propagator wavefunctions
 Finally evaluate amplitude (c-number)

```
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CALL JIOXXX (W (1 , 2) , W (1 , 1) , GAL , ZERO , ZERO , W (1 , 5) )
CALL IOVXXX (W (1 , 3) , W (1 , 4) , W (1 , 5) , GAL , AMP (1) )
```


- Idea: Evaluate \mathcal{M} for fixed helicity of external particles
 - ➔ Multiply \mathcal{M} with $\mathcal{M}^* \rightarrow |\mathcal{M}|^2$
 - ➔ Loop on Helicity and sum the results



Helicity amplitude calls
written by MadGraph

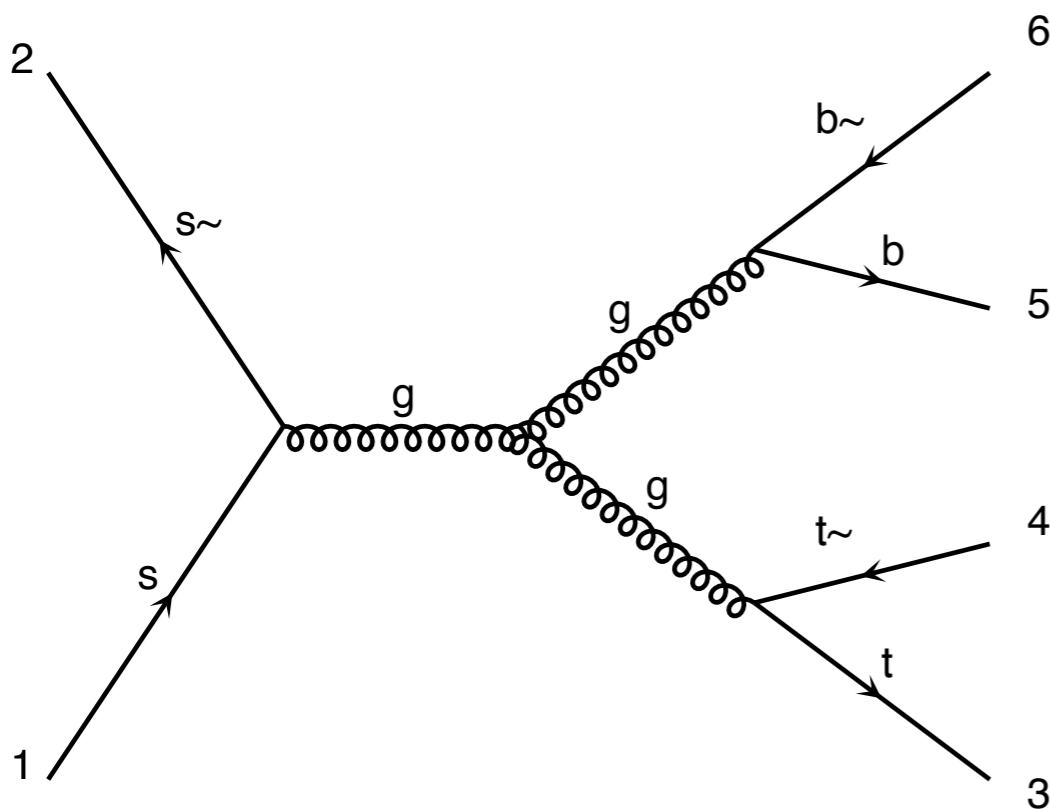
$$\mathcal{M} = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

Numbers for given helicity and momenta
Calculate propagator wavefunctions
Finally evaluate amplitude (c-number)

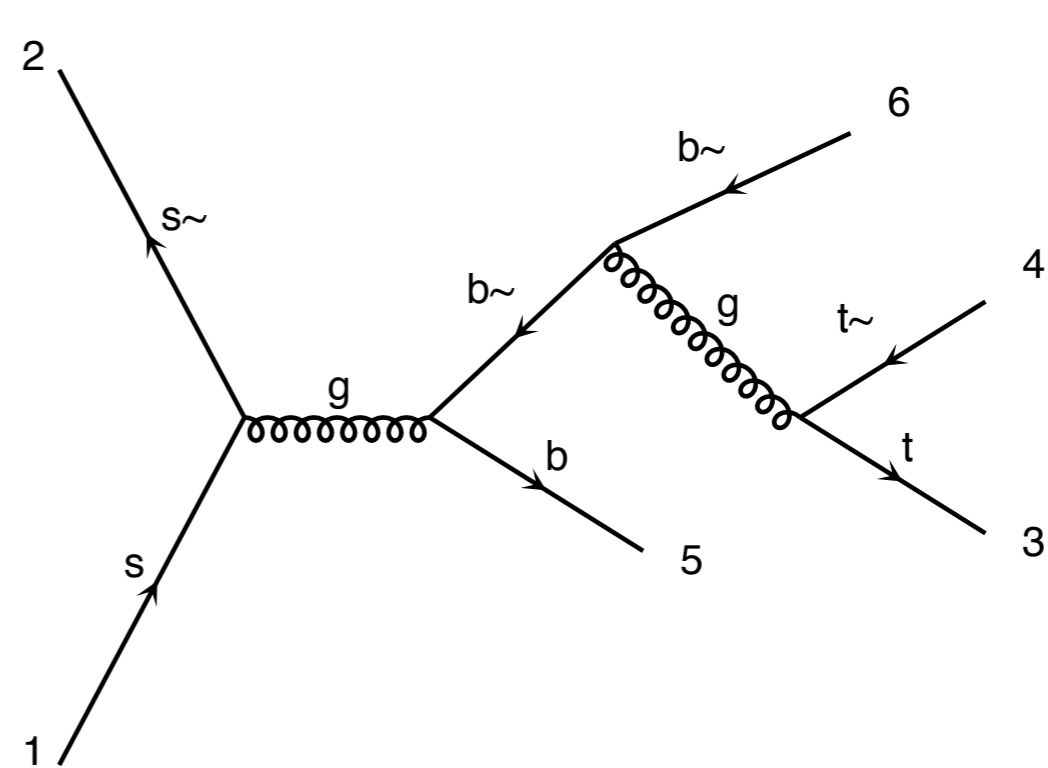
```
CALL OXXXXX (P (0 , 1) , ZERO , NHEL (1) , -1*IC (1) , W (1 , 1) )
CALL IXXXXX (P (0 , 2) , ZERO , NHEL (2) , +1*IC (2) , W (1 , 2) )
CALL IXXXXX (P (0 , 3) , ZERO , NHEL (3) , -1*IC (3) , W (1 , 3) )
CALL OXXXXX (P (0 , 4) , ZERO , NHEL (4) , +1*IC (4) , W (1 , 4) )
CALL JIOXXX (W (1 , 2) , W (1 , 1) , GAL , ZERO , ZERO , W (1 , 5) )
CALL IOVXXX (W (1 , 3) , W (1 , 4) , W (1 , 5) , GAL , AMP (1) )
```

Real case

 Known



Number of routines: 0

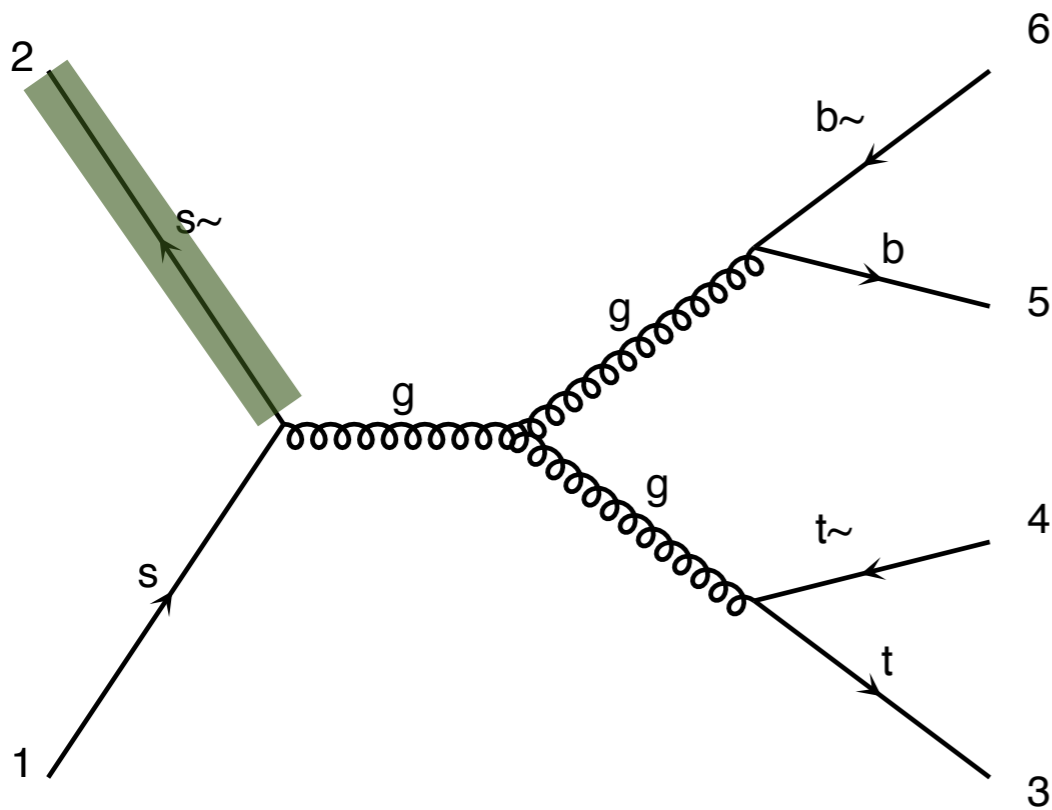


Number of routines: 0

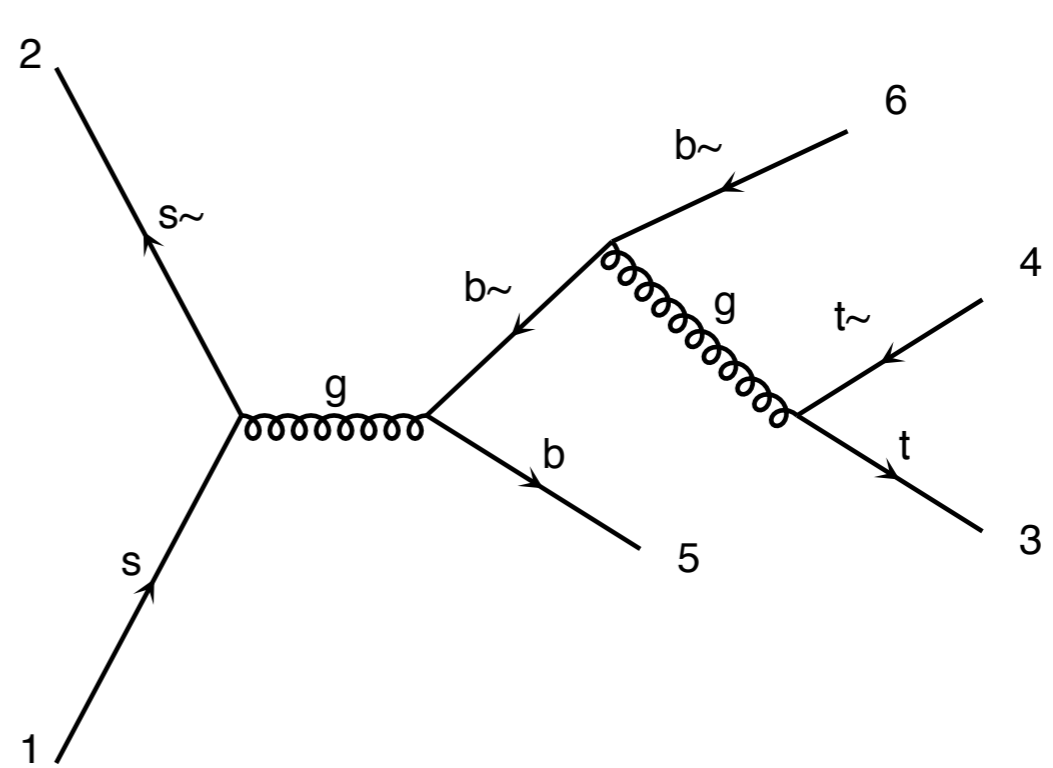
Number of routines for both: 0

Real case

 Known



Number of routines: 1



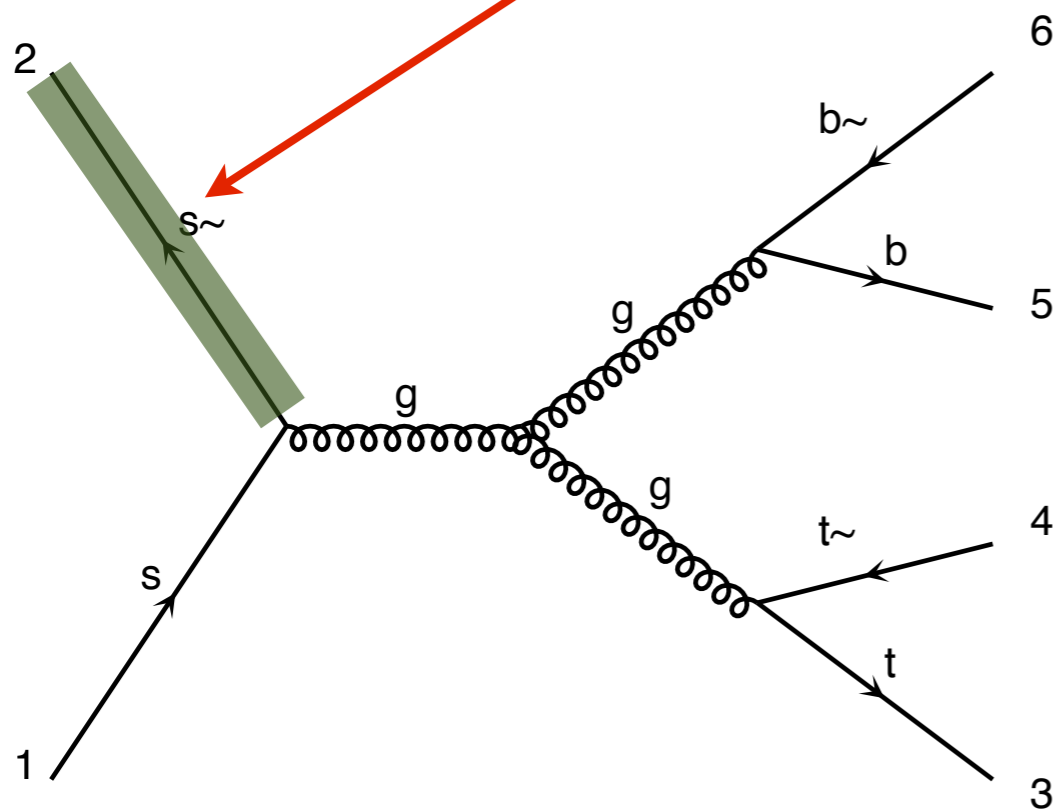
Number of routines: 0

Number of routines for both: 1

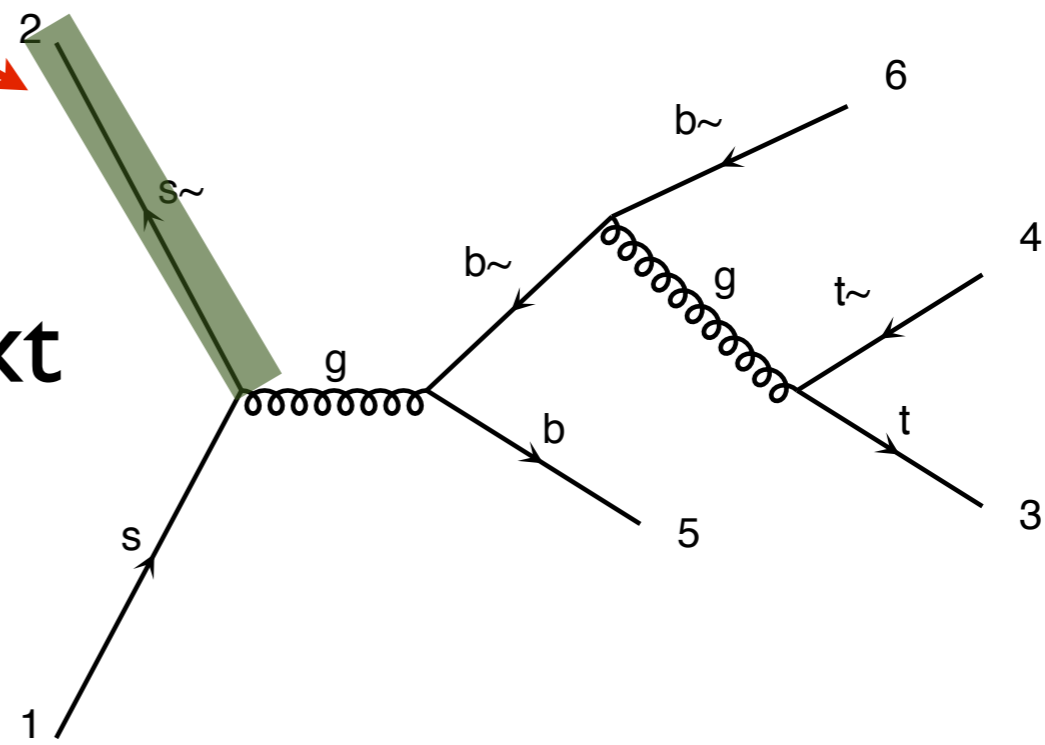
Real case

 Known

Identical



Text

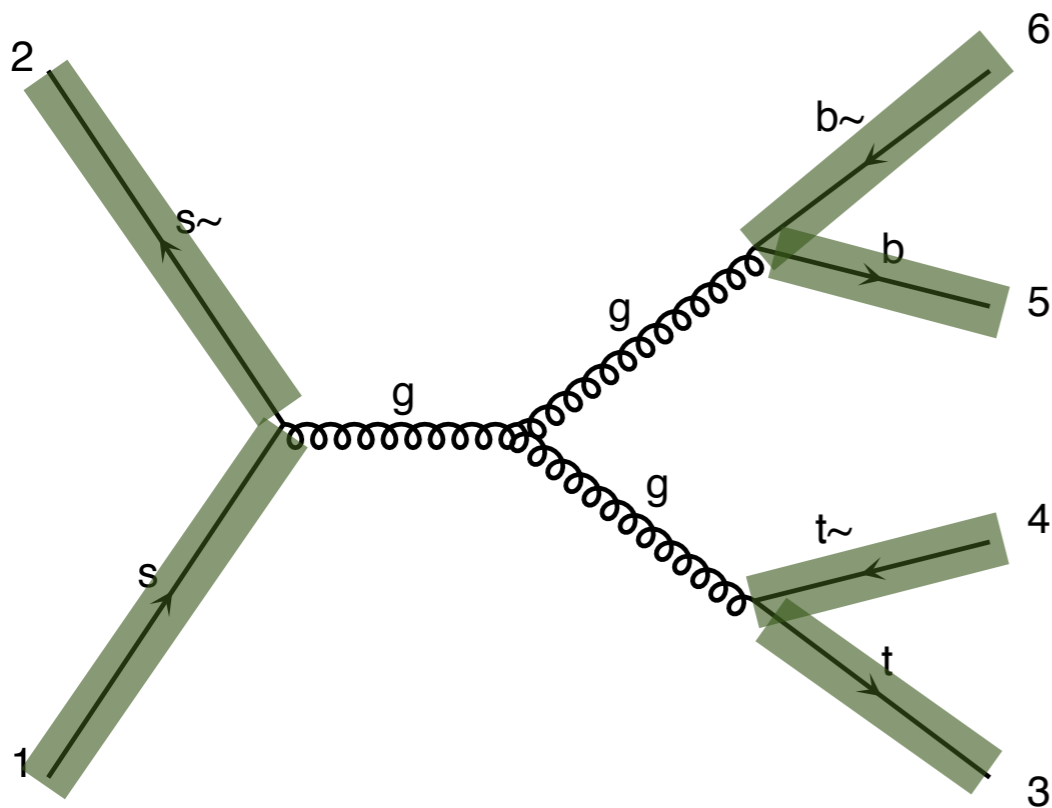


Number of routines: 1

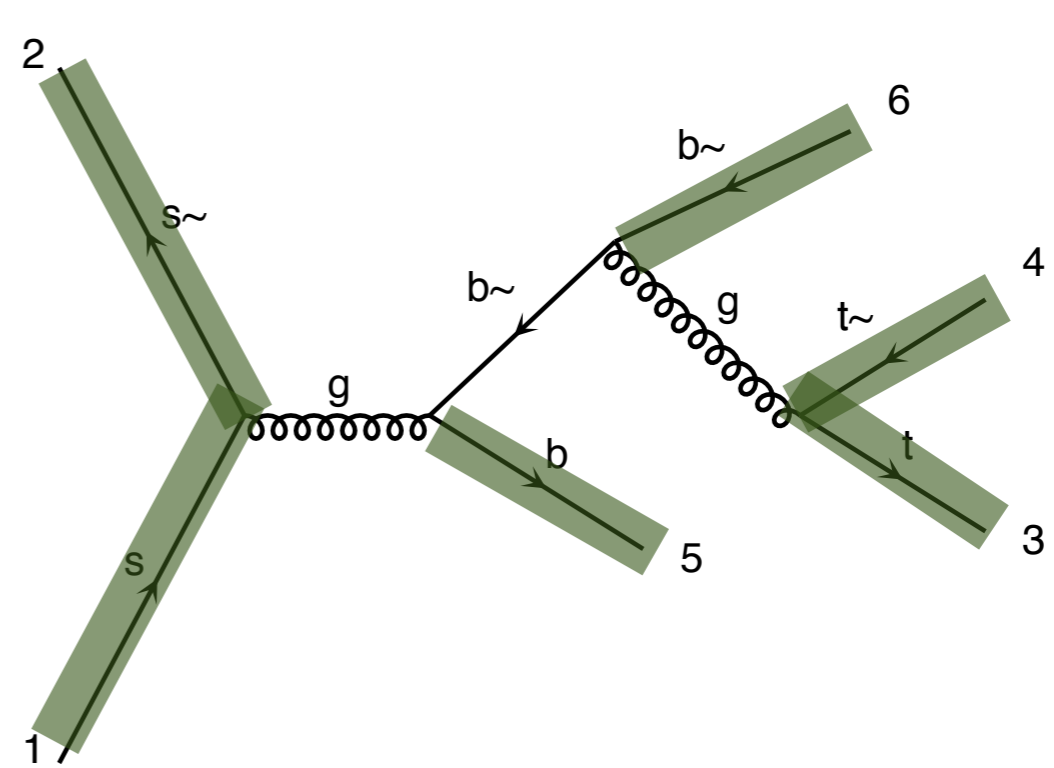
Number of routines: 1

Number of routines for both: 1

Real case

 Known


Number of routines: 6

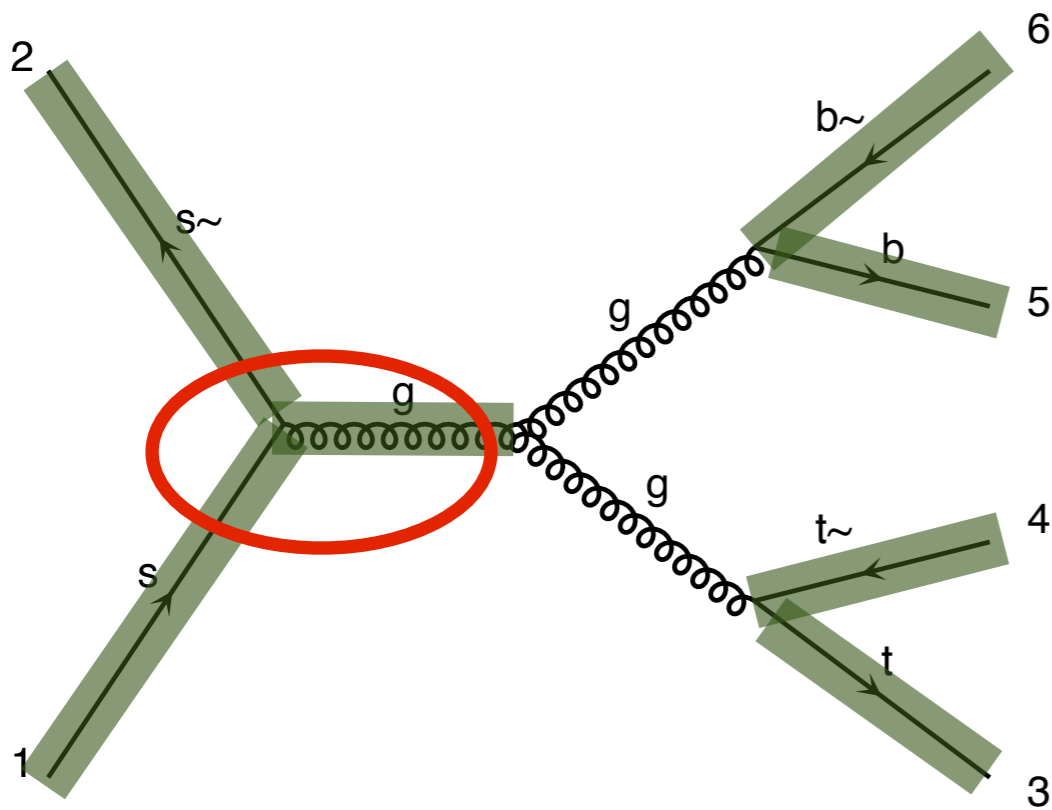


Number of routines: 6

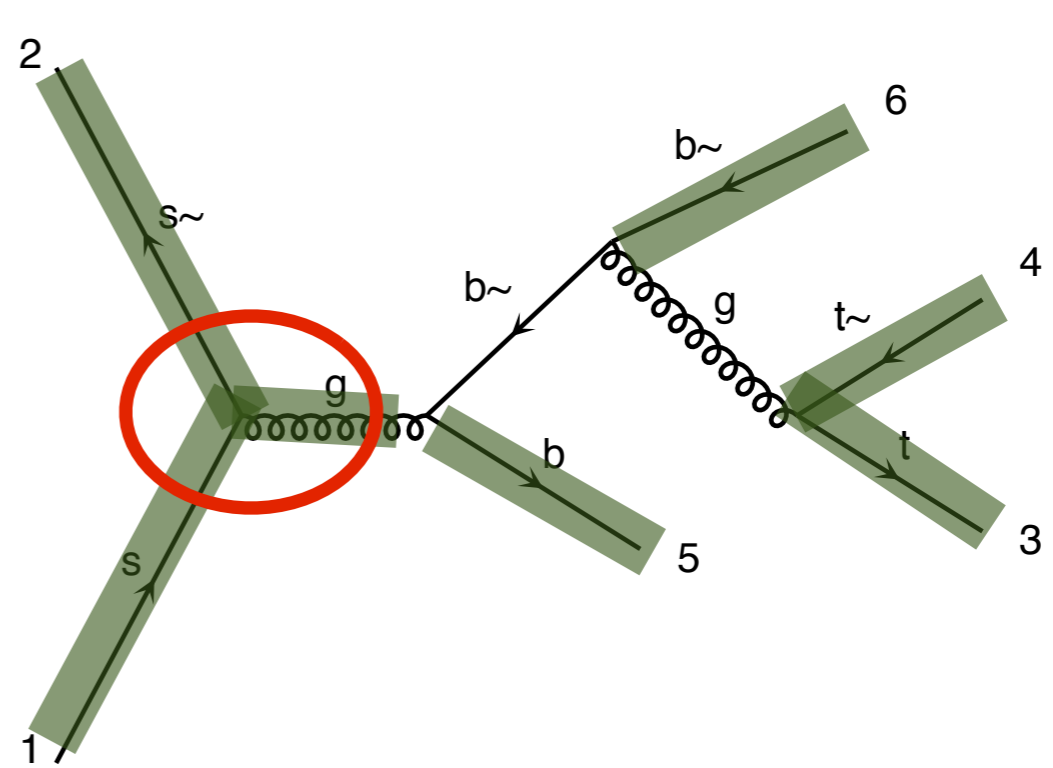
Number of routines for both: 6

Real case

 Known



Number of routines: 7

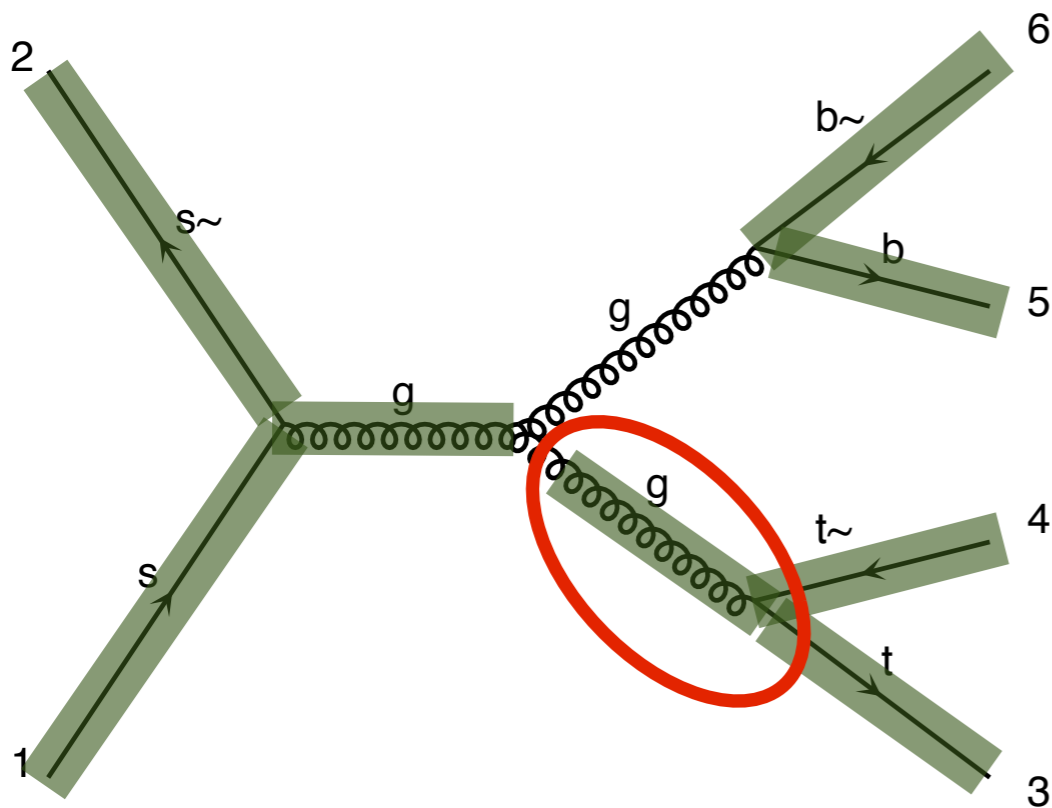


Number of routines: 7

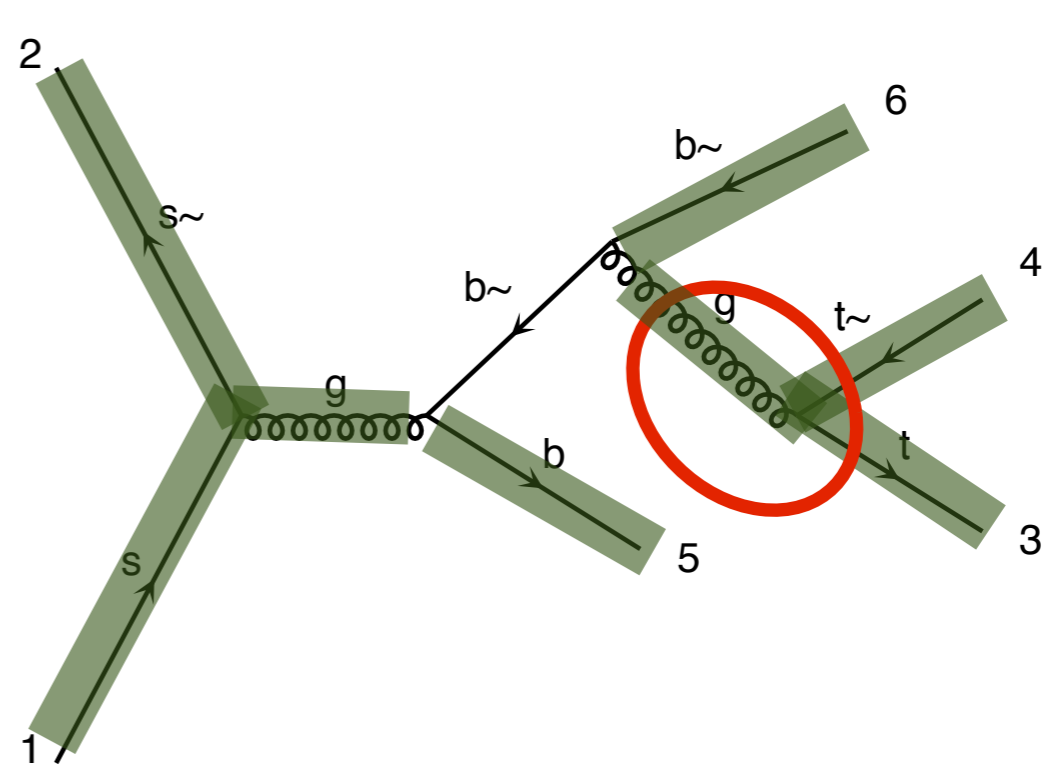
Number of routines for both: 7

Real case

 Known



Number of routines: 8

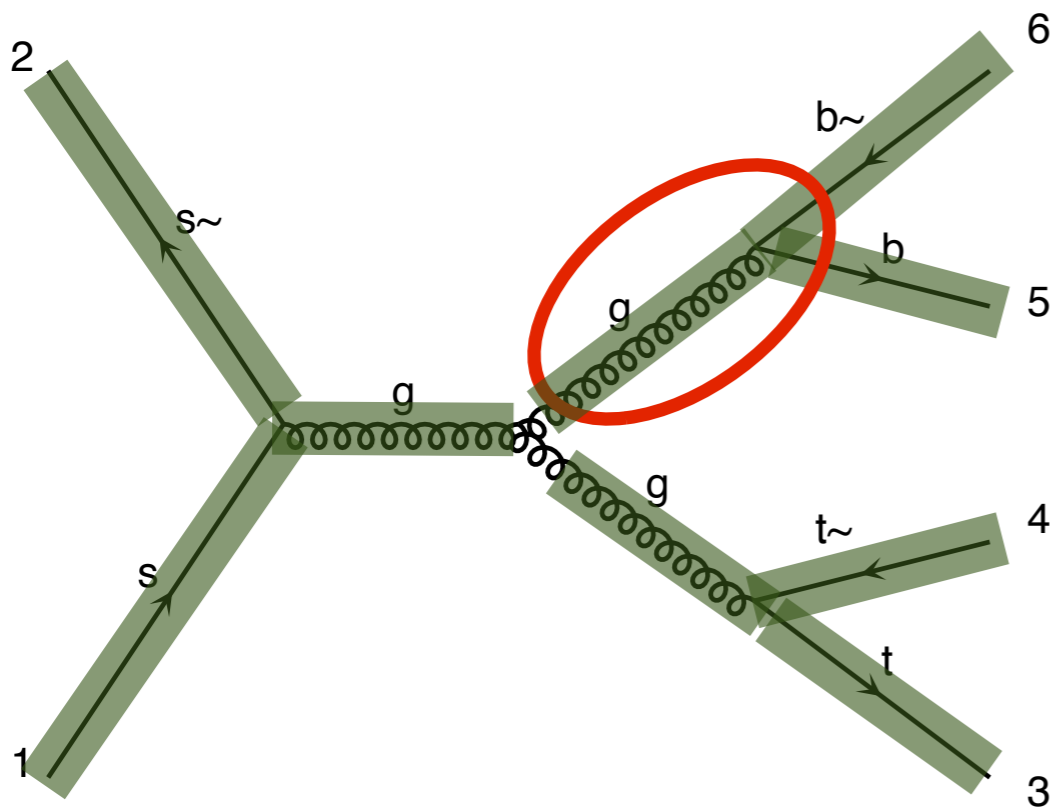


Number of routines: 8

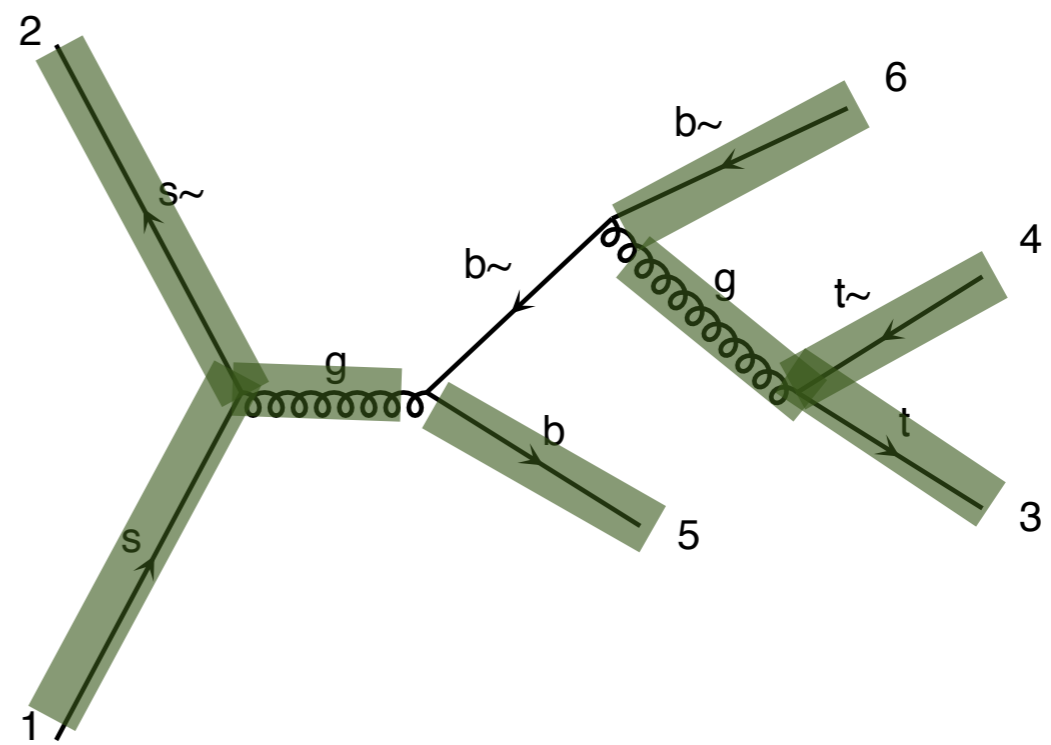
Number of routines for both: 8

Real case

 Known



Number of routines: 9

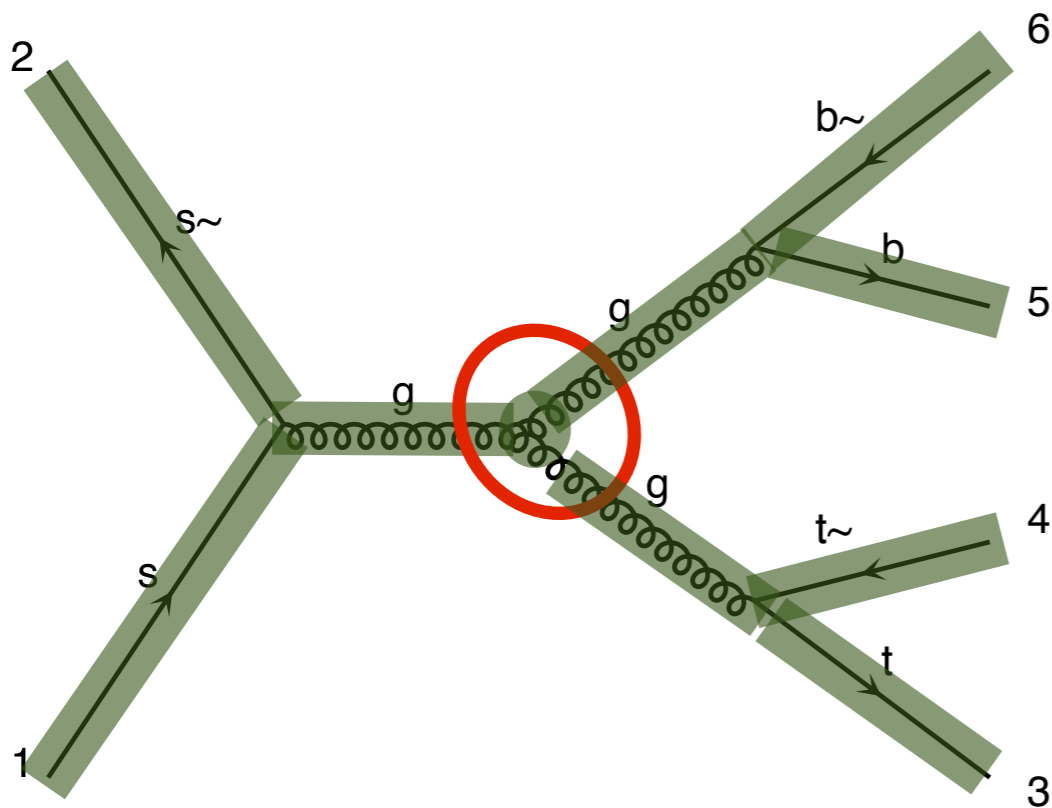


Number of routines: 8

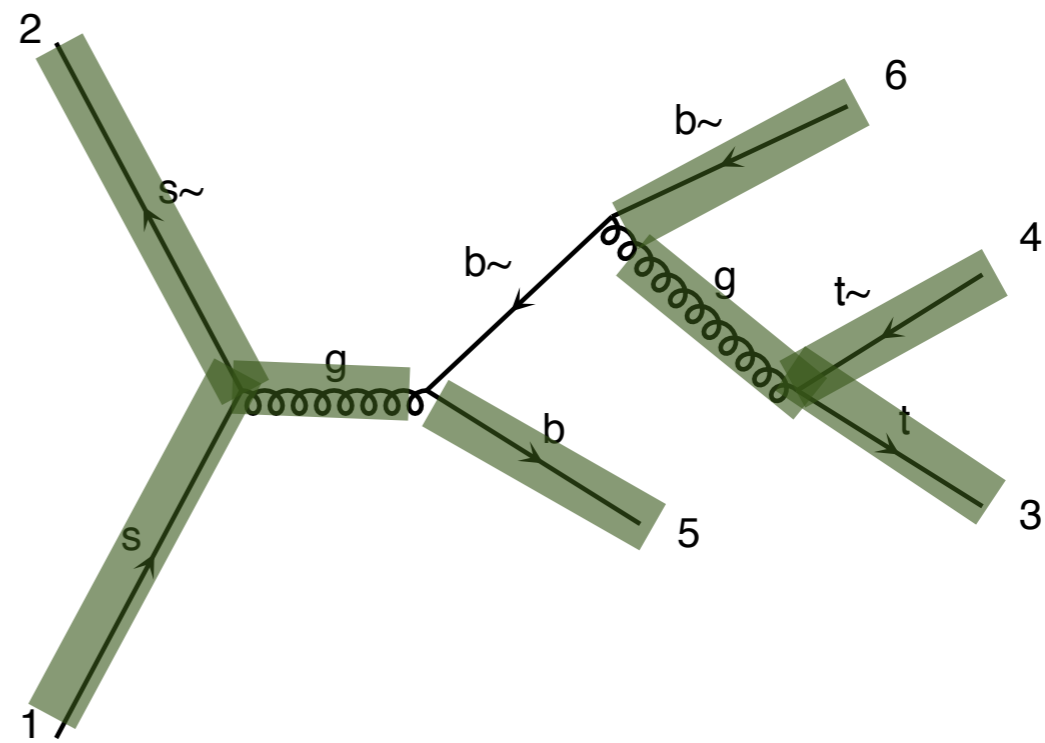
Number of routines for both: 9

Real case

 Known



Number of routines: 10

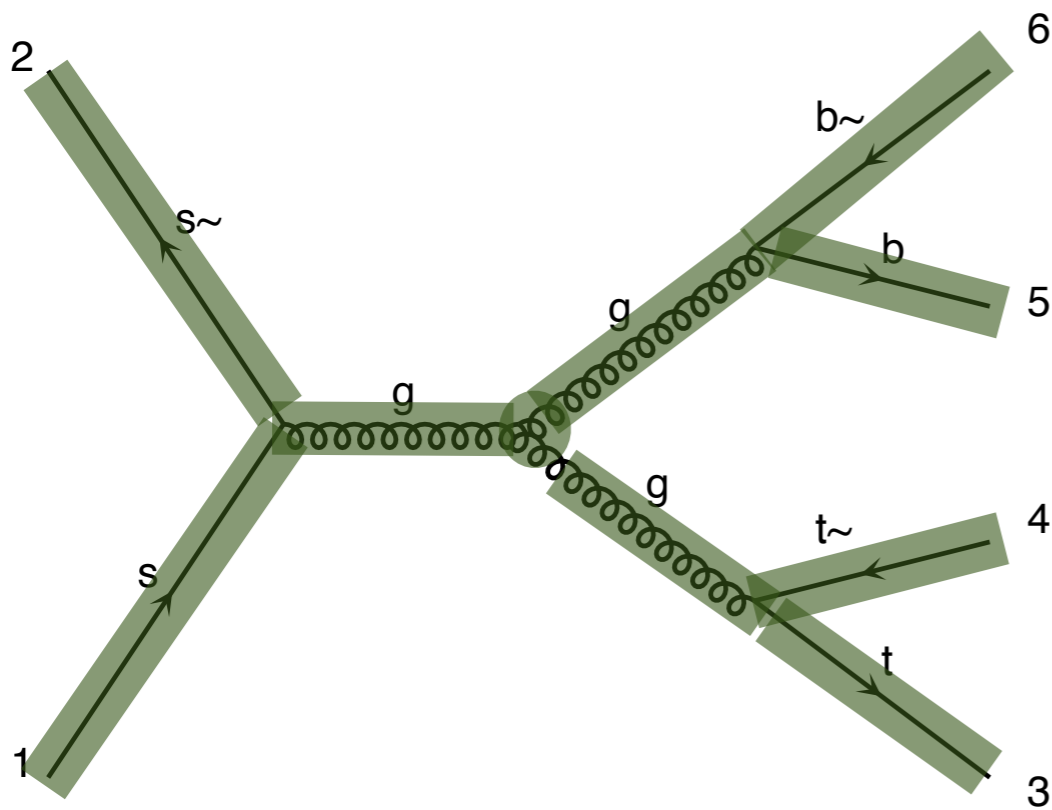


Number of routines: 8

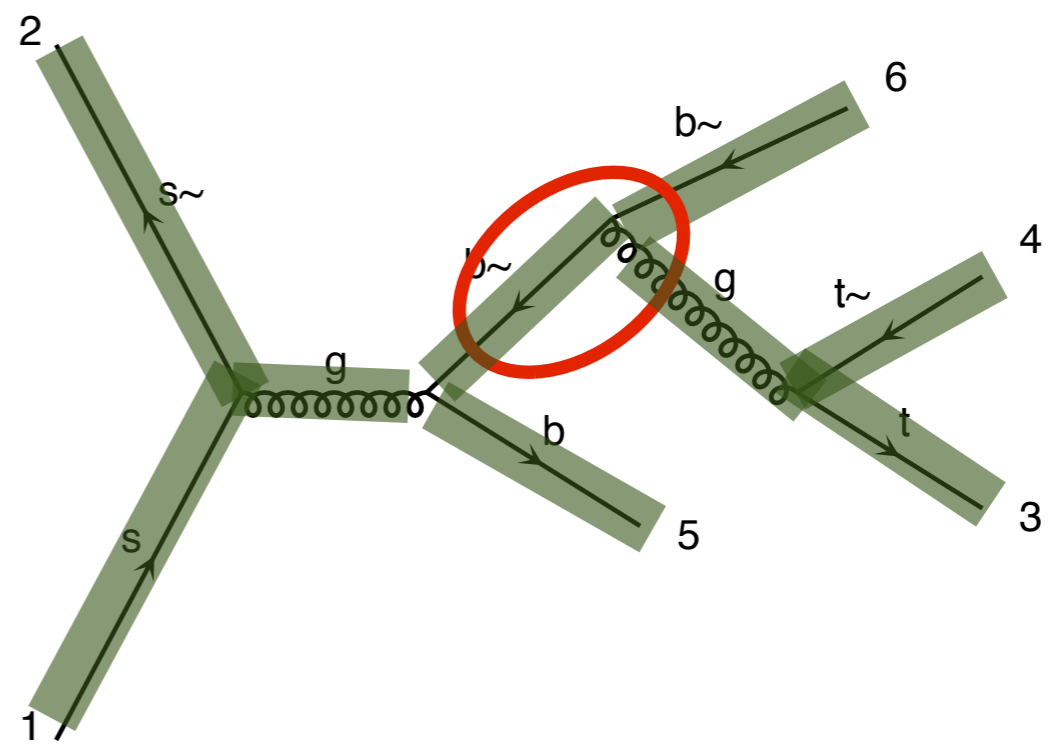
Number of routines for both: 10

Real case

 Known



Number of routines: 10

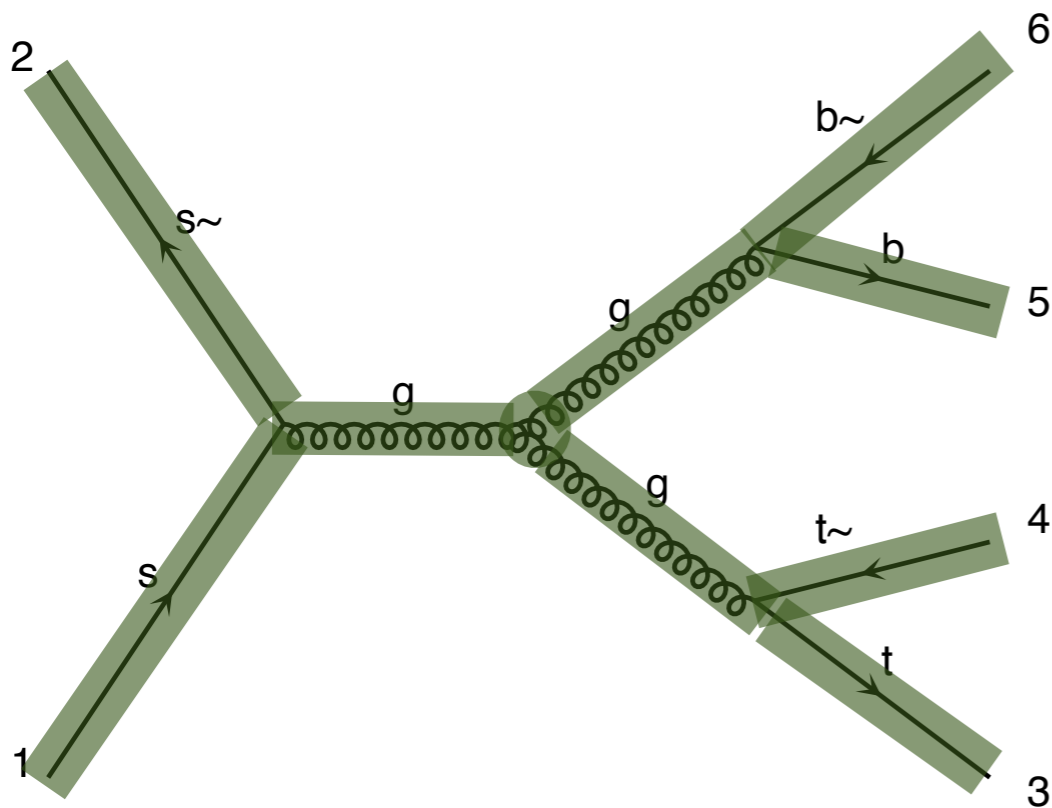


Number of routines: 9

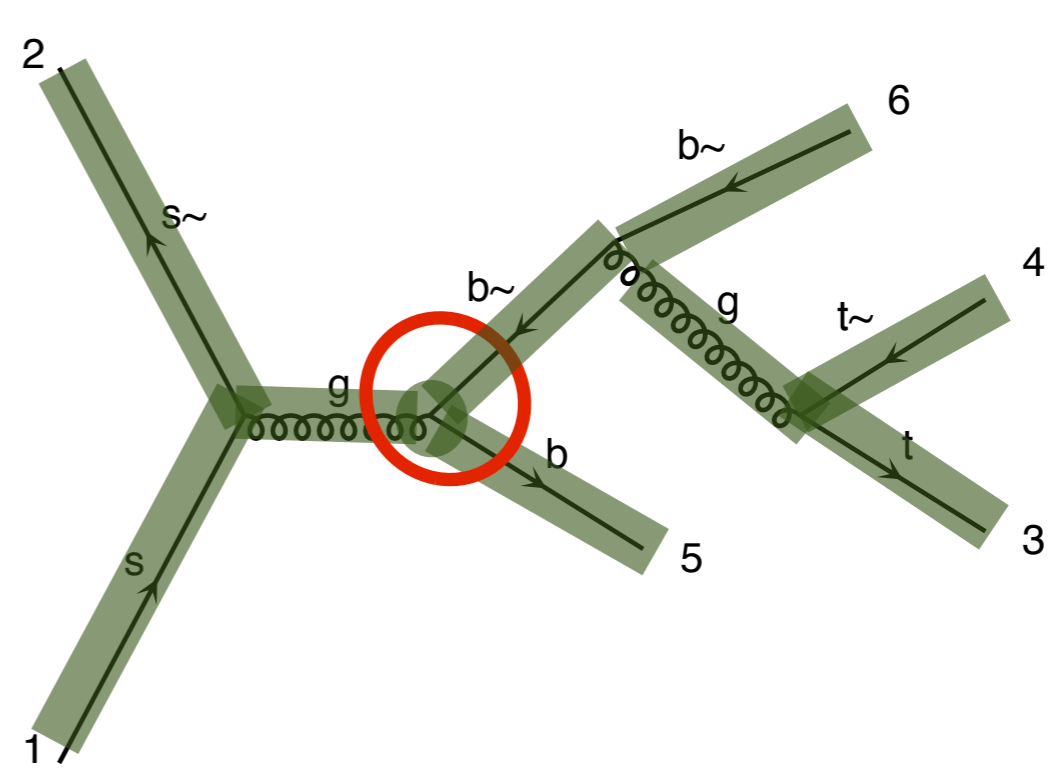
Number of routines for both: 11

Real case

 Known



Number of routines: 10



Number of routines: 10

Number of routines for both: 12

Basics: Helicity amplitudes

- Thanks to new diagram generation algorithm, wf recycling much more efficient in MG5 than MG4

Process	Amplitudes	Wavefunctions		Run time		no recycling
		MG 4	MG 5	MG 4	MG 5	
$u\bar{u} \rightarrow e^+e^-$	2	6	6	$< 6\mu\text{s}$	$< 6\mu\text{s}$	
$u\bar{u} \rightarrow e^+e^-e^+e^-$	48	62	32	0.22 ms	0.14 ms	
$u\bar{u} \rightarrow e^+e^-e^+e^-e^+e^-$	3474	3194	301	46.5 ms	19.0 ms	300k
$u\bar{u} \rightarrow d\bar{d}$	1	5	5	$< 4\mu\text{s}$	$< 4\mu\text{s}$	
$u\bar{u} \rightarrow d\bar{d}g$	5	11	11	27 μs	27 μs	
$u\bar{u} \rightarrow d\bar{d}gg$	38	47	29	0.42 ms	0.31 ms	
$u\bar{u} \rightarrow d\bar{d}ggg$	393	355	122	10.8 ms	6.75 ms	
$u\bar{u} \rightarrow u\bar{u}gg$	76	84	40	1.24 ms	0.80 ms	
$u\bar{u} \rightarrow u\bar{u}ggg$	786	682	174	35.7 ms	17.2 ms	
$u\bar{u} \rightarrow d\bar{d}d\bar{d}$	14	28	19	84 μs	83 μs	
$u\bar{u} \rightarrow d\bar{d}d\bar{d}g$	132	178	65	1.88 ms	1.15 ms	
$u\bar{u} \rightarrow d\bar{d}d\bar{d}gg$	1590	1782	286	141 ms	34.4 ms	
$u\bar{u} \rightarrow d\bar{d}d\bar{d}d\bar{d}$	612	758	141	42.5 ms	6.6 ms	5500

Time for matrix element evaluation on a Sony Vaio TZ laptop

HELAS

HELAS

- Original HELicity Amplitude Subroutine library
[Murayama, Watanabe, Hagiwara]

HELAS

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[Murayama, Watanabe, Hagiwara]
- One routine by Lorentz structure
 - ➔ MSSM [cho, al] hep-ph/0601063 (2006)
 - ➔ HEFT [Frederix] (2007)
 - ➔ Spin 2 [Hagiwara, al] 0805.2554 (2008)
 - ➔ Spin 3/2 [Mawatari, al] 1101.1289 (2011)

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SLIH

Chiral Perturbation

BNV Model

Effective Field Theory

NMSSM

Full HEFT

Chromo-magnetic
operator

Black Holes

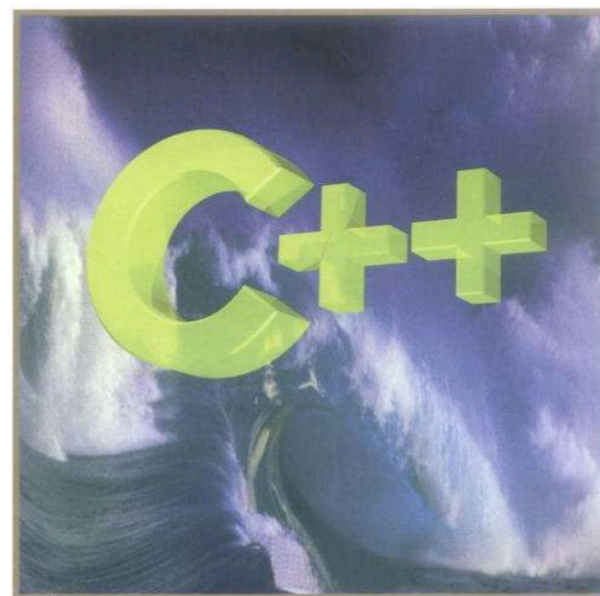
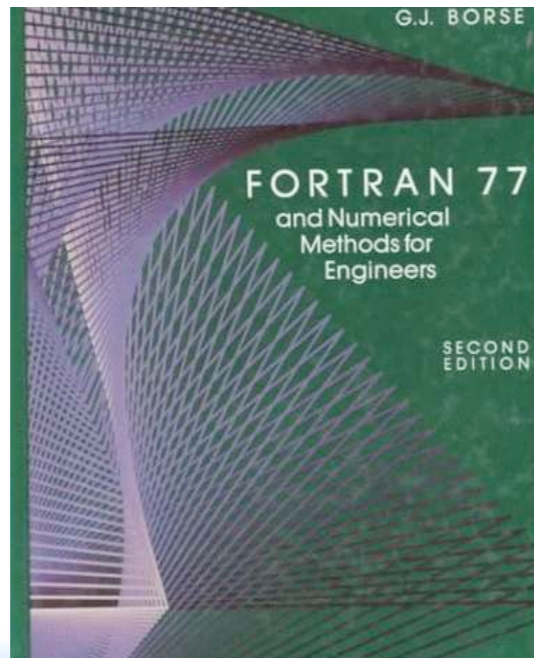


ALOHA

~~ALOHA Google translate~~

From: [UFO] To: Helicity [Translate]

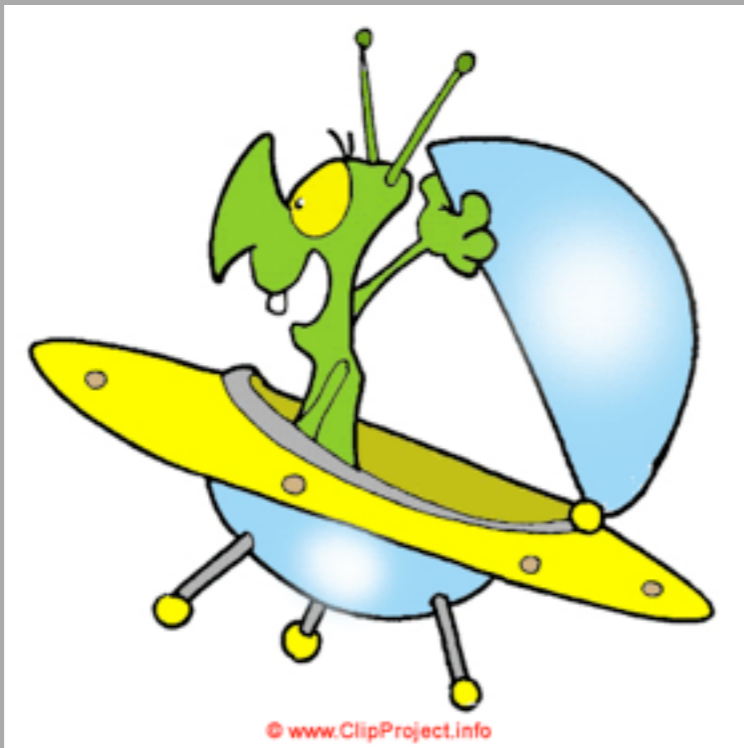
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ALOHA

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From: [UFO] To: Helicity [Translate]



- FeynRules output
- New Model Format
- Gosam/ Herwig++/ MG5
- Fully generic color/Lorentz/...

[Degrande, Duhr, Fuks, Grellscheid, OM, Reiter: I08.2040]

WESLEY J. CHUN

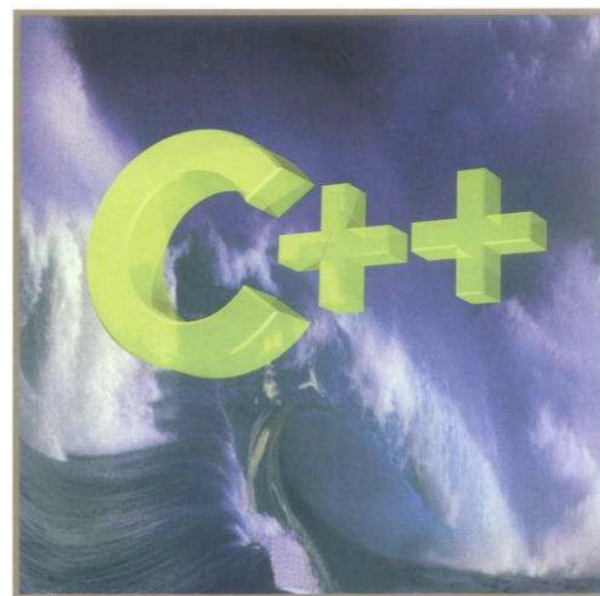
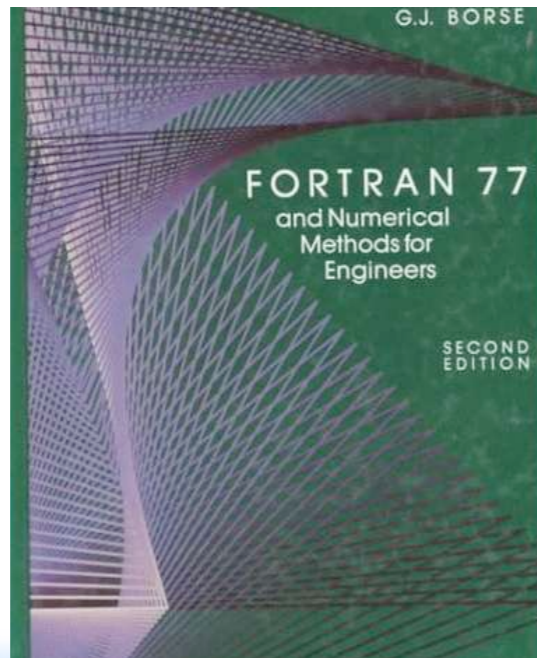


ALOHA

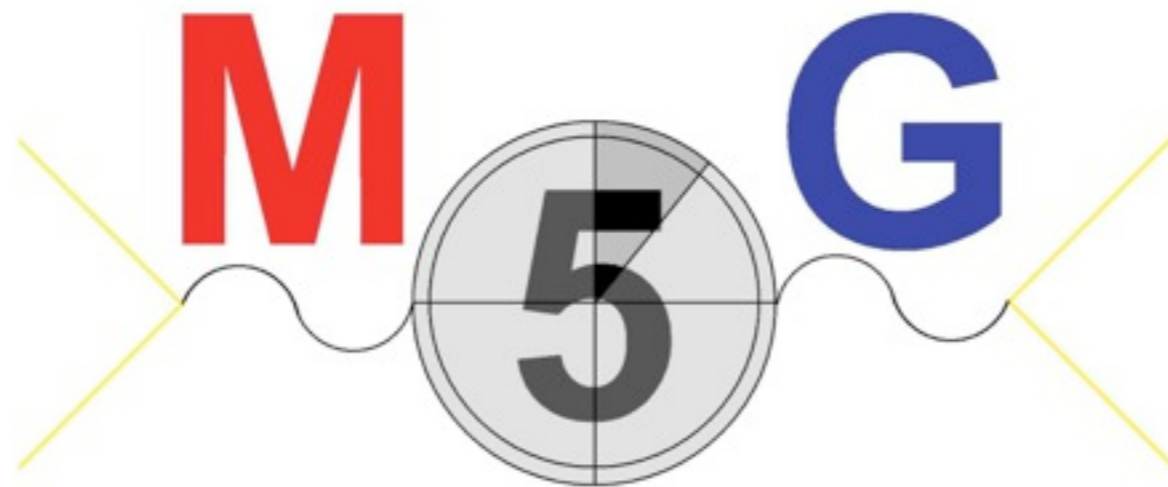
ALOHA
~~Google~~ translate

From: [UFO] To: Helicity [Translate]

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MADGRAPH 5



MADGRAPH

MADGRAPH

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Not possible to detail everything

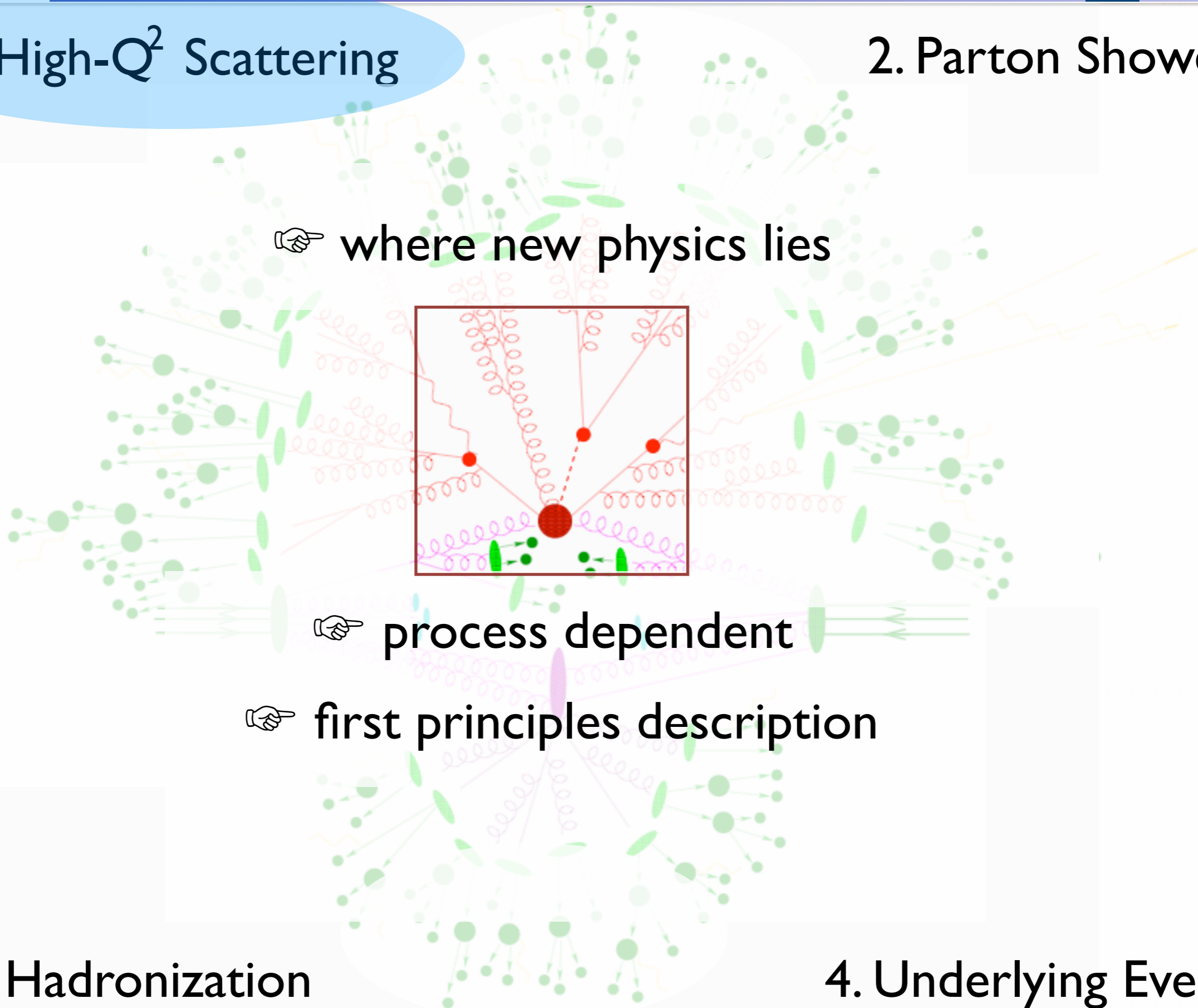
1.4.0

MadGraph

- Original MadGraph by Tim Stelzer was written in Fortran, first version from 1994 [hep-ph/9401258](https://arxiv.org/abs/hep-ph/9401258)

I. High- Q^2 Scattering

2. Parton Shower



3. Hadronization

4. Underlying Event

MadGraph

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- Event generation by MadEvent using the single diagram enhanced multichannel integration technique in 2002 (Stelzer, Maltoni) [hep-ph/0208156](https://arxiv.org/abs/hep-ph/0208156)

Master formula

$$\int \hat{\sigma}_{ab \rightarrow X}(\hat{s}, \dots) f_a(x_1) f_b(x_2) dx_1 dx_2 d\Phi_{FS}$$

Parton level cross section
Parton density functions
Phase space integral

- Parton level cross section from matrix element
- Parton density (or distribution) functions:
Process independent, determined by particle type

MadGraph

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- Rewritten in Python in 2011: MG5 [arXiv:1106.0522](https://arxiv.org/abs/hep-ph/11060522)
 - ➔ Full automatic support of BSM

MadGraph

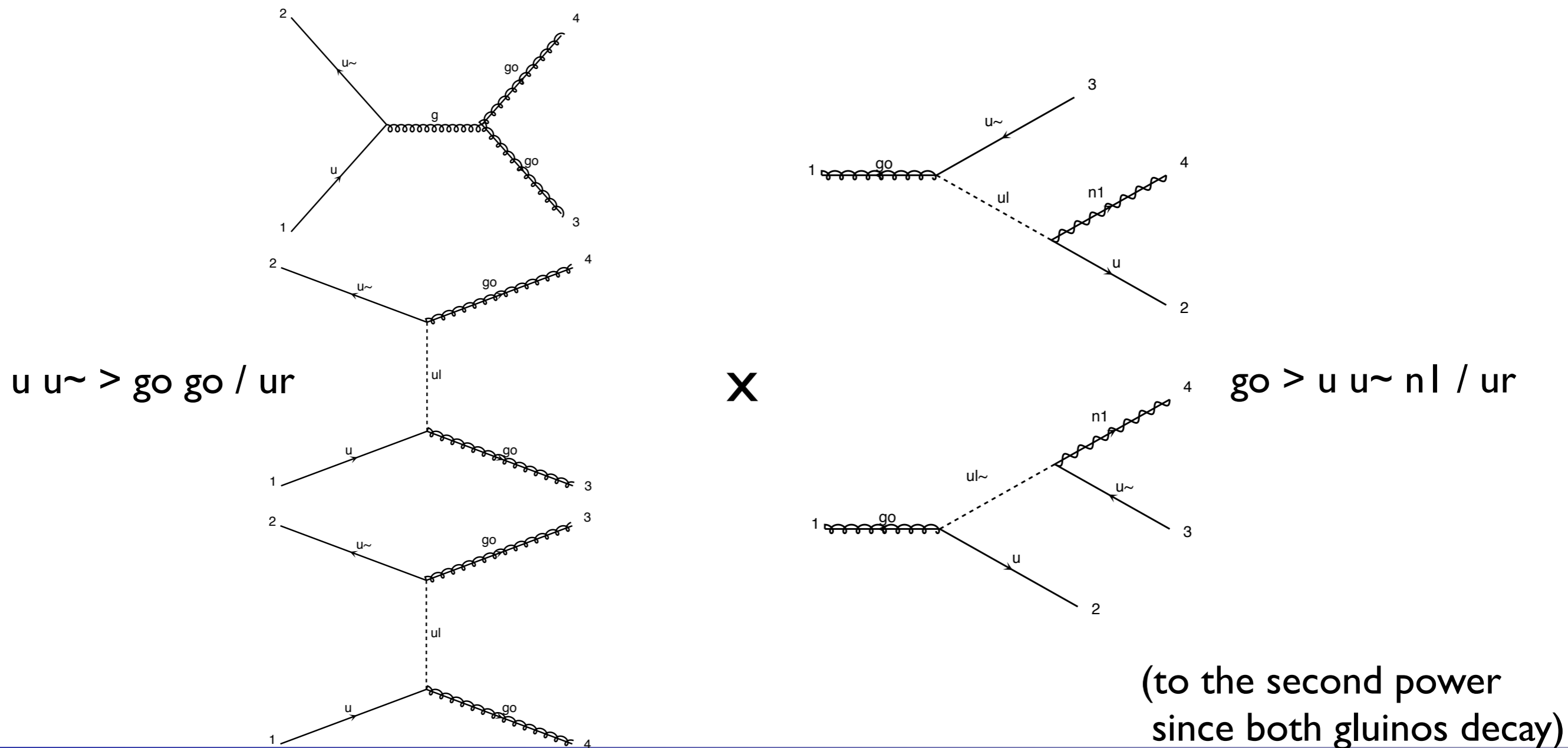
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 - ➔ Full automatic support of BSM
- First version of aMC@NLO in 2013 [In preparation](#)

Decay chains

- $p \rightarrow t \rightarrow w^+, (t \rightarrow w^+ b, w^+ \rightarrow l^+ \nu_l), \backslash$
 $(\bar{t} \rightarrow w^- \bar{b}, w^- \rightarrow j \bar{j}), \backslash$
 $w^+ \rightarrow l^+ \nu_l$
- Separately generate core process and each decay
 - Decays generated with the decaying particle as resulting wavefunction
- Iteratively combine decays and core processes
- **Difficulty: Multiple diagrams in decays**

Decay chains

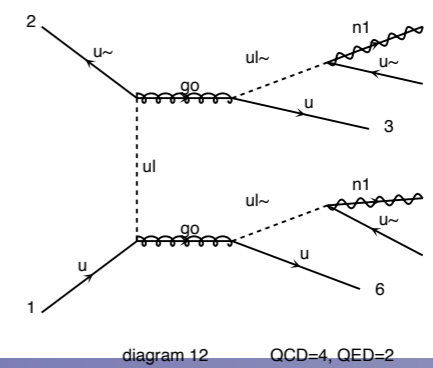
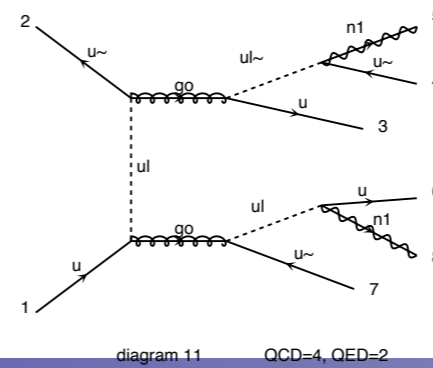
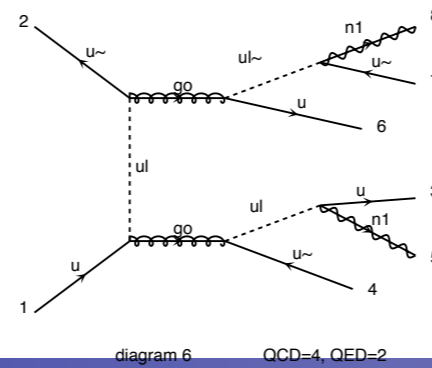
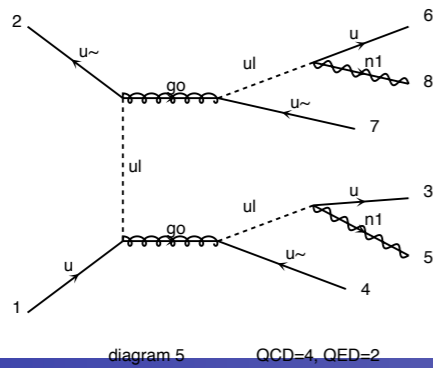
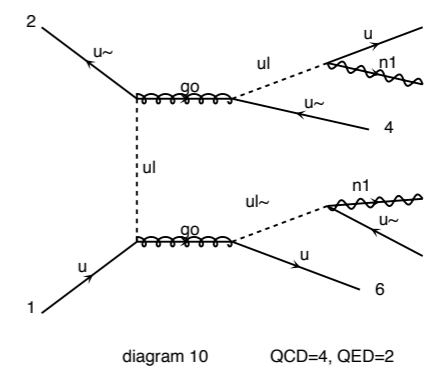
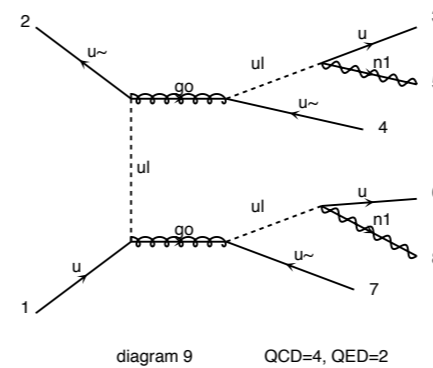
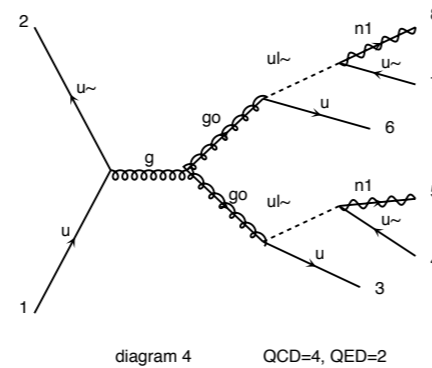
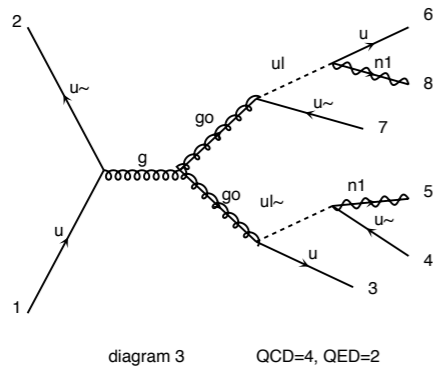
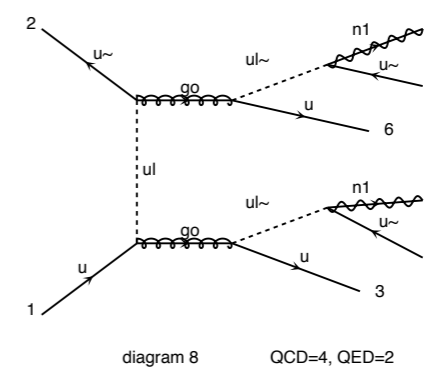
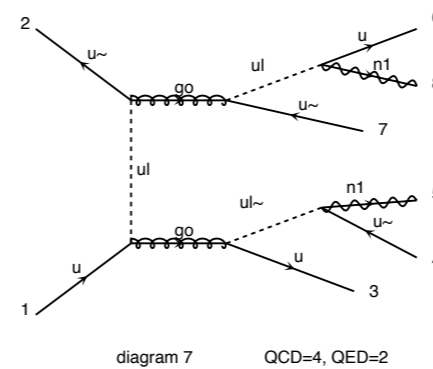
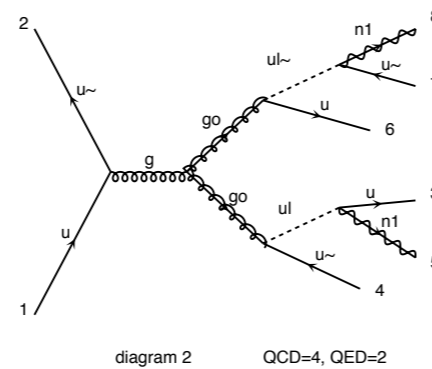
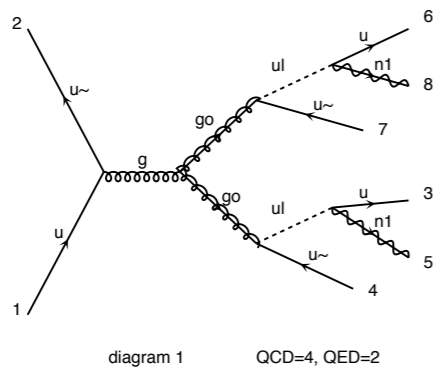
- If multiple diagrams in decays, need to multiply together core process and decay diagrams:



Decay chains

- If multiple diagrams in decays, need to multiply together core process and decay diagrams:

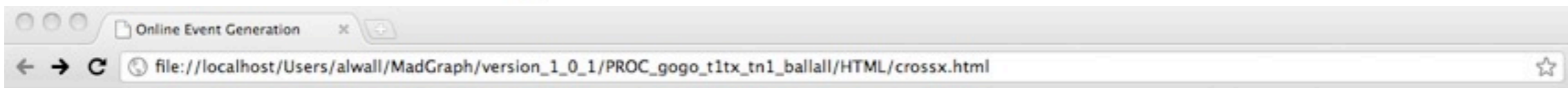
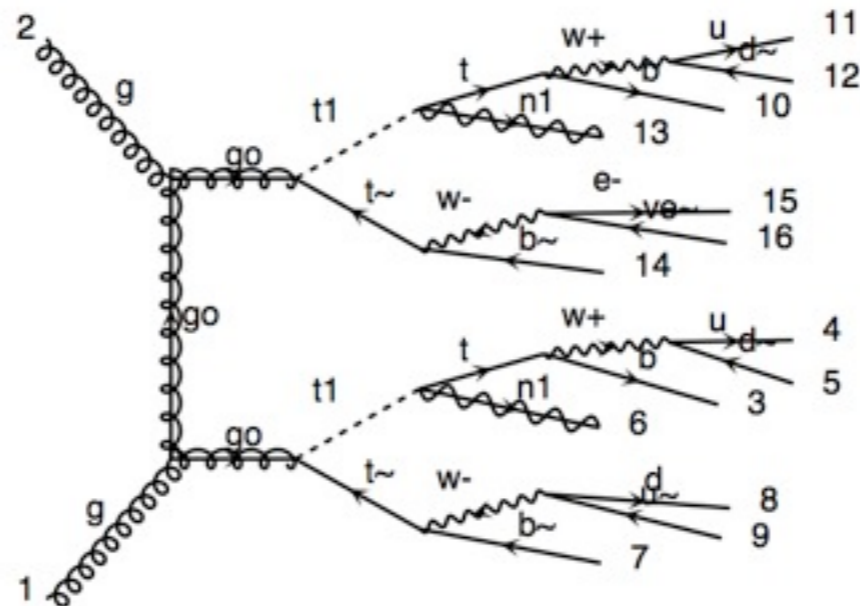
$$u u^{\sim} \rightarrow g o g o / u r, g o \rightarrow u u^{\sim} n l / u r$$



Decay chains

- Decay chains retain **full matrix element** for the diagrams compatible with the decay
- Full spin correlations (within and between decays)
- Full width effects
- However, no interference with non-resonant diagrams
 - ➔ Description only valid close to pole mass
 - ➔ Cutoff at $|m \pm n\Gamma|$ where n is set in `run_card`.

Decay chains



Results for $g g \rightarrow g_0 g_0$, ($g_0 \rightarrow t \bar{t}$, $t \rightarrow b W^+$, $\bar{t} \rightarrow \bar{b} W^-$) in the mssm

Available Results

Links	Events	Tag	Run	Collider	Cross section (pb)	Events
results banner	Parton-level LHE	fermi	test	pp 7000 x 7000 GeV	.33857E-03	10000

[Main Page](#)

Thanks to developments in MadEvent, also (very) long decay chains possible to simulate directly in MadGraph!

Output formats in MadGraph 5

- Thanks to UFO/ALOHA, we now have automatic helicity amplitude routines in any language
 - ➔ So it makes sense to have also matrix element output in multiple languages!
- Presently implemented: Fortran, C++, Python
 - ➔ Fortran - for MadEvent and Standalone
 - ➔ C++ - for Pythia 8 and Standalone
 - ➔ Python - for internal use in MG5 (checks of gauge, perturbation and Lorentz invariance)

Pythia 8 Matrix Element output

- ➔ Library of process .h and .cc files, sorted by model
+ all needed model and helicity amplitude files
+ example main file
(for user convenience!)
- ➔ Run as standard internal Pythia processes
- ➔ Allows using Pythia for ANY (2→1,2,3) process in ANY model at the push of a key!

Sigma_sm_qq_ttx.h

```
#include "SigmaProcess.h"
#include "Parameters_sm.h"

using namespace std;

namespace Pythia8
{
//=====
// A class for calculating the matrix elements for
// Process: u u~ > t t~
// Process: c c~ > t t~
// Process: d d~ > t t~
// Process: s s~ > t t~
//-----
class Sigma_sm_qq_ttx : public Sigma2Process
{
public:

// Constructor.
Sigma_sm_qq_ttx() {}

// Initialize process.
virtual void initProc();

// Calculate flavour-independent parts of cross section.
virtual void sigmaKin();

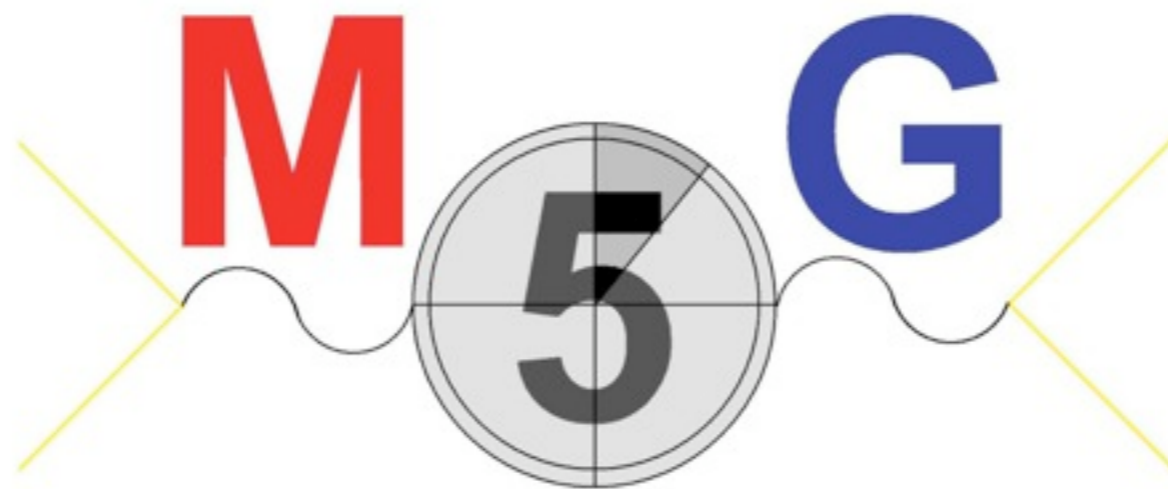
// Evaluate sigmaHat(sHat).
virtual double sigmaHat();

// Select flavour, colour and anticolour.
virtual void setIdColAcol();

...
}
```

MADGRAPH 5

Life Demonstration



Examples shown

- $p p \rightarrow t \bar{t}$
This gives only (the dominant) QCD vertices, and ignores (the negligible) QED vertices.
- $p p \rightarrow t \bar{t}$ QED=2
This gives both QED and QCD vertices.
- $p p \rightarrow w^+ j j, w^+ \rightarrow l^+ \nu_l$
More complicated example.

More syntax examples

- $p p \rightarrow t \bar{t} j$ QED=2: Generate all combinations of processes for particles defined in multiparticle labels p / j , including up to two QED vertices (and unlimited QCD vertices)
- $p p \rightarrow t \bar{t}, (t \rightarrow b W^+, W^+ \rightarrow l^+ \nu_l), \bar{t} \rightarrow \bar{b} j j$:
 - Only diagrams compatible with given decay
 - Only t / \bar{t} and W^+ close to mass shell in event generation
- $p p \rightarrow W^+ W^- / h$: Exclude any diagrams with h
- $p p \rightarrow W^+ W^- \& h$: Exclude on-shell h in event generation (but retain interference effects)

MadSpin

Decay with Full Spin correlation

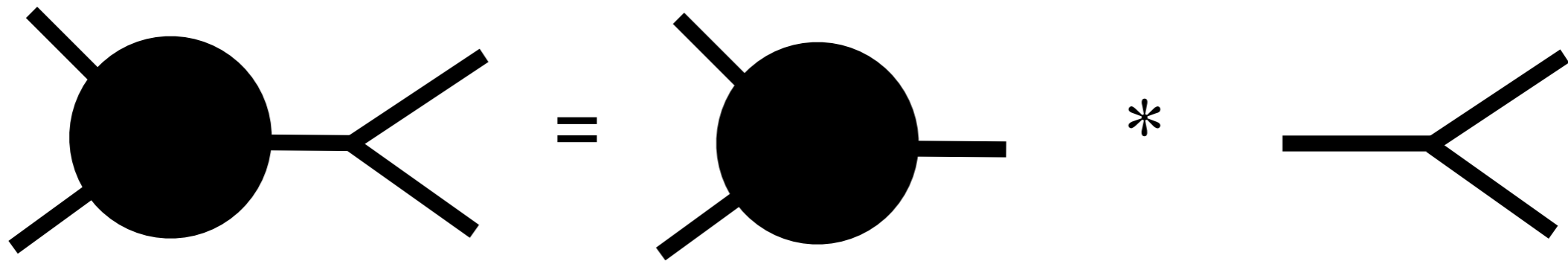
[P.Artoisenet, R. Frederix, OM, R. RietKerk (2012)]

MADSPIN

- Separate production from decay
 - ➔ Matrix Element can't be integrate
 - ◆ NLO
- This is valid in the Narrow width approximation

MADSPIN

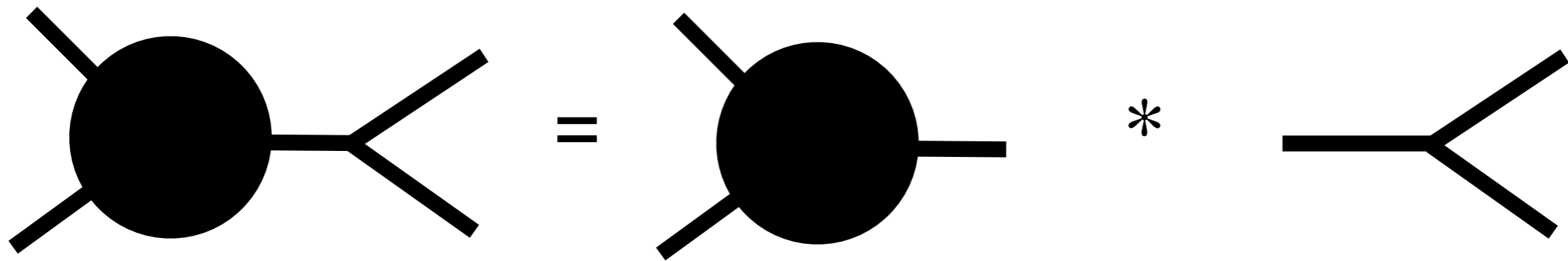
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 - ➔ Matrix Element can't be integrate
 - ✦ NLO
- This is valid in the Narrow width approximation



$$\sigma_{N+1} \simeq \sigma_N * \frac{\Gamma_{1 \rightarrow 2}}{\Gamma_{tot}}$$

- You loose:
 - ➔ Full spin correlation
 - ➔ finite width effect

MADSPIN

Read Event

generate a virtual mass

generate a decay

[Frixione, Leanen, Motylinski, Webber (2007)]

MADSPIN

Read Event

generate a virtual mass

generate a decay

- Finite width
- Spin correlation
- unweighted events

[Frixione, Leenen, Motylinski, Webber (2007)]

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$$|M_{LO}^P|^2 \longrightarrow |M_{LO}^{P+D}|^2$$

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[Frixione, Leenen, Motylinski, Webber (2007)]

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$$|M_{LO}^{P+D}|^2 / |M_{LO}^P|^2$$

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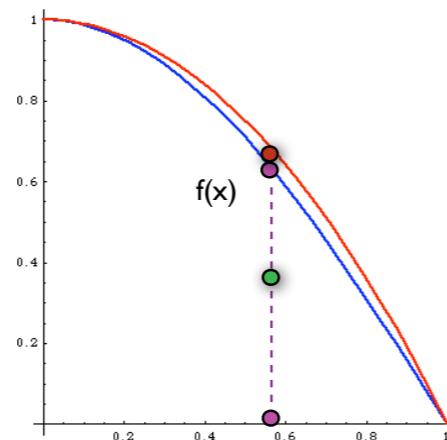
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[Frixione, Leanen, Motylinski, Webber (2007)]

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PASS

- Finite width

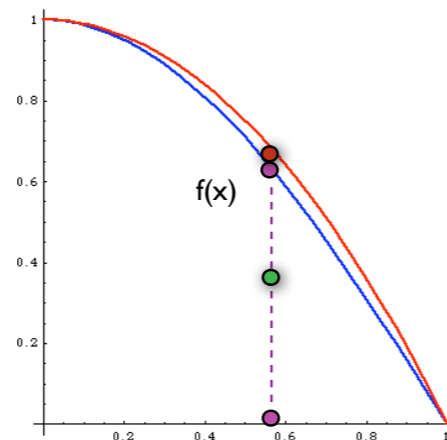
- Spin correlation

- unweighted events

- Finite width

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[Frixione, Leanen, Motylinski, Webber (2007)]

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unweighting

FAIL

PASS

- Finite width

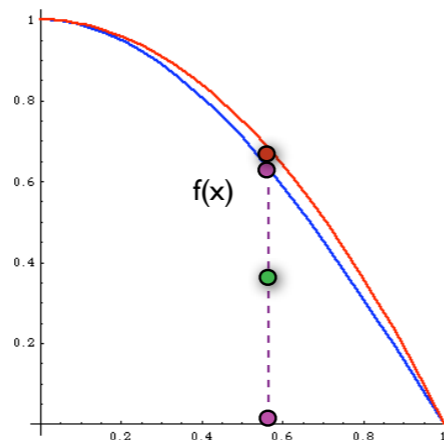
- Spin correlation

- unweighted events

- Finite width

- Spin correlation

- unweighted events



[Frixione, Leanen, Motylinski, Webber (2007)]

MADSPIN

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$$|M_{LO}^{P+D}|^2 / |M_{LO}^P|^2$$

unweighting

FAIL

PASS

- Finite width

- Spin correlation

- unweighted events

- Finite width

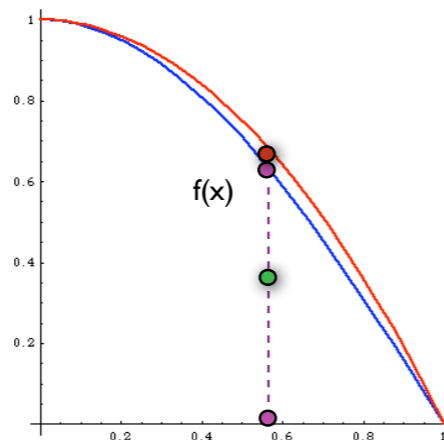
- Spin correlation

- unweighted events

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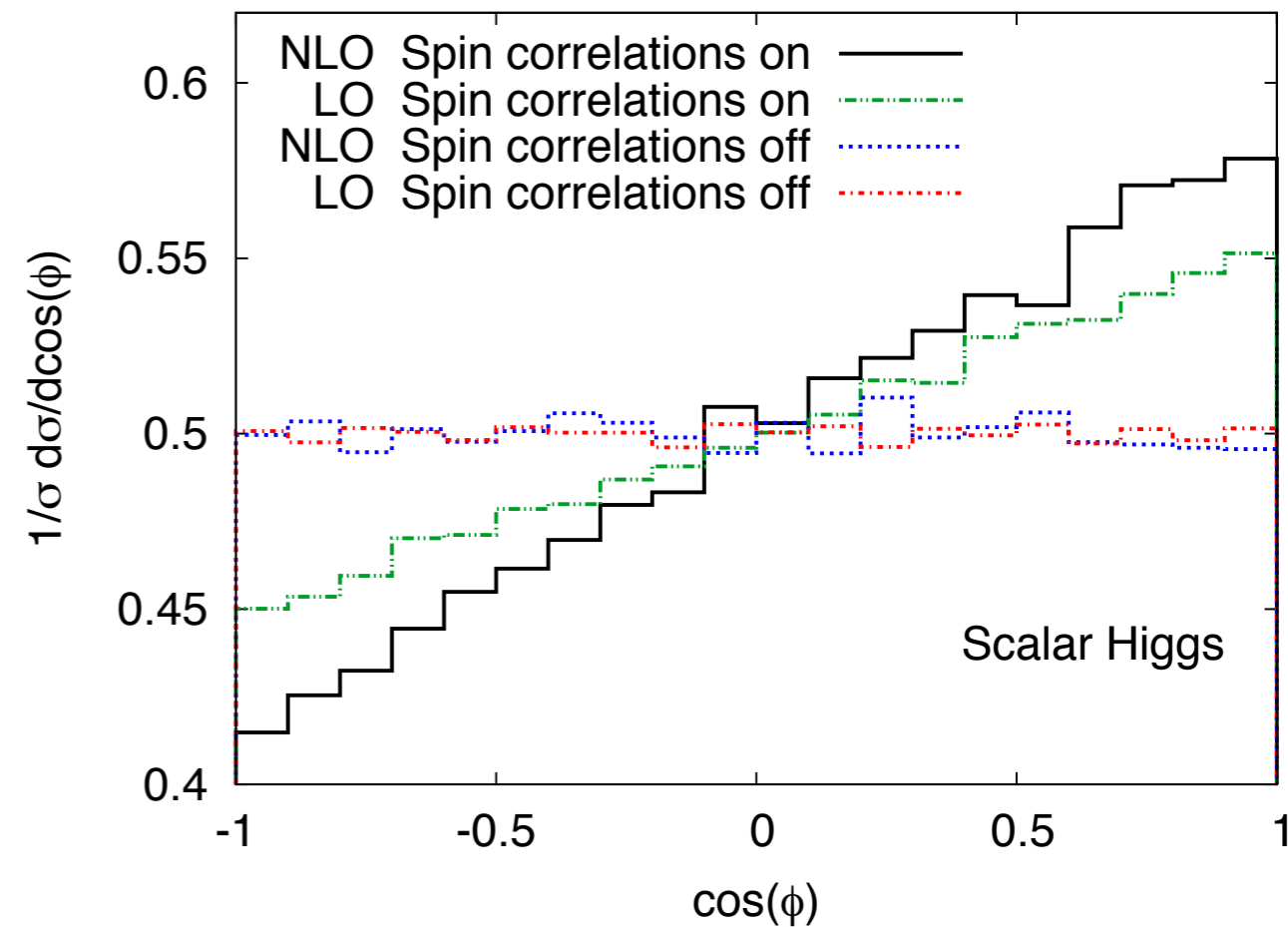
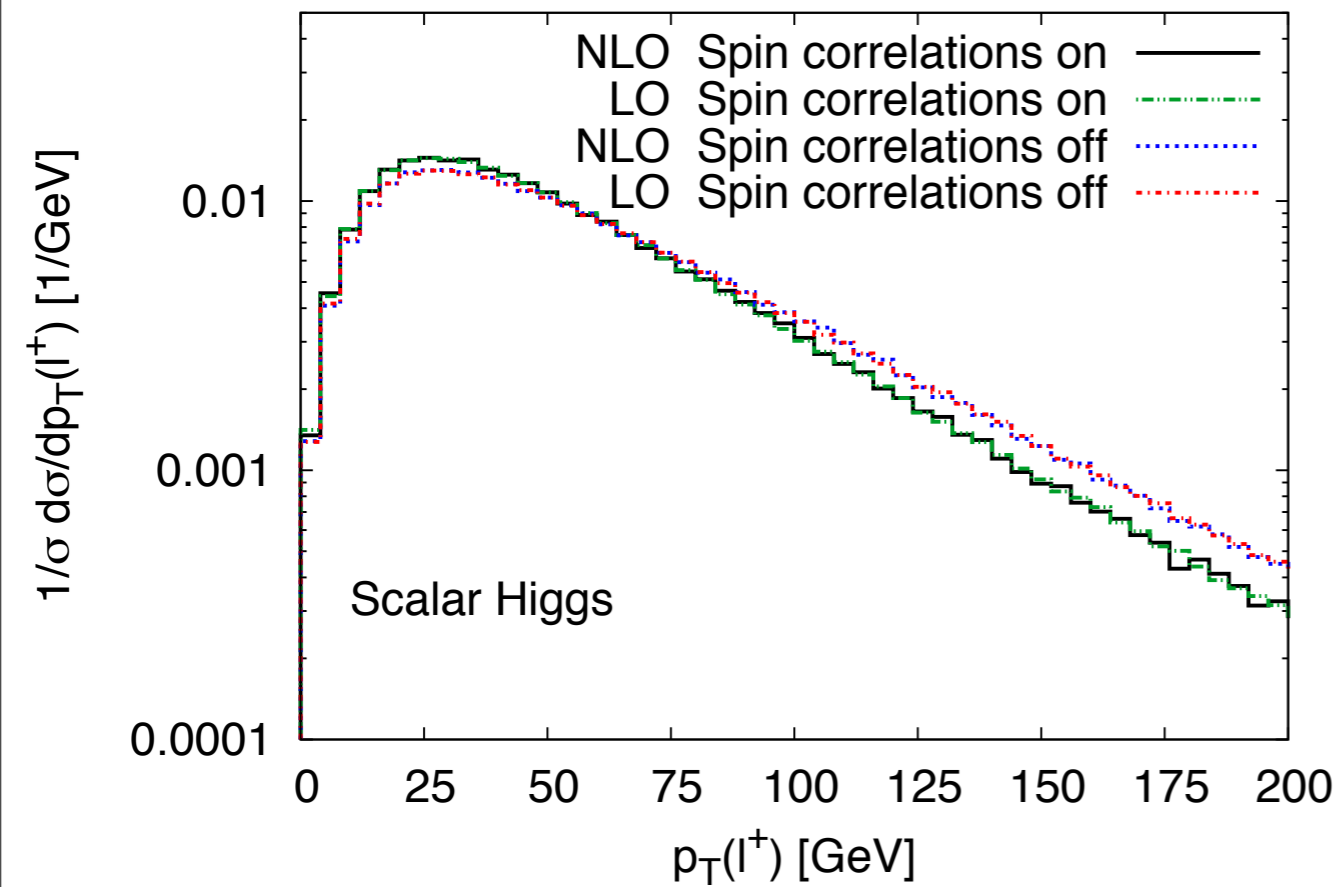
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MadSpin

- Fully automatic
 - ➔ Fully integrated in MG5 [LO and NLO]
 - ➔ Can be run in StandAlone

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- Fully automatic
 - ➔ Fully integrated in MG5 [LO and NLO]
 - ➔ Can be run in StandAlone
- Example $t \bar{t} h$:



Tutorial

- MG5 Tutorial today
 - ➔ Learn how to generate simple process
 - ◆ Learn the syntax
 - ➔ Learn the meaning of the cards
 - ➔ Learn decay chains syntax and the associate limitations

Conclusion

- UFO + ALOHA + MG5:
 - ➔ ANY BSM is available
 - ➔ HELAS Routine => very fast
- MG5
 - ➔ decay chains
 - ➔ nice interface
 - ➔ easy to use
- MadSpin
 - ➔ Efficient decay