MadGraph5

Olivier Mattelaer





Aim of the Lecture

- Get you acquainted with the concepts and techniques used in event generation
- Give you hands-on experience
- Answer as many of your questions as I can

Lecture I

- Introduction
- Evaluation of Matrix Element
- Integration of the cross-section/ events generation

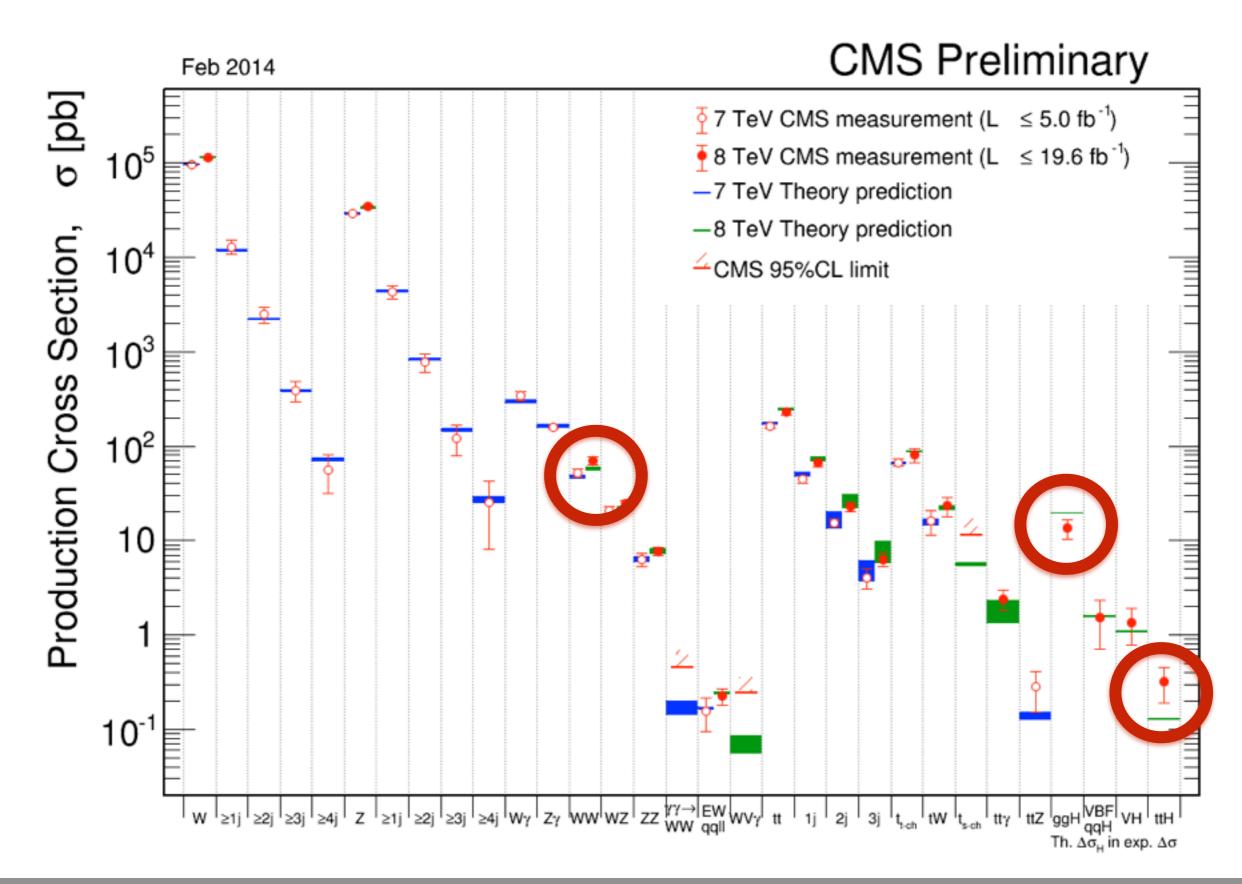
Lecture II

- Shower Monte-Carlo
- Matching/Merging



Standard Model

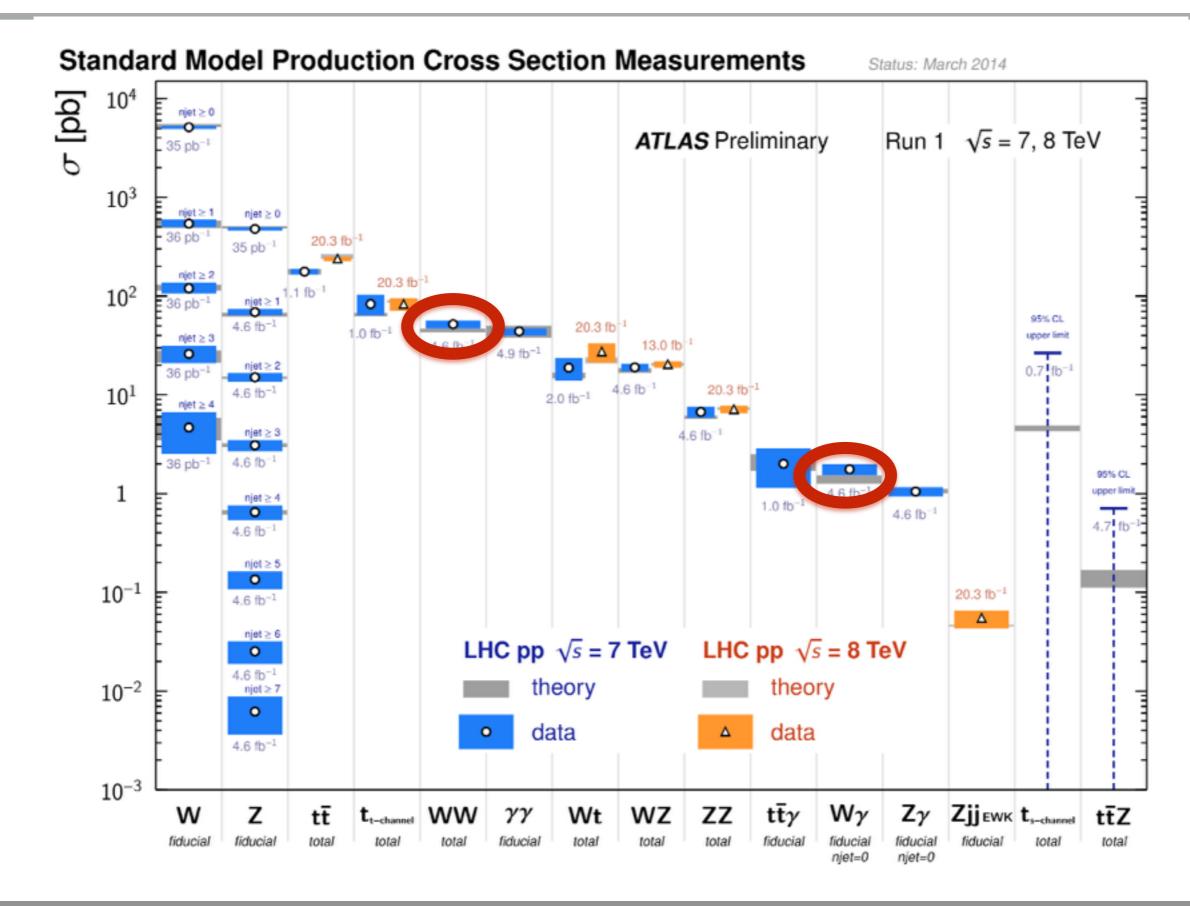






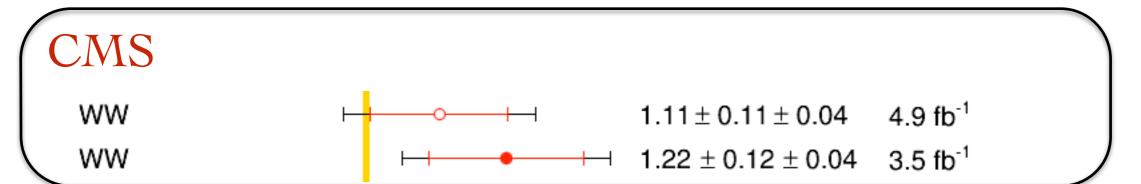
ATLAS

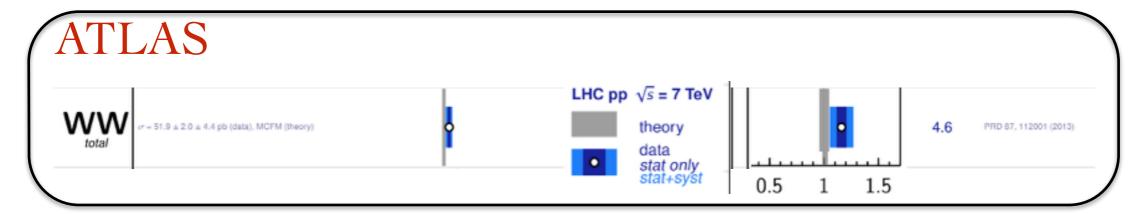












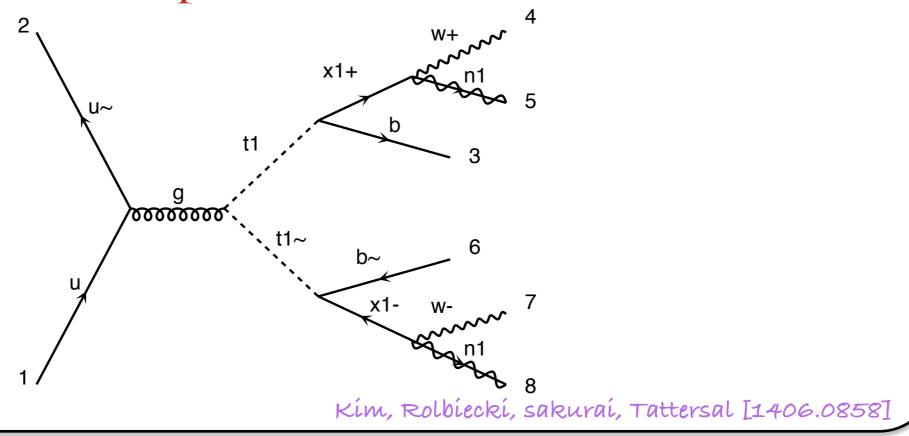
COMBINE

- Both seems indicates a 15-20% excess
- Not significant at all
- Need more data / theoretical precision





SUSY Like Explanation



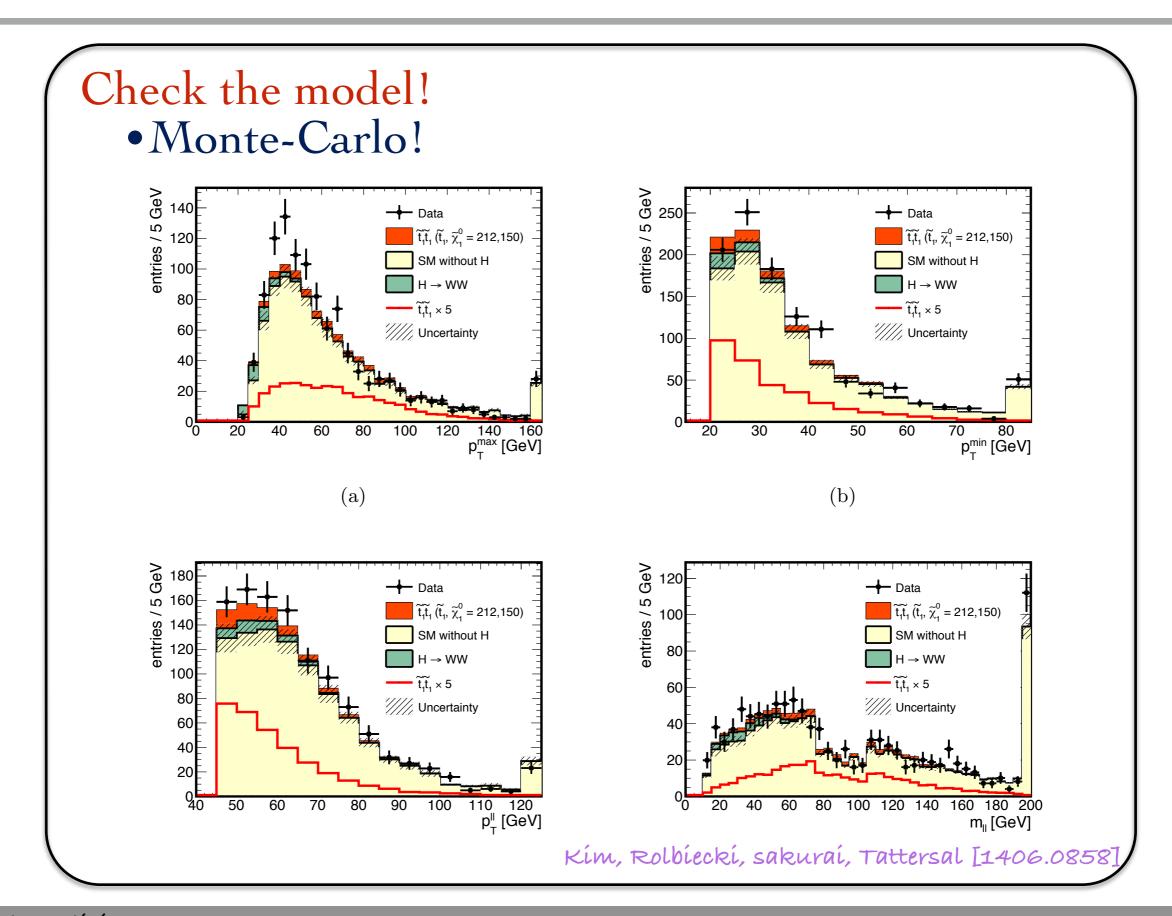
Compressed Spectrum $M_{\tilde{t}} \approx M_{\chi^+}$

$$M_{\tilde t} pprox M_{\chi^+}$$

- Soft b/b~
 - → not observed
- evade direct searches constraints



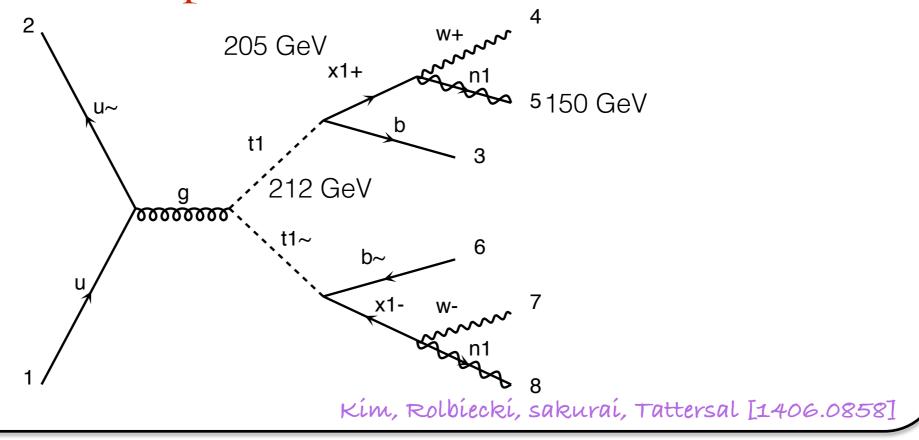








SUSY Like Explanation



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- 2. Exhaust SM explanations for the excess





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- 3. Think of possible new physics explanations
 - Within or outside of conventional/high scale models

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- 4. Find range of model parameters that can explain excess
 - → Typically, using Monte Carlo simulations





- I. An excess is discovered in data
- 2. Exhaust SM explanations for the excess
- 3. Think of possible new physics explanations
 - Within or outside of conventional/high scale models
- 4. Find range of model parameters that can explain excess
 - → Typically, using Monte Carlo simulations
- 5. Find other observables (collider as well as flavor/EWP/ cosmology) where the explanation can be verified/falsified
 - Note that indirect constraints (flavor/EWP/cosmology)
 typically modified by additional particles in the spectrum



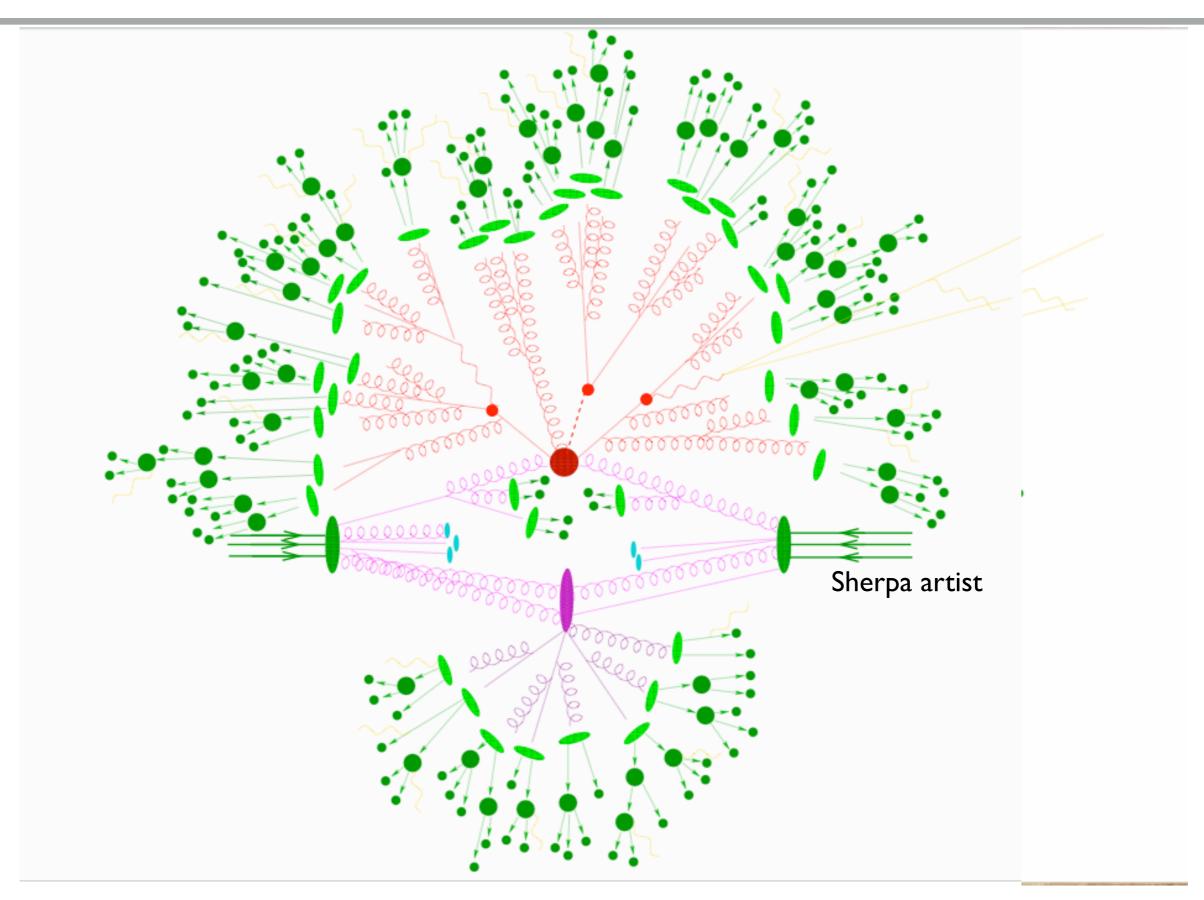
Simulation of collider events



Simulation of collider events







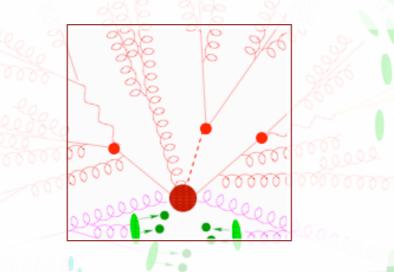




I. High-Q² Scattering

2. Parton Shower

where new physics lies



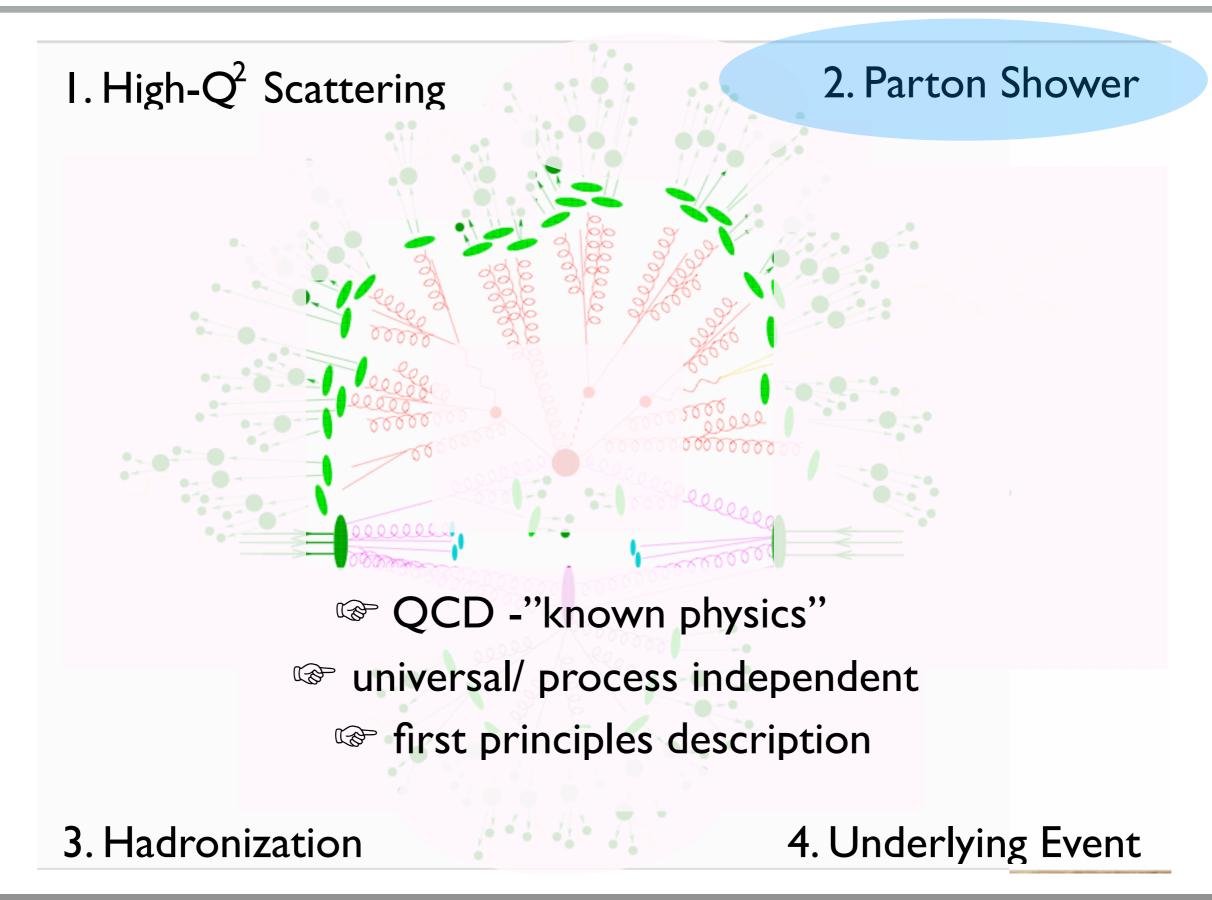
- process dependent
- first principles description
- it can be systematically improved

3. Hadronization

4. Underlying Event



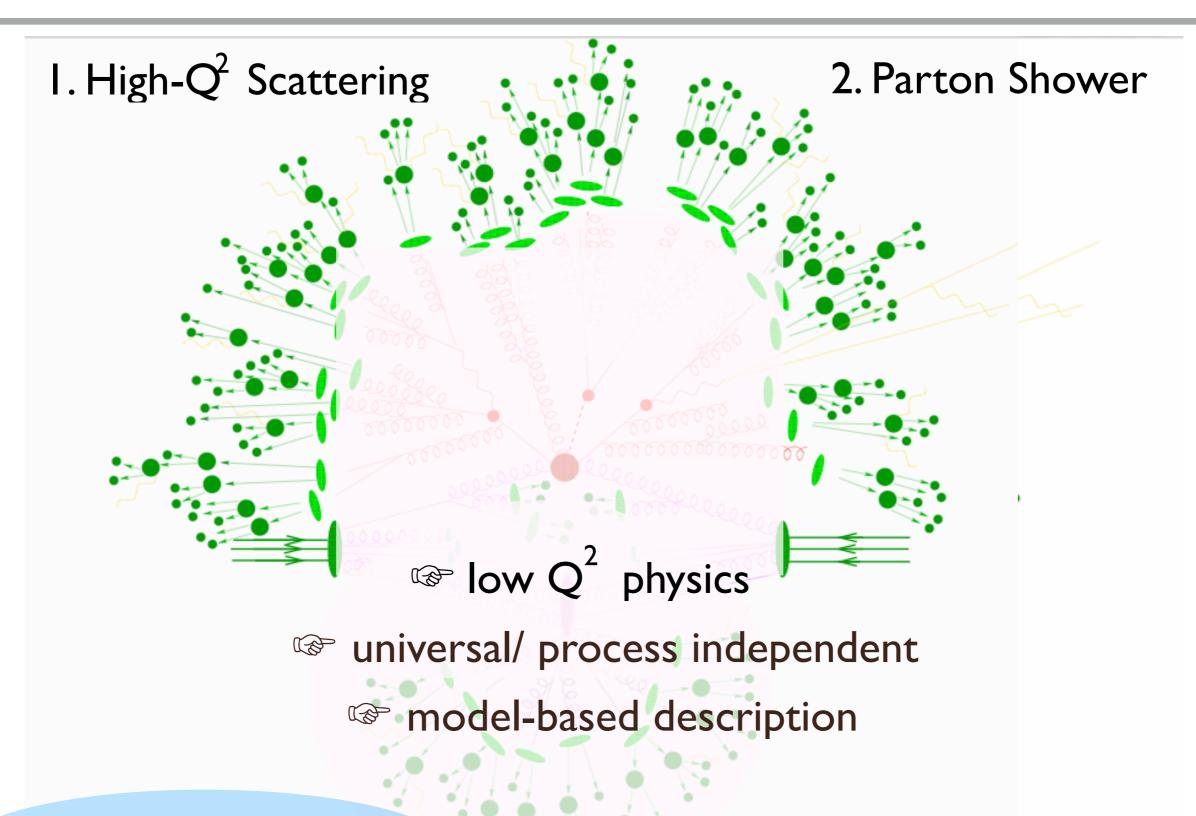




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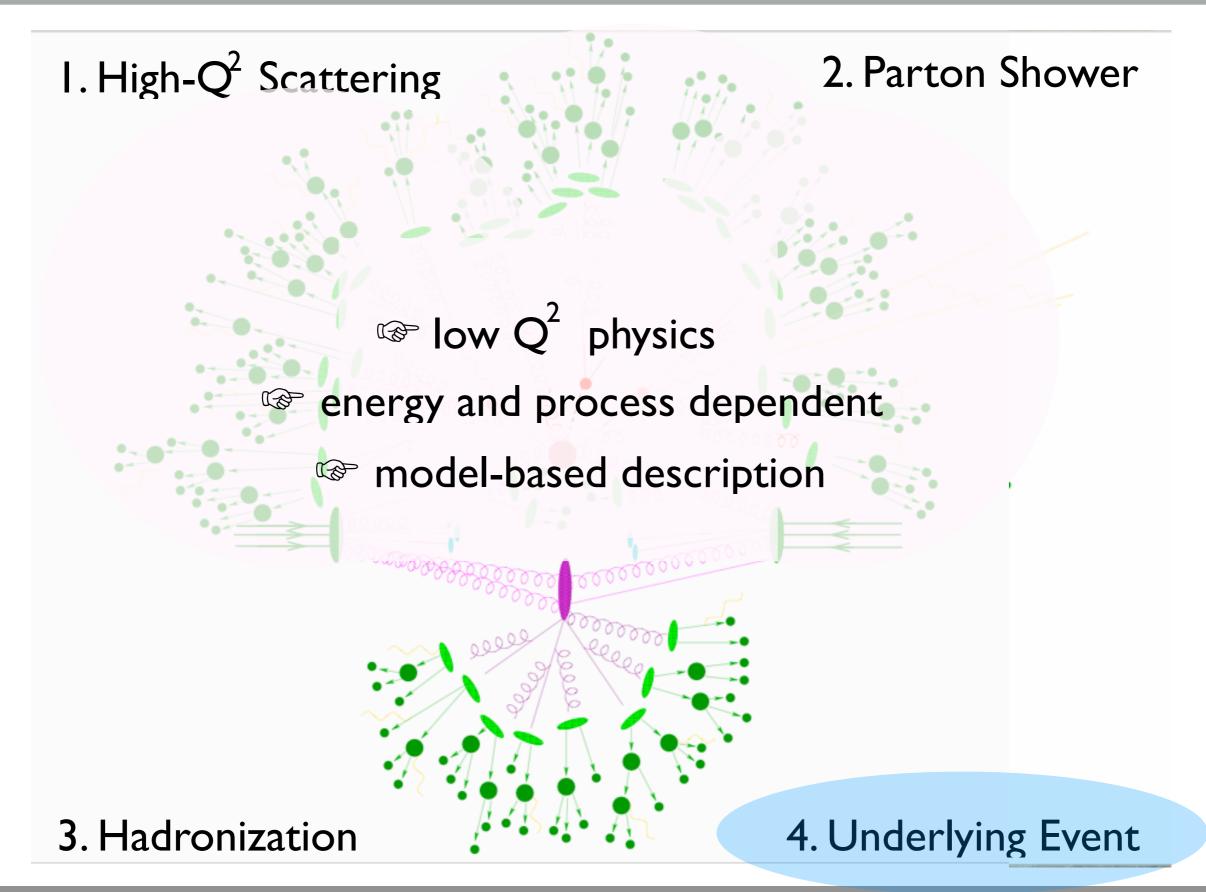


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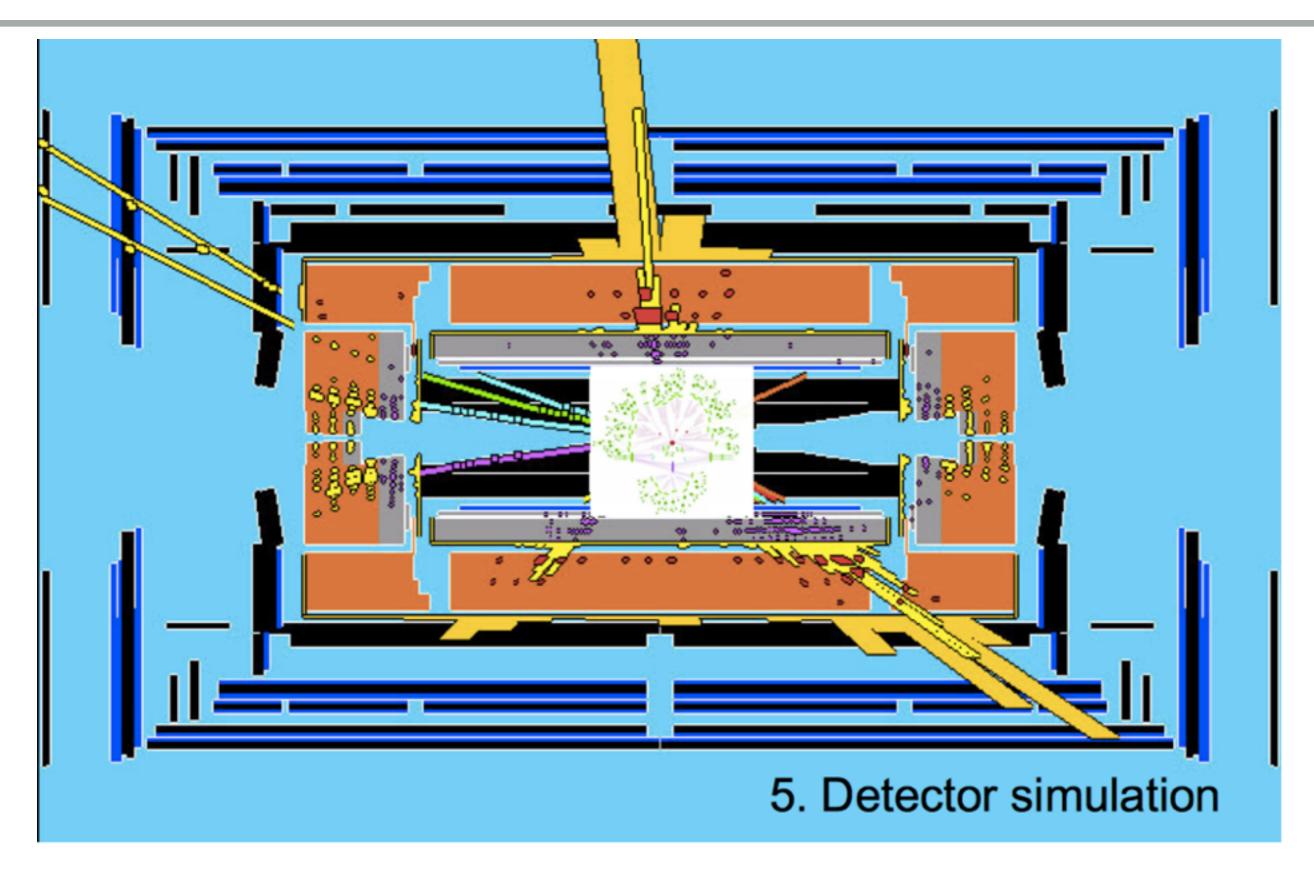














Tevatron vs. the LHC







- Tevatron: 2 TeV proton-antiproton collider
 - → Most important: q-q annihilation (85% of t t)
- LHC: 8-14 TeV proton-proton collider
 - → Most important: g-g annihilation (90% of t t)



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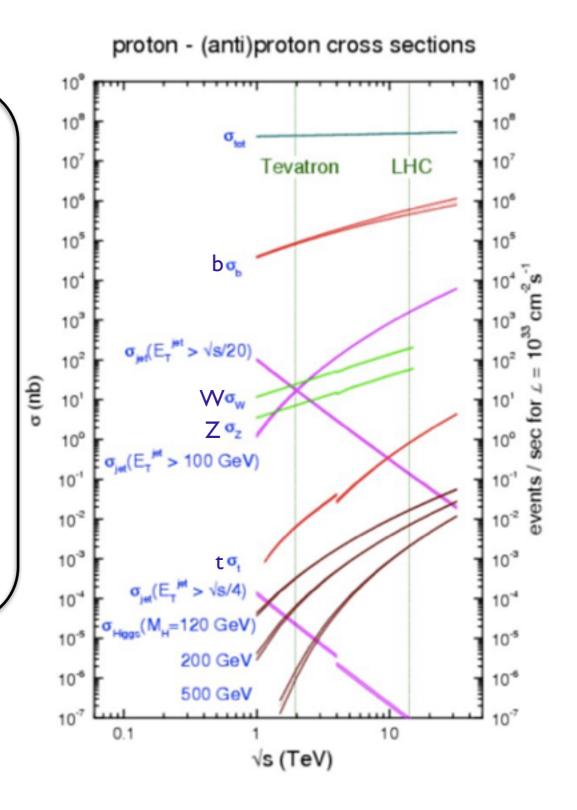
Hadron Colliders



First: Understand our processes!

Cross sections at a collider depend on:

- Coupling strength
- Coupling to what?
 (light quarks, gluons, heavy quarks, EW gauge bosons?)
- Mass
- Single production/pair production





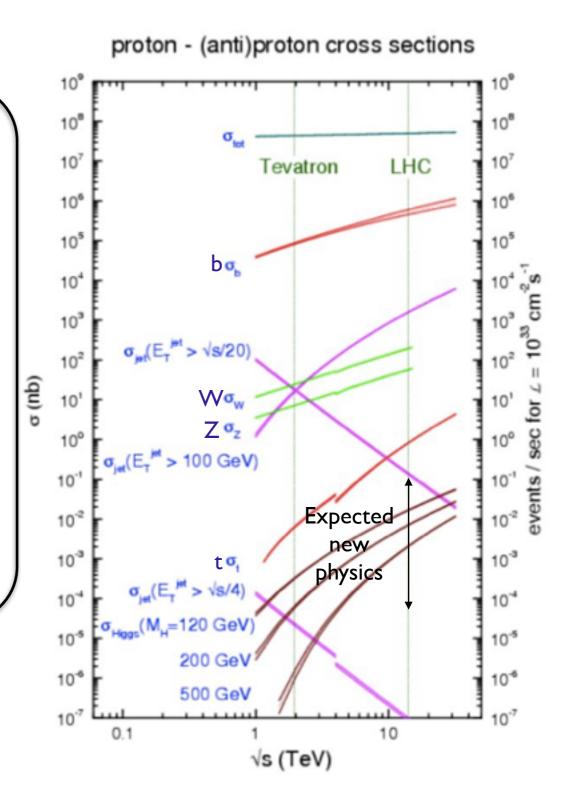
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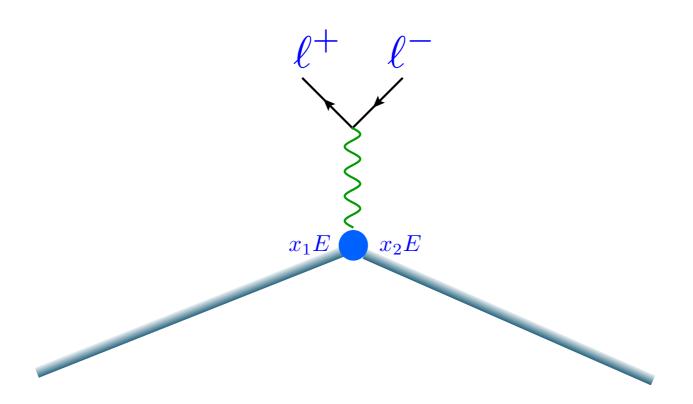
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MASTER FORMULA FOR THE LHC





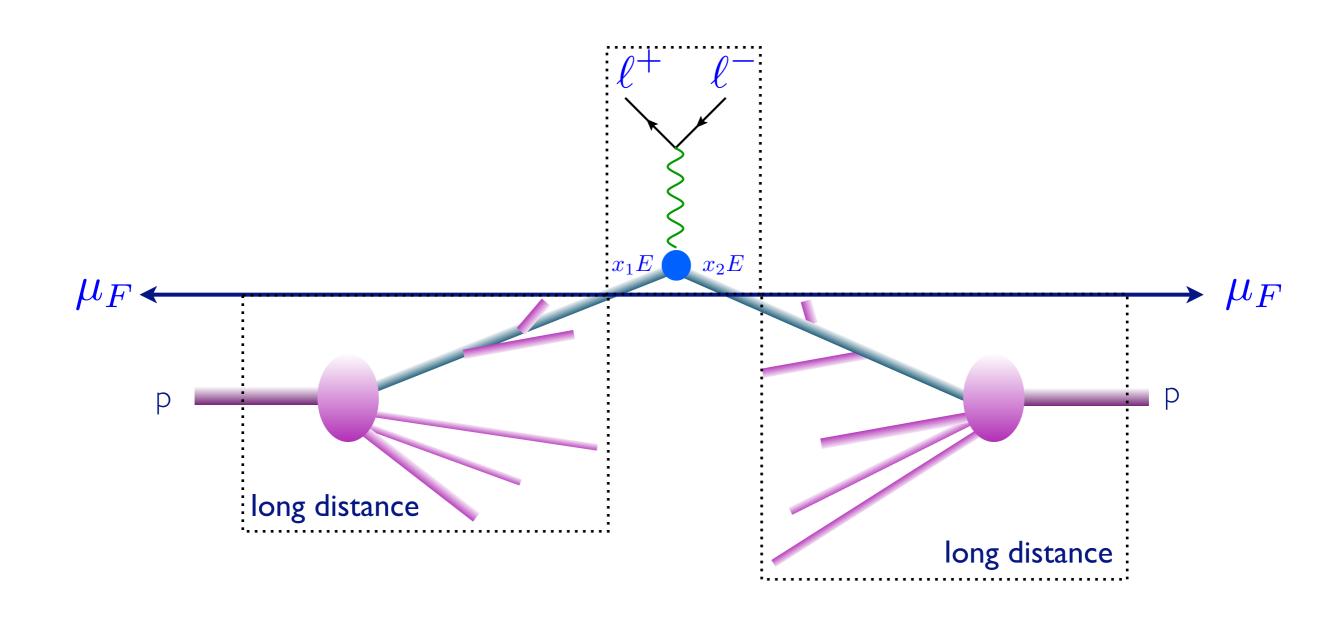
$$\hat{\sigma}_{ab\to X}(\hat{s},\mu_F,\mu_R)$$

Parton-level cross section



MASTER FORMULA FOR THE LHC





$$f_a(x_1, \mu_F) f_b(x_2, \mu_F) \hat{\sigma}_{ab \to X}(\hat{s}, \mu_F, \mu_R)$$

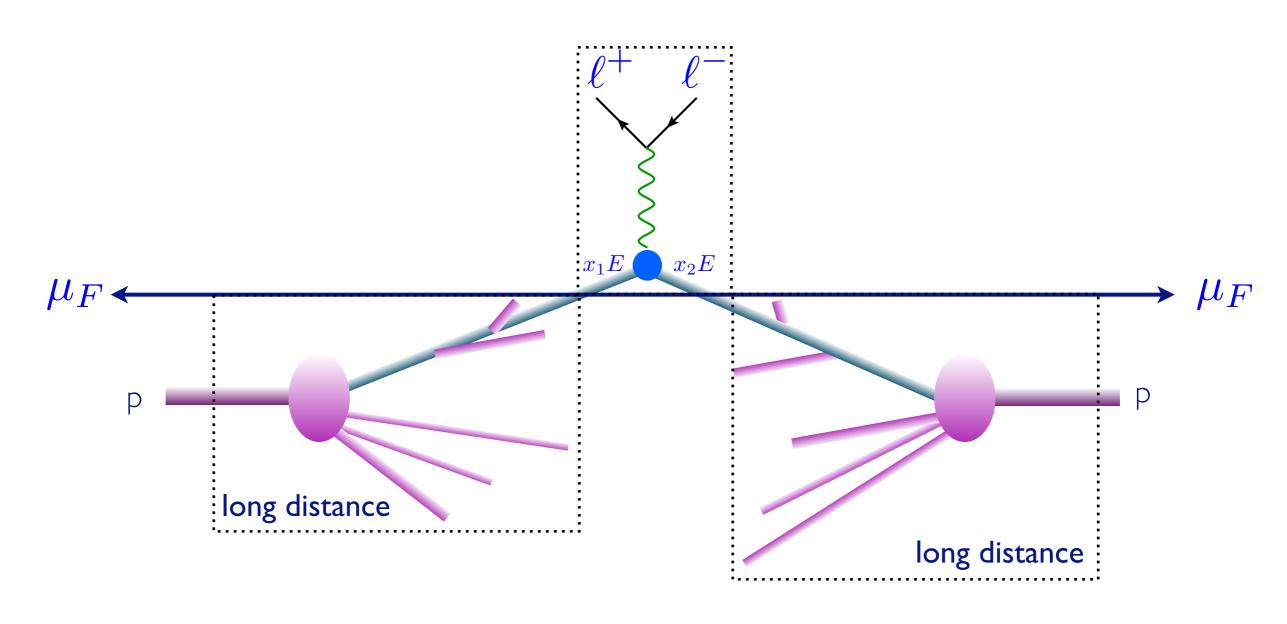
Parton density functions

Parton-level cross section



MASTER FORMULA FOR THE LHC



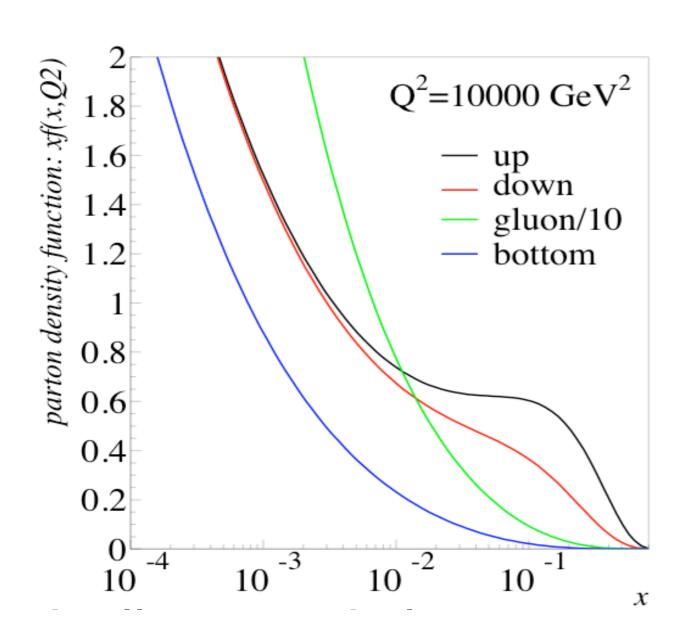


 $\sum_{a,b} \int \! dx_1 dx_2 d\Phi_{\mathrm{FS}} \, f_a(x_1,\mu_F) f_b(x_2,\mu_F) \, \hat{\sigma}_{ab \to X}(\hat{s},\mu_F,\mu_R)$ Phase-space Parton density Parton-level cross integral functions section

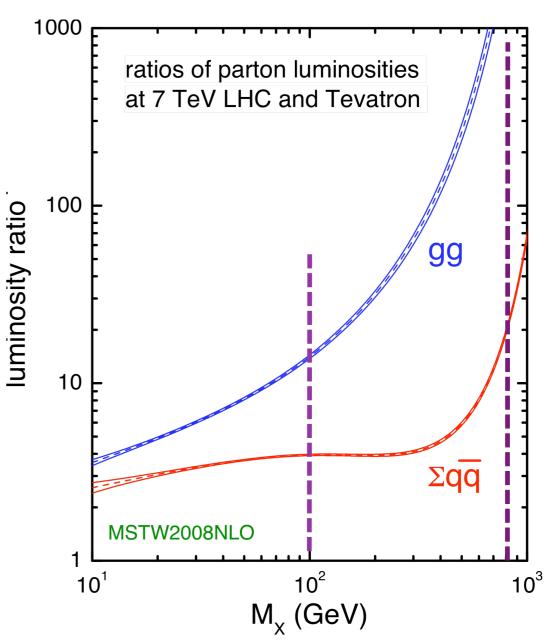


Parton densities





At small x (small \$), gluon domination. At large x valence quarks



LHC formidable at large mass – For low mass, Tevatron backgrounds smaller





The Matrix Element

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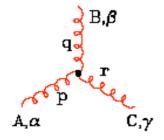




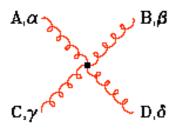
$$\delta^{AB} \left[-g^{\alpha\beta} + (1-\lambda) \frac{p^{\alpha}p^{\beta}}{p^{2} + i\epsilon} \right] \frac{i}{p^{2} + i\epsilon}$$

$$\delta^{AB} \frac{i}{(p^2+i\epsilon)}$$

$$\delta^{ab} \frac{i}{(p'-m+i\epsilon)_{ti}}$$



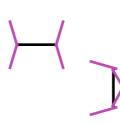
$$-g \ f^{ABC}[(p-q)^{\gamma}g^{\alpha\beta}+(q-r)^{\alpha}g^{\beta\gamma}+(r-p)^{\beta}g^{\gamma\alpha}]$$
(all momenta incoming)



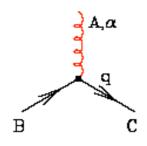
$$-ig^{2} f^{XAC} f^{XBD} \left[g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\delta} g^{\beta\gamma} \right]$$

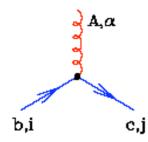
$$-ig^{2} f^{XAD} f^{XBC} \left[g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\gamma} g^{\beta\delta} \right]$$

$$-ig^{2} f^{XAB} f^{XCD} \left[g^{\alpha\gamma} g^{\beta\delta} - g^{\alpha\delta} g^{\beta\gamma} \right]$$





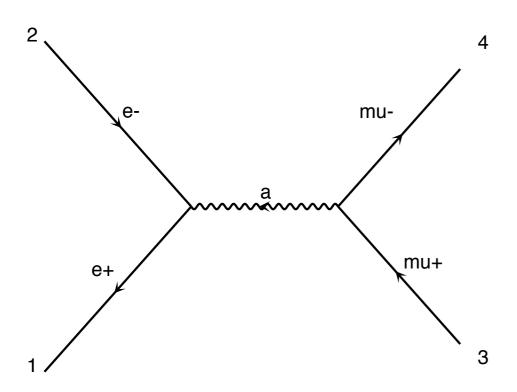




$$-ig\ (t^{A})_{ab}\ (\gamma^{\alpha})_{ji}$$

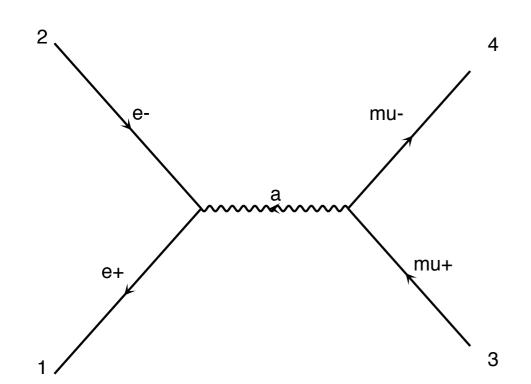








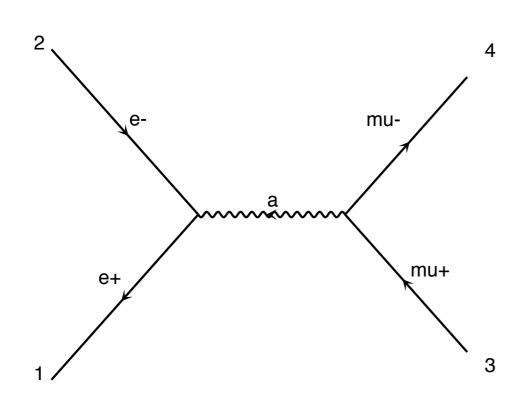




$$\mathcal{M} = e^2(\bar{u}\gamma^{\mu}v) \frac{g_{\mu\nu}}{q^2} (\bar{u}\gamma^{\nu}v)$$



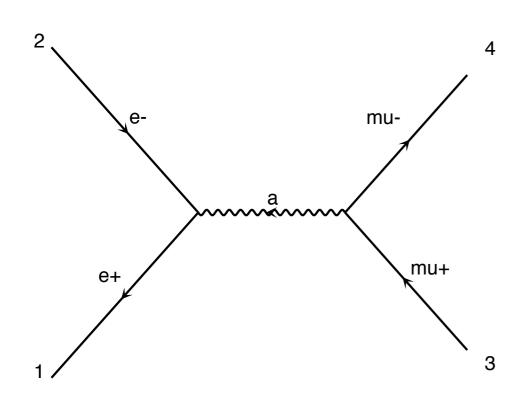




$$\mathcal{M} = e^2(\bar{u}\gamma^{\mu}v) \frac{g_{\mu\nu}}{q^2} (\bar{u}\gamma^{\nu}v)$$
$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$







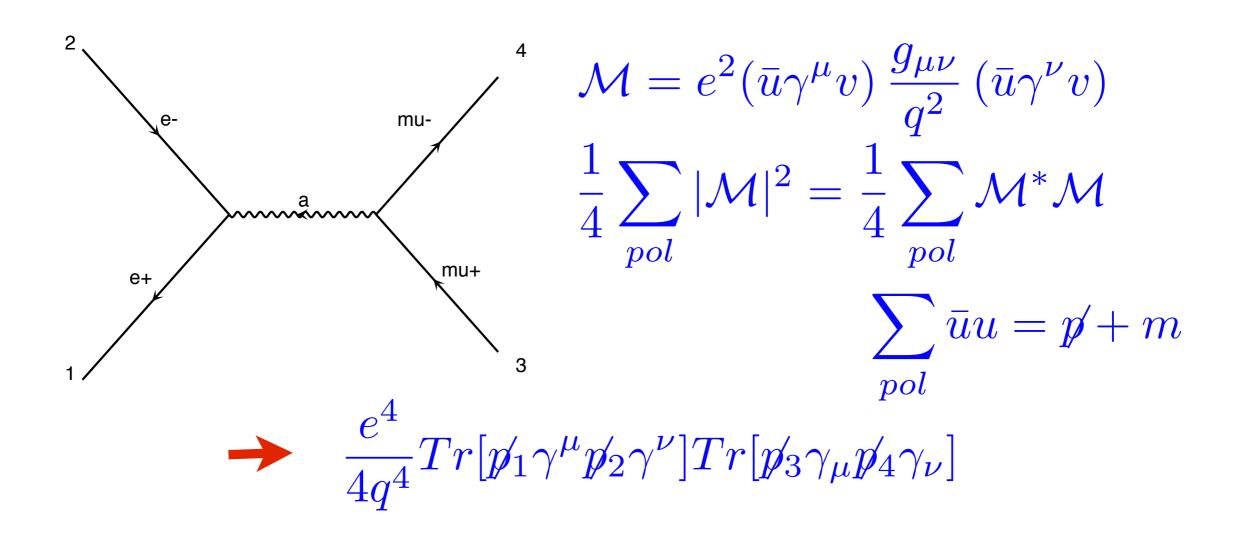
$$\mathcal{M} = e^2(\bar{u}\gamma^{\mu}v) \frac{g_{\mu\nu}}{q^2} (\bar{u}\gamma^{\nu}v)$$

$$\frac{1}{4} \sum_{pol} |\mathcal{M}|^2 = \frac{1}{4} \sum_{pol} \mathcal{M}^* \mathcal{M}$$

$$\sum_{pol} \bar{u}u = p + m$$



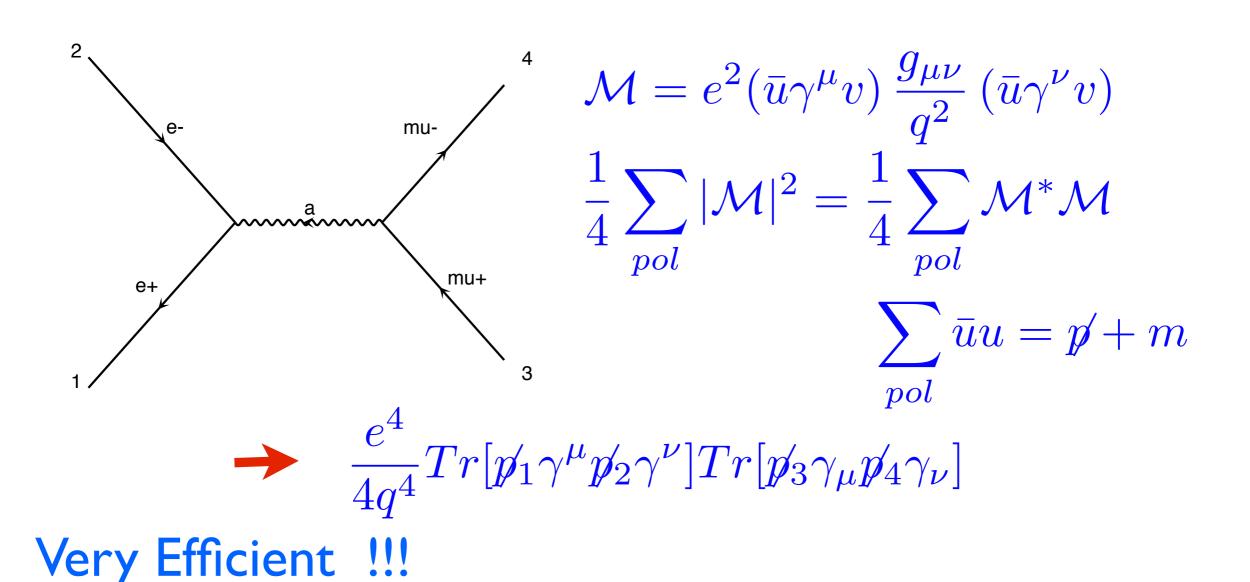






Matrix Element

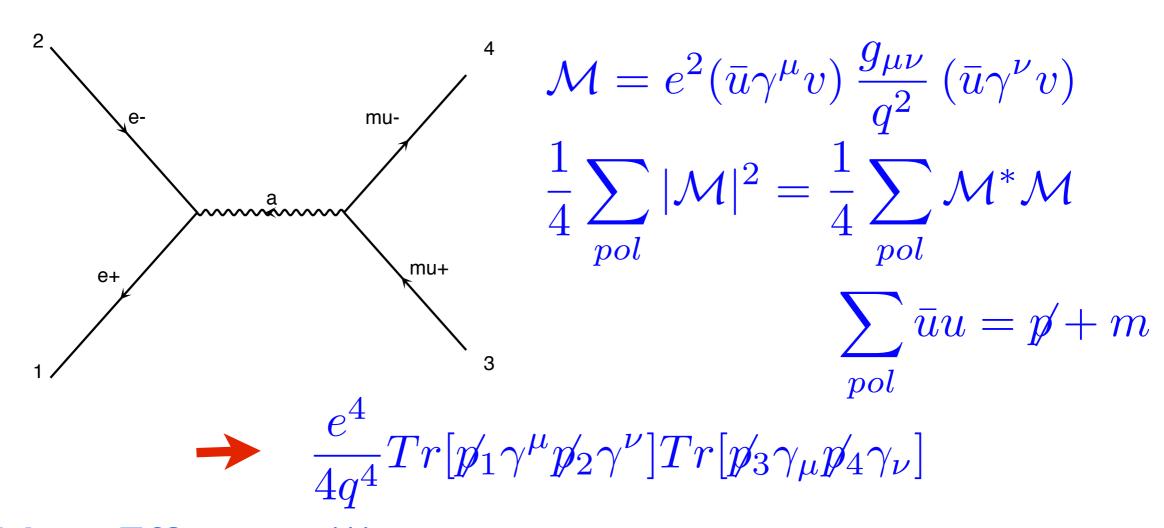






Matrix Element





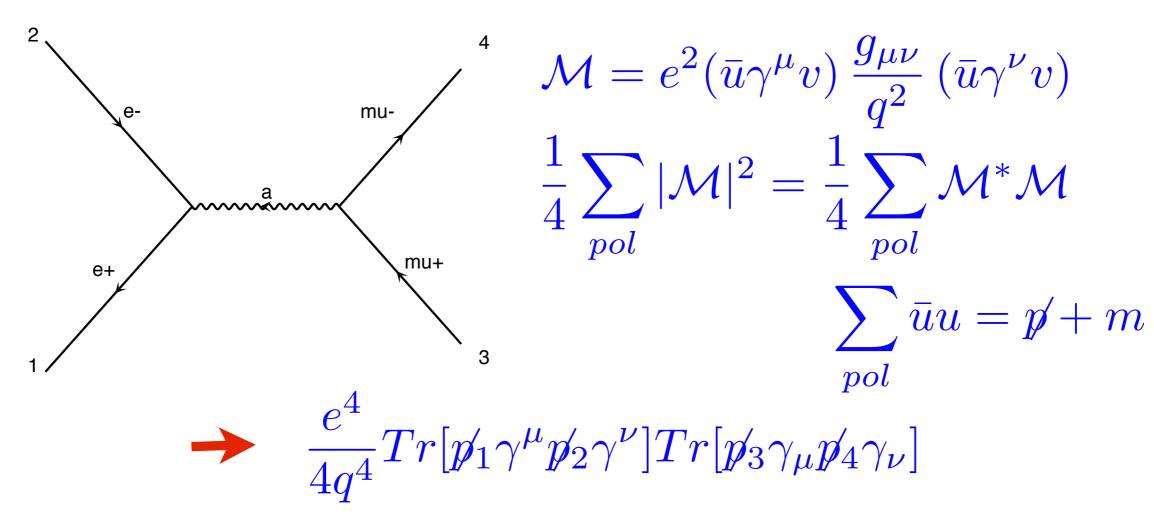
Very Efficient !!! But the number of terms rises as N^2

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Matrix Element





Very Efficient !!!

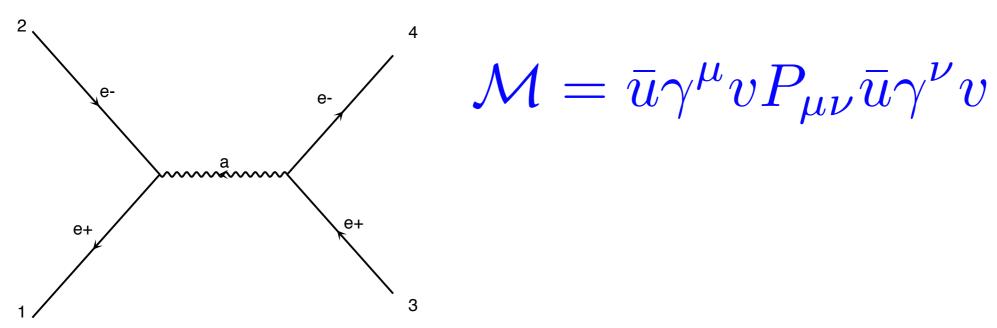
But the number of terms rises as N^2

Only for $2 \rightarrow 2$ and $2 \rightarrow 3$





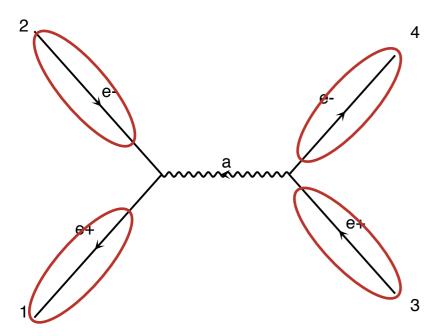
- Idea: Evaluate **M** for fixed helicity of external particles
 - → Multiply \mathcal{M} with \mathcal{M}^* -> $|\mathcal{M}|^2$
 - → Loop on Helicity and sum the results







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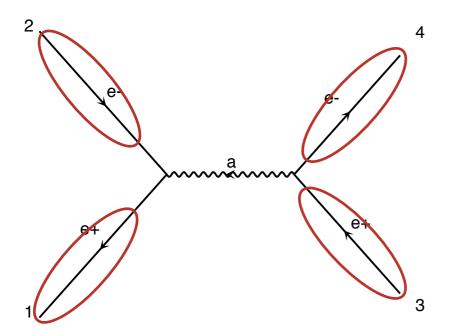
$$\mathcal{M} = \overline{\overline{u}} \gamma^{\mu} v P_{\mu\nu} \overline{\overline{u}} \gamma^{\nu} v$$

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- Idea: Evaluate *M* for fixed helicity of external particles
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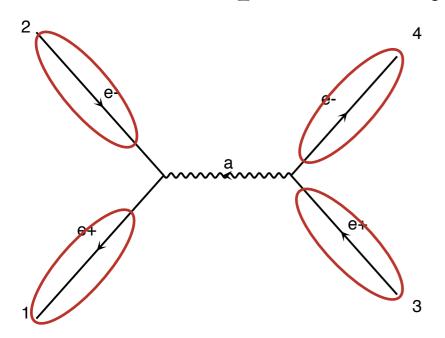
$$\mathcal{M} = (\bar{u})^{\mu} (v) P_{\mu\nu} (\bar{u})^{\nu} (v)$$

```
CALL OXXXXX(P(0,1),ZERO,NHEL(1),-1*IC(1),W(1,1))
CALL IXXXXX(P(0,2),ZERO,NHEL(2),+1*IC(2),W(1,2))
CALL IXXXXX(P(0,3),ZERO,NHEL(3),-1*IC(3),W(1,3))
CALL OXXXXX(P(0,4),ZERO,NHEL(4),+1*IC(4),W(1,4))
```





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$$\mathcal{M} = (\bar{u})^{\mu} (v) P_{\mu\nu} (\bar{u})^{\nu} (v)$$

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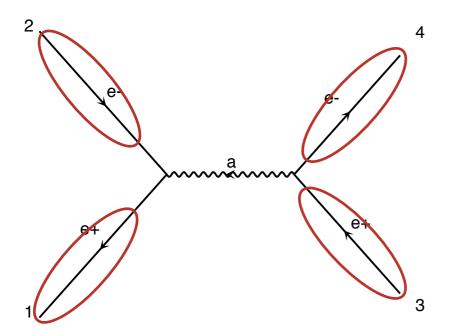
Input: momenta, mass, helicity

Ouput: Wavefunction (given by an analytical formula)





- Idea: Evaluate *M* for fixed helicity of external particles
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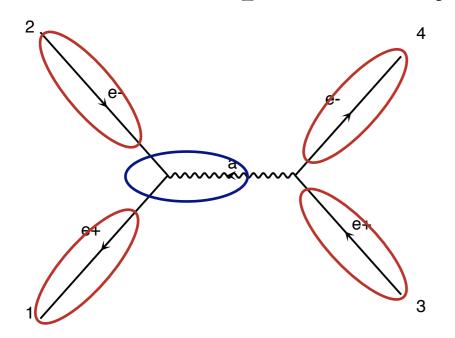
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Numbers for given helicity and momenta Calculate propagator wavefunctions

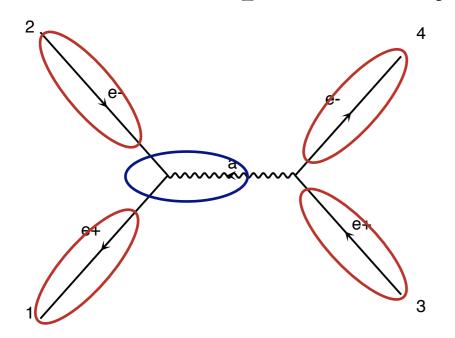
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CALL OXXXXX(P(0,4), ZERO, NHEL(4), +1*IC(4), W(1,4))

CALL JIOXXX(W(1,2), W(1,1), GAL, ZERO, ZERO, W(1,5))
```





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 - → Multiply \mathcal{M} with \mathcal{M}^* -> $|\mathcal{M}|^2$
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```
\mathcal{M} = \overline{\overline{u}} \gamma^{\mu} \underline{v} P_{\mu\nu} \overline{\overline{u}} \gamma^{\nu} \underline{v}
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Numbers for given helicity and momenta Calculate propagator wavefunctions

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CALL OXXXXX(P(0,1),ZERO,NHEL(1),-1*IC(1),W(1,1))
CALL IXXXXX(P(0,2),ZERO,NHEL(2),+1*IC(2),W(1,2))
```

Input: Wavefunctions, mass, width, coupling

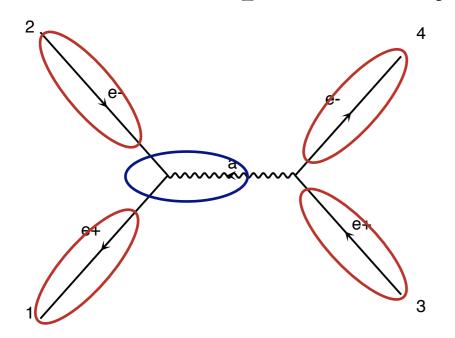
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CALL JIOXXX (W(1,2), W(1,1), GAL, ZERO, ZERO, W(1,5))
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Ouput: Wavefunction (given by an analytical formula)





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Numbers for given helicity and momenta Calculate propagator wavefunctions

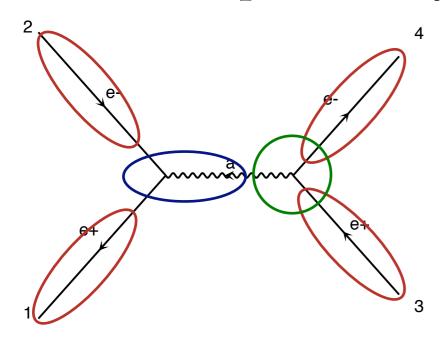
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Calculate propagator wavefunctions
Finally evaluate amplitude (c-number)

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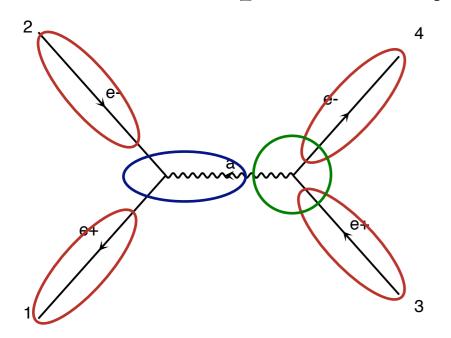
CALL JIOXXX(W(1,2),W(1,1),GAL,ZERO,ZERO,W(1,5))

CALL IOVXXX(W(1,3),W(1,4),W(1,5),GAL,AMP(1))
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CALL OXXXXX(P(0,4), ZERO, NHEL(4), +1*IC(4), W(1,4))
```

Input: Wavefunctions, coupling

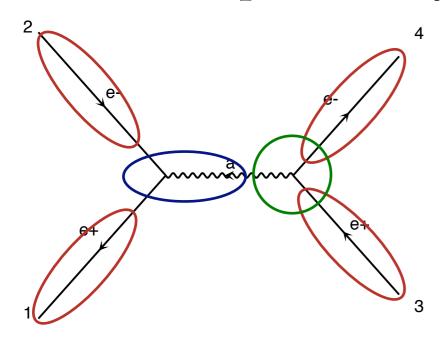
CALL IOVXXX(W(1,3),W(1,4),W(1,5),GAL,AMP(1))

Ouput: Amplitude





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CALL OXXXXX(P(0,4),ZERO,NHEL(4),+1*IC(4),W(1,4))

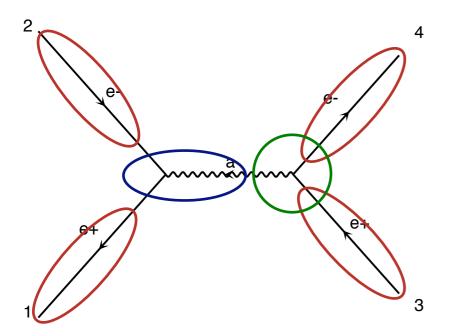
CALL JIOXXX(W(1,2),W(1,1),GAL,ZERO,ZERO,W(1,5))

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- Idea: Evaluate *M* for fixed helicity of external particles
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 $\mathcal{M} = \overline{\overline{u}} \gamma^{\mu} v P_{\mu\nu} \overline{u} \gamma^{\nu} v$

Numbers for given helicity and momenta

Calculate propagator wavefunctions
Finally evaluate amplitude (c-number)

Helicity amplitude calls written by MadGraph

```
CALL OXXXXX(P(0,1), ZERO, NHEL(1), -1*IC(1), W(1,1))
CALL IXXXXX(P(0,2), ZERO, NHEL(2), +1*IC(2), W(1,2))
CALL IXXXXX(P(0,3), ZERO, NHEL(3), -1*IC(3), W(1,3))
CALL OXXXXX(P(0,4), ZERO, NHEL(4), +1*IC(4), W(1,4))

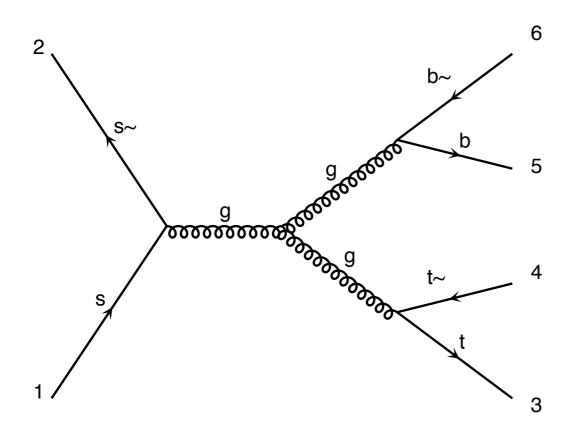
CALL JIOXXX(W(1,2), W(1,1), GAL, ZERO, ZERO, W(1,5))

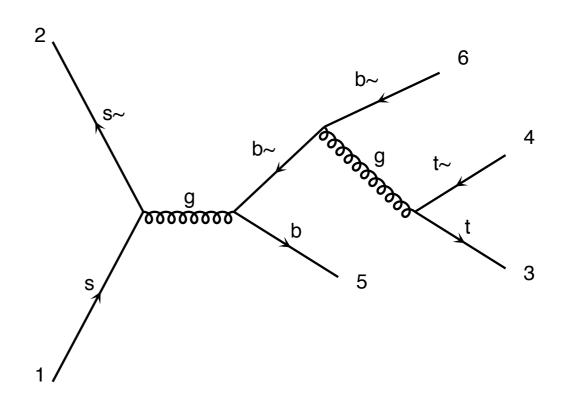
CALL IOVXXX(W(1,3), W(1,4), W(1,5), GAL, AMP(1))
```











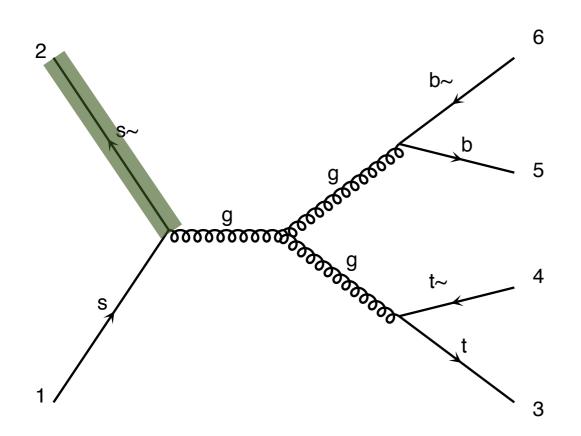
Number of routines: 0

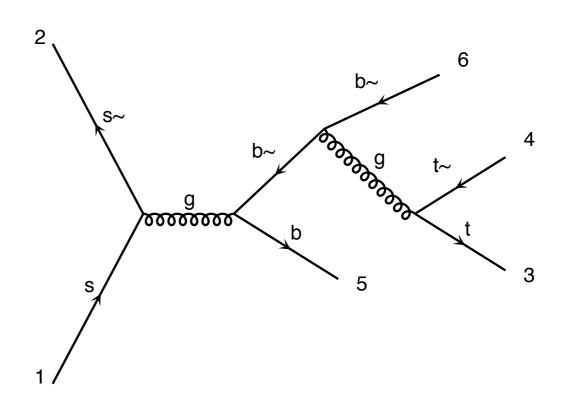
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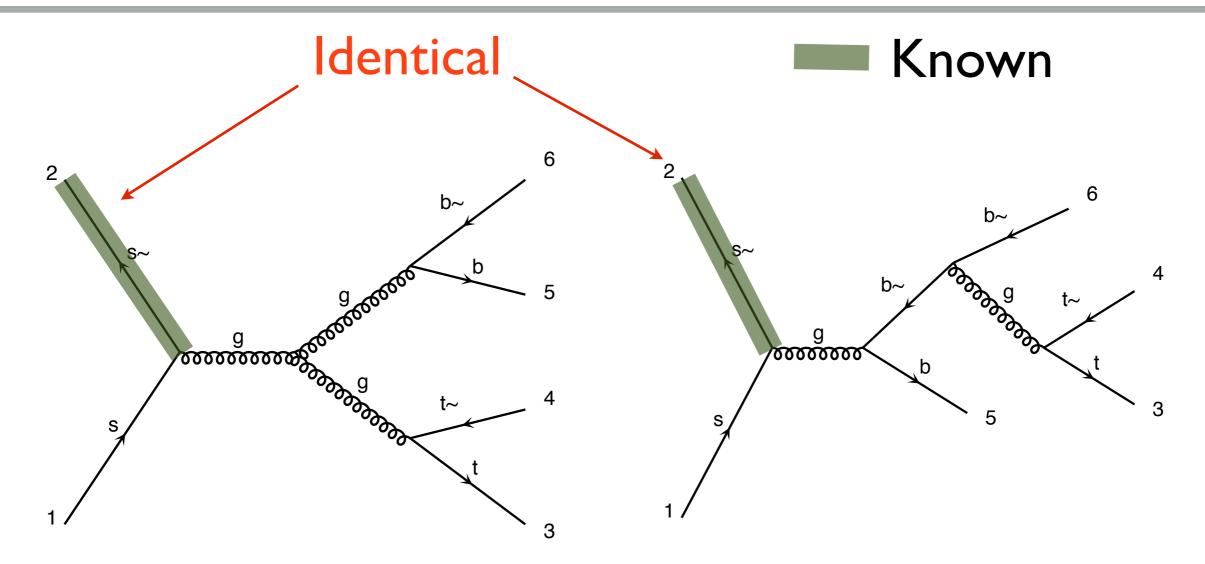


Number of routines: I

Number of routines: 0







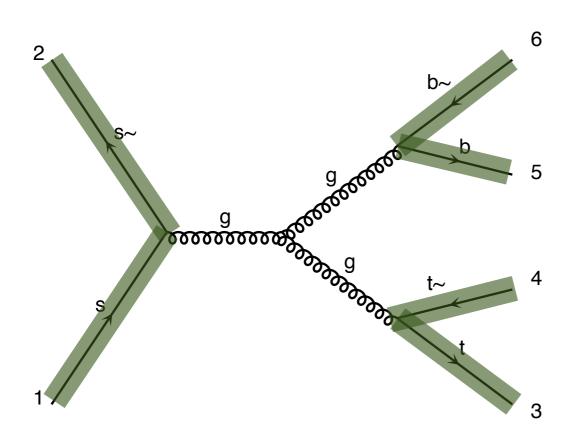
Number of routines: I

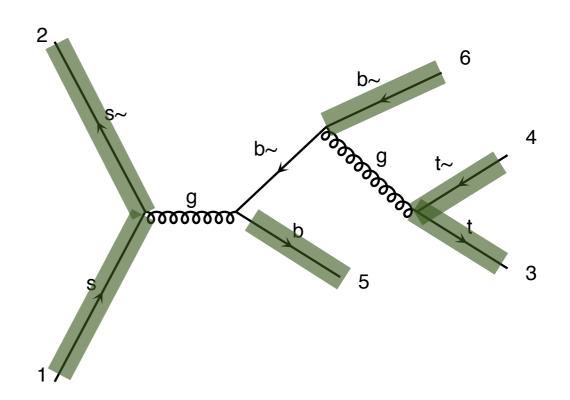
Number of routines: |











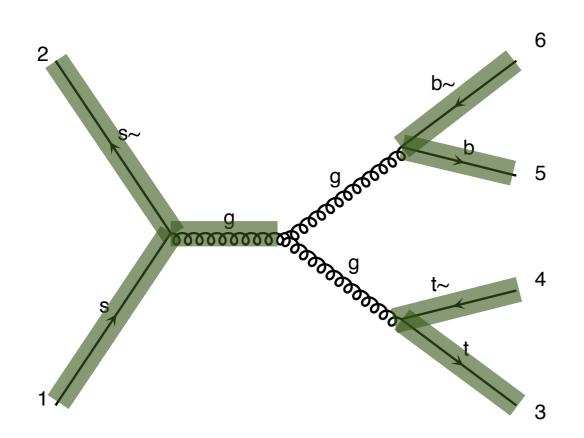
Number of routines: 6

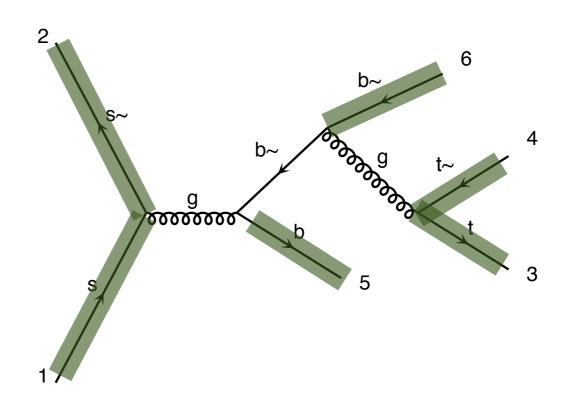
Number of routines: 6









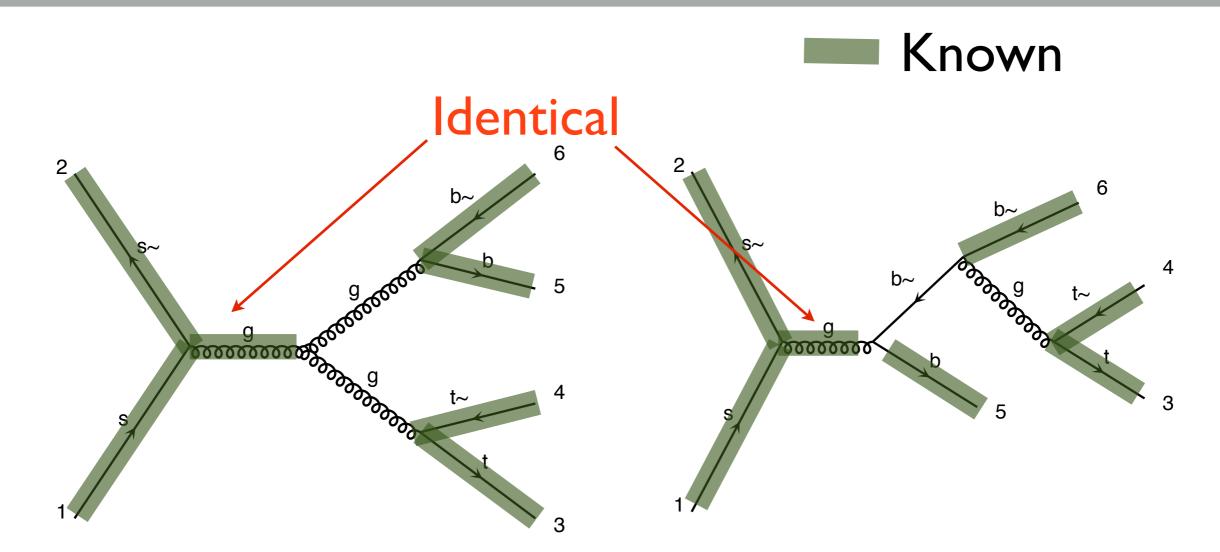


Number of routines: 7

Number of routines: 6





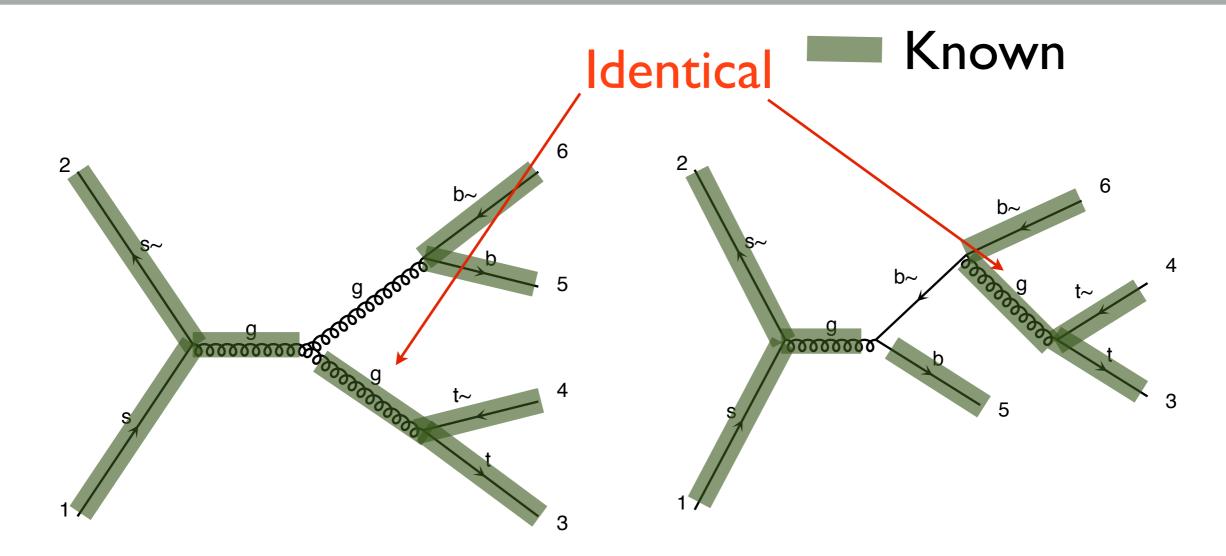


Number of routines: 7

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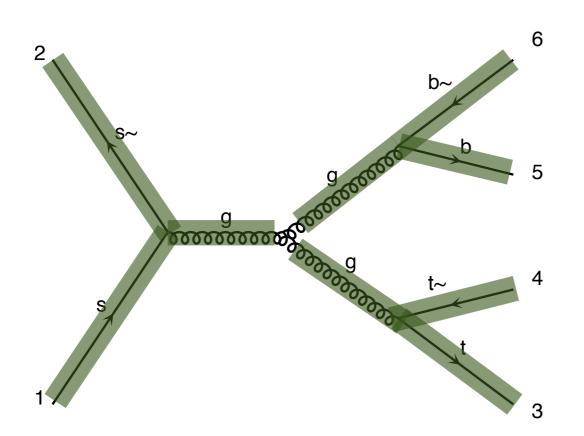
Number of routines: 8

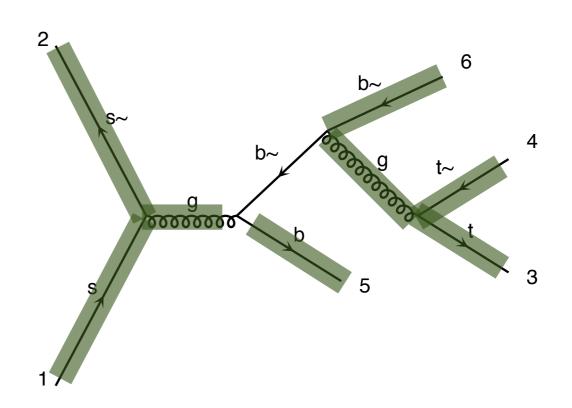
Number of routines: 8











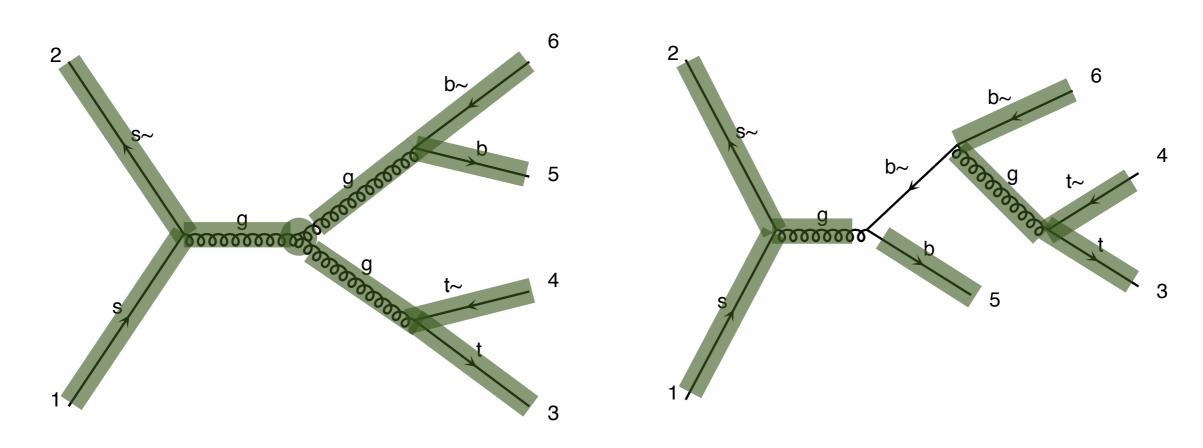
Number of routines: 9

Number of routines: 8







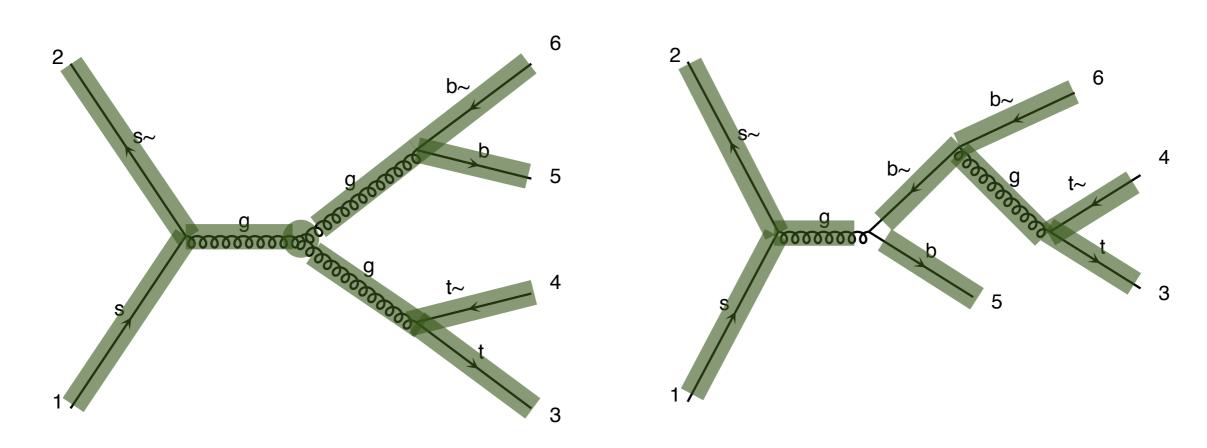


Number of routines: 10 Number of routines: 8







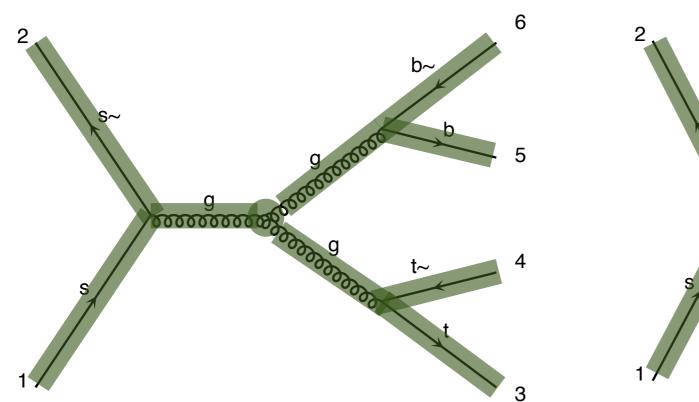


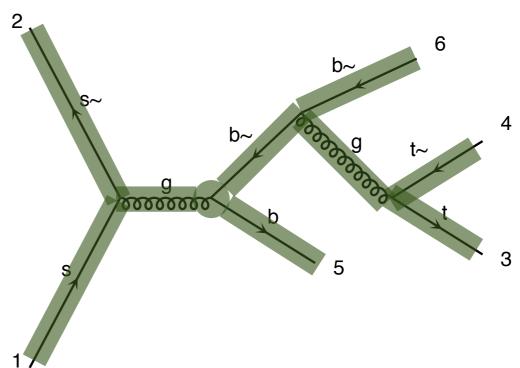
Number of routines: 10 Number of routines: 9











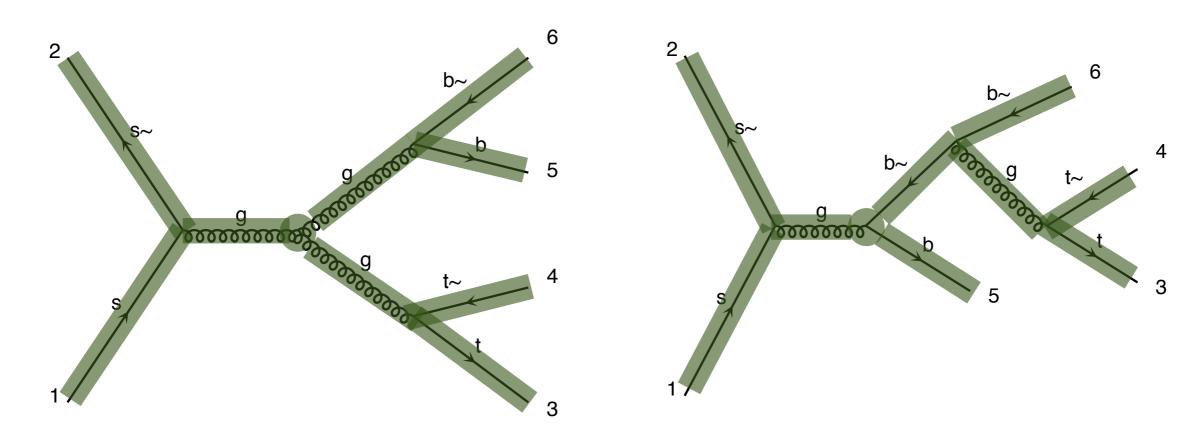
Number of routines: 10

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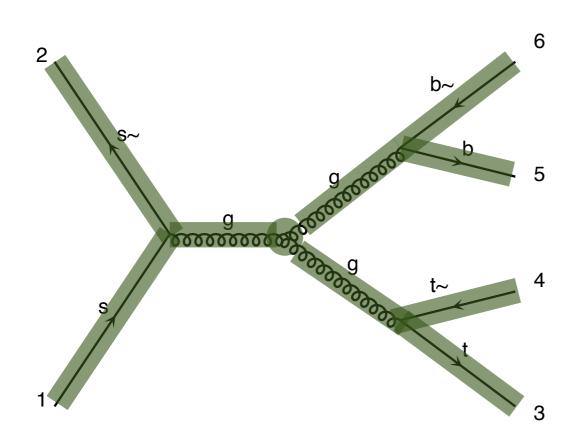


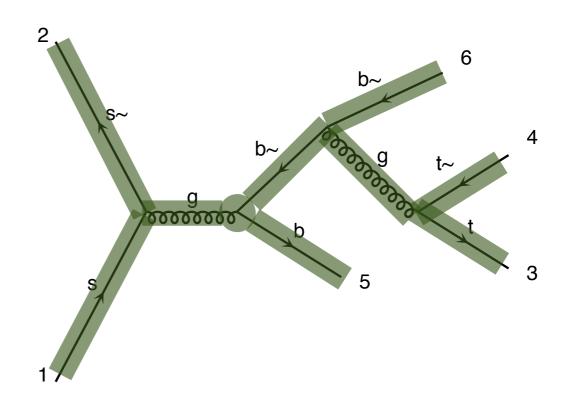
Number of routines: 10 Number of routines: 10 2(N+1) 2(N+1)











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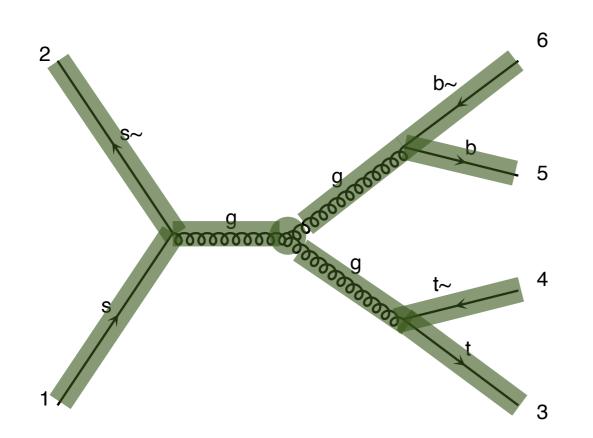
Number of routines for both: 12

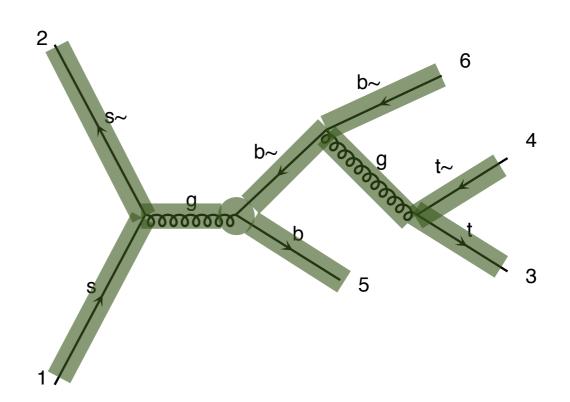
 $N!*2(N+1) \longrightarrow N!$











Number of routines: 10 Number of routines: 10 2(N+1)

2(N+1)

$$N!*2(N+1) \longrightarrow N!$$
 in progress 2^N



Helicity amplitudes



• Thanks to new diagram generation algorithm, wf recycling much more efficient in MG5 than MG4

Process	Amplitudes	Wavefunctions		Run time		no recycling
		MG 4	MG 5	MG 4	MG 5	
$u\bar{u} \rightarrow e^+e^-$	2	6	6	$< 6 \mu s$	$< 6 \mu s$	
$u\bar{u} \rightarrow e^+e^-e^+e^-$	48	62	32	$0.22~\mathrm{ms}$	0.14 ms	
$u\bar{u} \to e^+e^-e^+e^-e^+e^-$	3474	3194	301	46.5 ms	19.0 ms	300,000
$u\bar{u} \to d\bar{d}$	1	5	5	$< 4\mu s$	$< 4 \mu s$	
$u\bar{u} o d\bar{d}g$	5	11	11	$27 \mu s$	$27 \mu s$	
$u \bar{u} o d \bar{d} g g$	38	47	29	$0.42~\mathrm{ms}$	0.31 ms	
$u\bar{u} o d\bar{d}ggg$	393	355	122	$10.8 \; \mathrm{ms}$	6.75 ms	
$u\bar{u} \rightarrow u\bar{u}gg$	76	84	40	1.24 ms	0.80 ms	
$u\bar{u} \rightarrow u\bar{u}ggg$	786	682	174	35.7 ms	17.2 ms	
$u\bar{u} o d\bar{d}d\bar{d}$	14	28	19	$84~\mu s$	$83 \mu s$	
$u\bar{u} o d\bar{d}d\bar{d}g$	132	178	65	$1.88~\mathrm{ms}$	1.15 ms	
$u\bar{u} o d\bar{d}d\bar{d}gg$	1590	1782	286	141 ms	34.4 ms	
$u\bar{u} \rightarrow d\bar{d}d\bar{d}d\bar{d}$	612	758	141	42.5 ms	6.6 ms	5500

Time for matrix element evaluation on a Sony Vaio TZ laptop



HELAS



[Murayama, Watanabe, Hagiwara]

• Original HELicity Amplitude Subroutine library



HELAS



[Murayama, Watanabe, Hagiwara]

- Original HELicity Amplitude Subroutine library
- One routine per Lorentz structure
 - → MSSM [cho, al] hep-ph/0601063 (2006)
 - → HEFT [Frederix] (2007)
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Chiral Perturbation

Effective Field Theory

Full HEFT

Chromo-magnetic operator

BNV Model

NMSSM

Black Holes



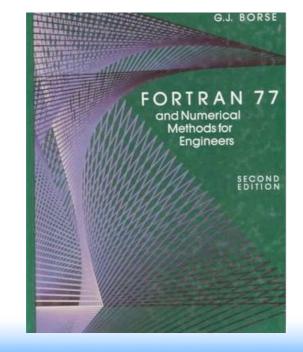


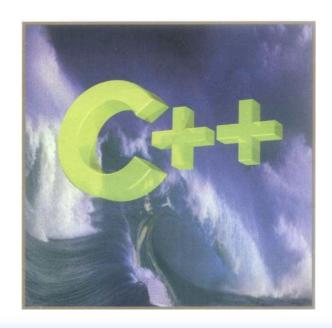
ALOHA



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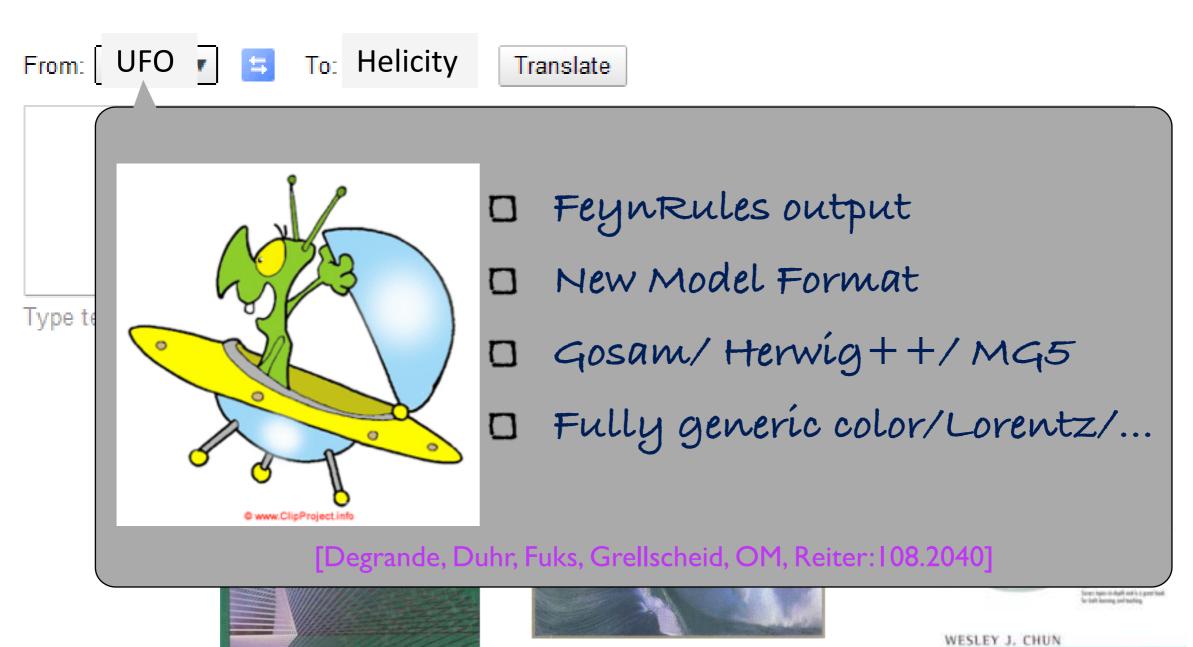






ALOHA





Brussels October 2010 Tim Stelzer



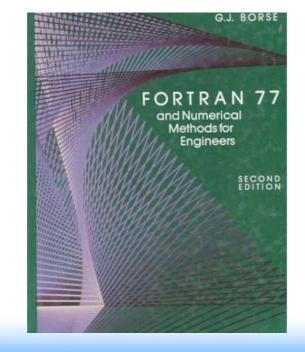


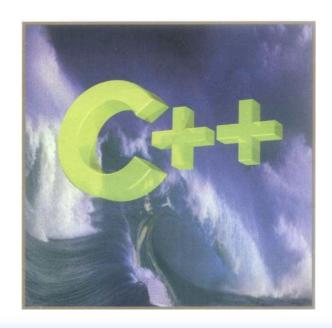
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ALOHA



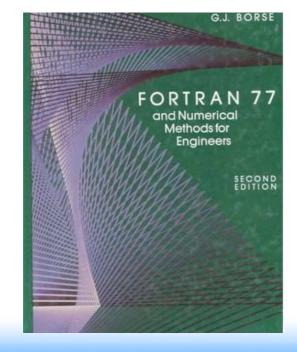
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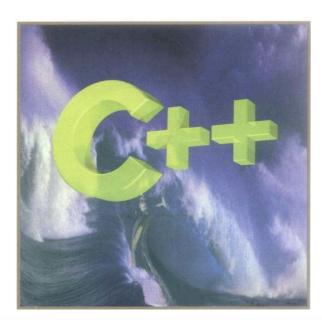
To: Helicity

Translate

Basically Any BSM Model should be working in MG5 out of the box!

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Monte Carlo Integration and Generation

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Monte Carlo Integration



Calculations of cross section or decay widths involve integrations over high-dimension phase space of very peaked functions:



Monte Carlo Integration ** Durham University



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$$\sigma = \frac{1}{2s} \int |\mathcal{M}|^2 d\Phi(n)$$



Monte Carlo Integration Turbum



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$$Dim[\Phi(n)] \sim 3n$$



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General and flexible method is needed





$$I = \int_{x_1}^{x_2} f(x) dx$$

$$I_N = (x_2 - x_1) \frac{1}{N} \sum_{i=1}^{N} f(x)$$

$$V = (x_2 - x_1) \int_{x_1}^{x_2} [f(x)]^2 dx - I^2 \qquad V_N = (x_2 - x_1)^2 \frac{1}{N} \sum_{i=1}^N [f(x)]^2 - I_N^2$$

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$$I = I_N \pm \sqrt{V_N/N}$$

32 NCTS 2014





$$I = \int_{x_1}^{x_2} f(x) dx \qquad \qquad \blacksquare \qquad I_N = (x_2 - x_1) \frac{1}{N} \sum_{i=1}^{N} f(x)$$

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- Convergence is slow but it can be easily estimated
- Error does not depend on # of dimensions!







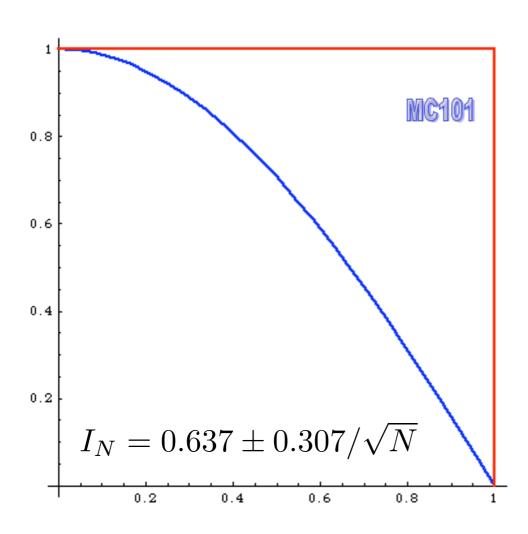
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- \bigcirc Optimal/Ideal case: $f(x)=C \Rightarrow V_N=0$



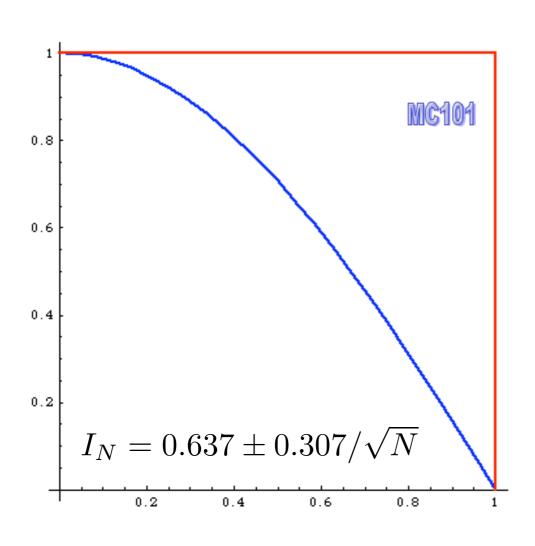




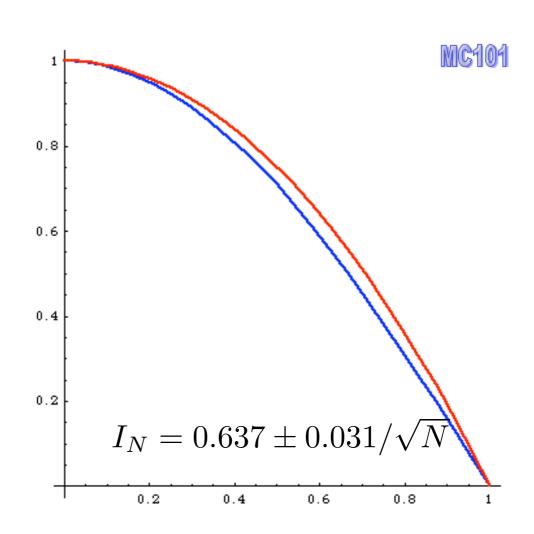
$$I = \int_0^1 dx \cos \frac{\pi}{2} x$$







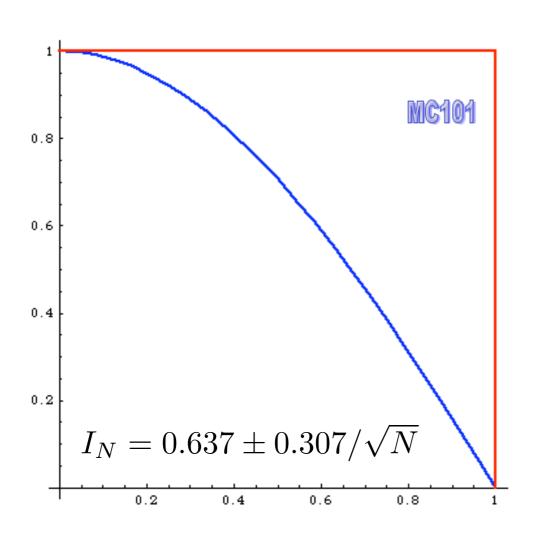
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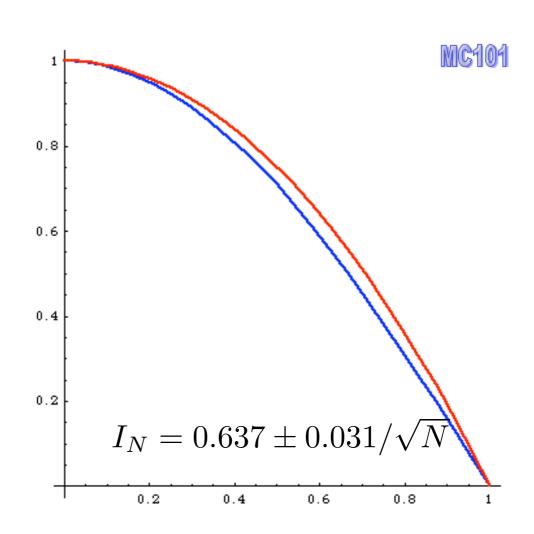
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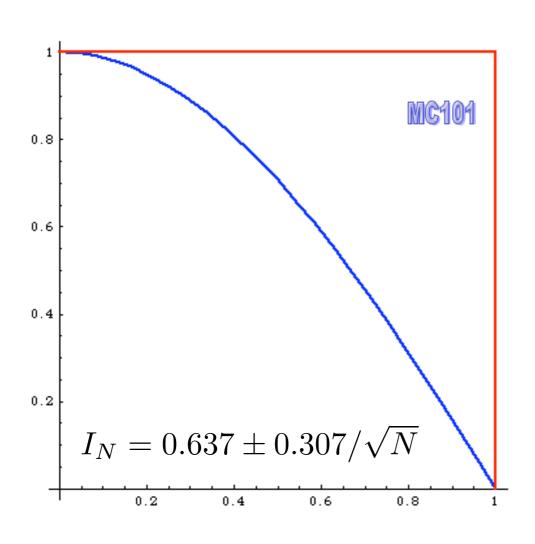
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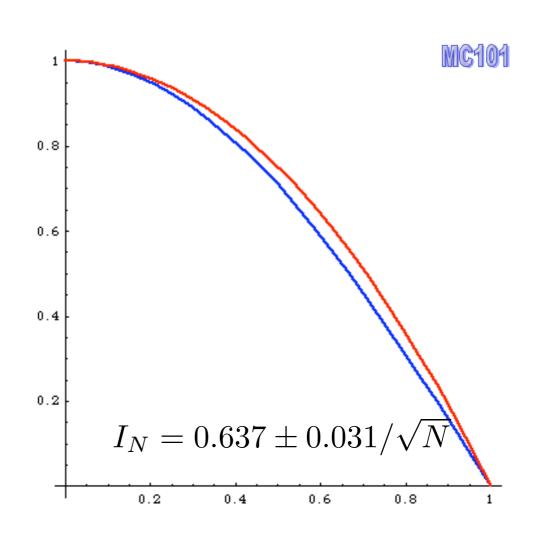
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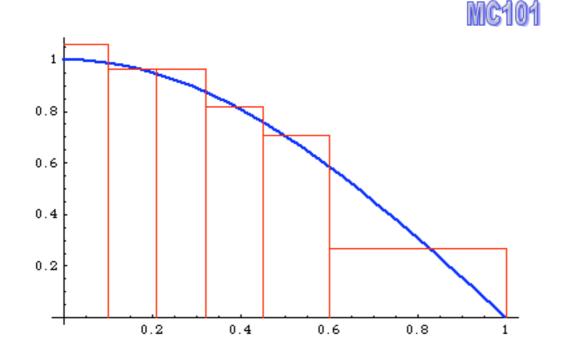
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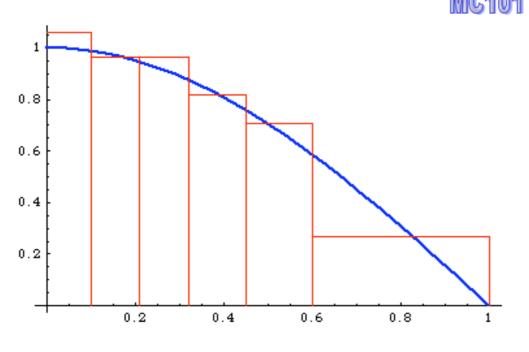






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Alternative: learn during the run and build a step-function approximation p(x) of f(x) VEGAS



many bins where f(x) is large

$$p(x) = \frac{1}{N_b \Delta x_i}, \quad x_i - \Delta x_i < x < x_i$$





can be generalized to n dimensions:

$$\overrightarrow{p(x)} = p(x) \cdot p(y) \cdot p(z) \dots$$





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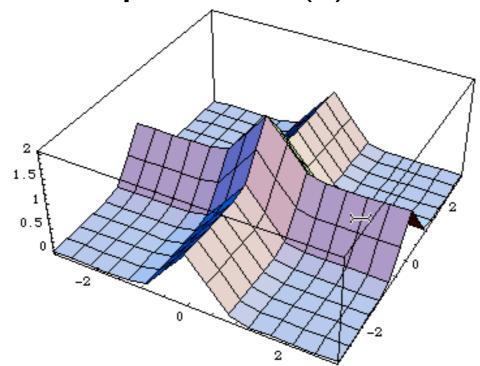




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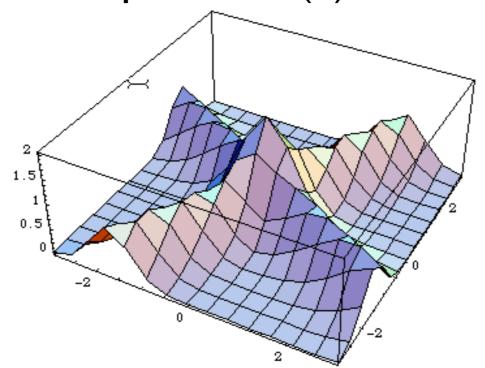


Importance Sampling

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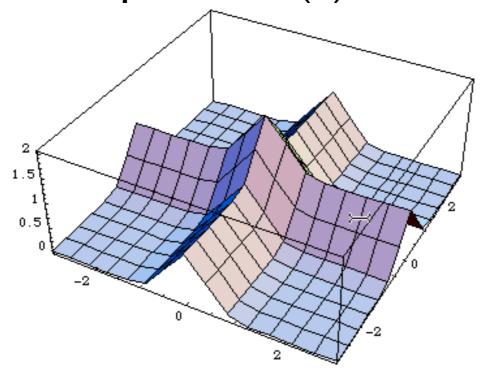


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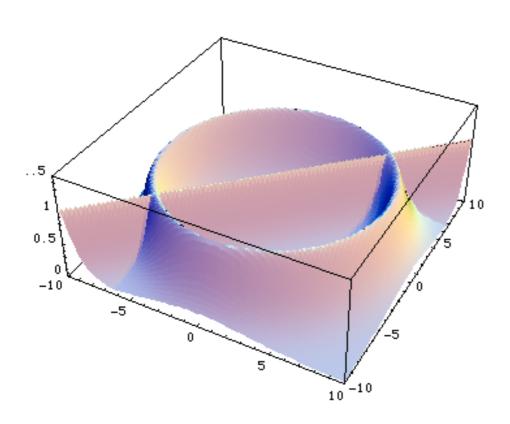
but the peaks of f(x) need to be "aligned" to the axis!



but it is sufficient to make a change of variables!



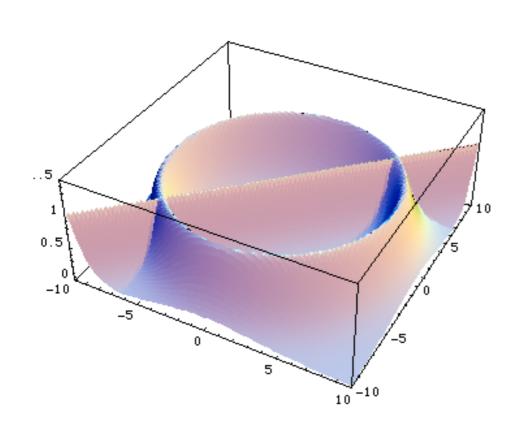




What do we do if there is no transformation that aligns all integrand peaks to the chosen axes? Vegas is bound to fail!







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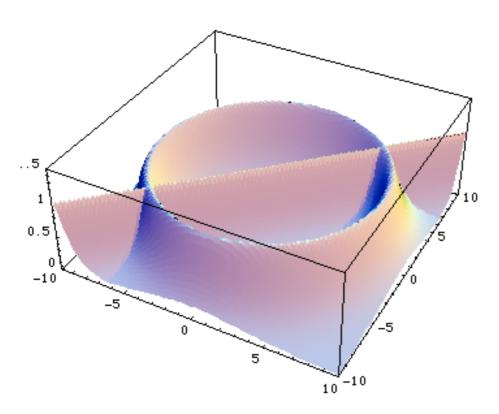
Solution: use different transformations = channels

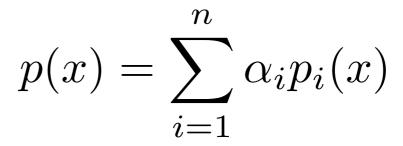
$$p(x) = \sum_{i=1}^{n} \alpha_i p_i(x) \qquad \text{with} \qquad \sum_{i=1}^{n} \alpha_i = 1$$

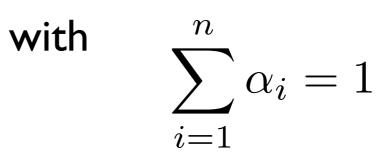
with each pi(x) taking care of one "peak" at the time

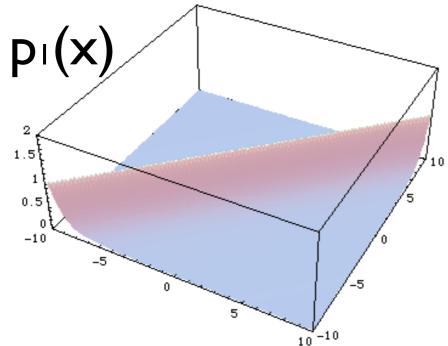


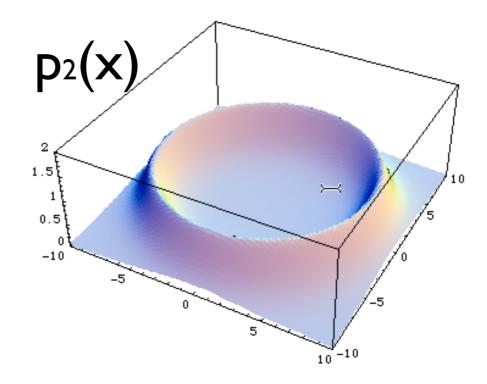






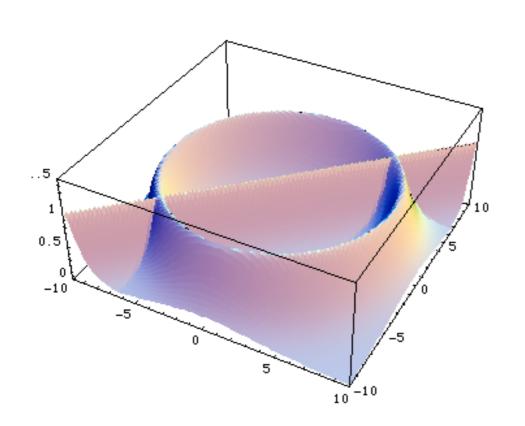












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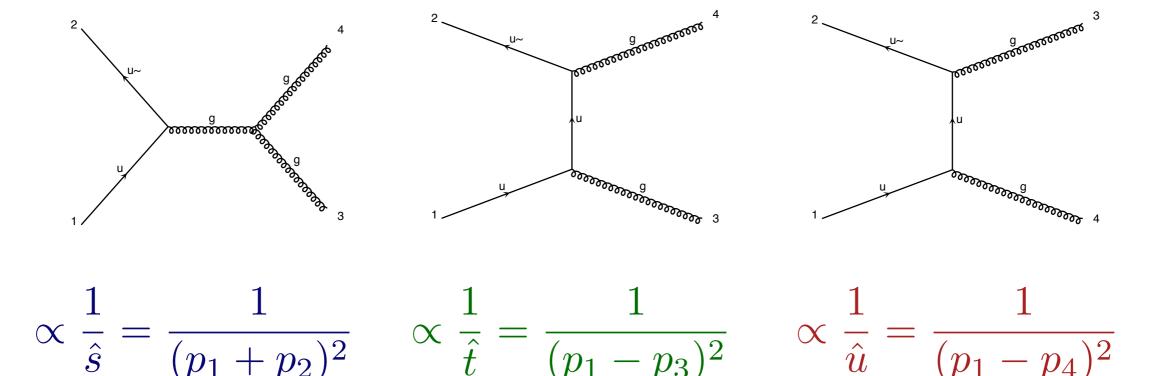
Then,

$$I = \int f(x)dx = \sum_{i=1}^{n} \alpha_i \int \frac{f(x)}{p(x)} p_i(x)dx$$



Example: QCD 2 → 2





Three very different pole structures contributing to the same matrix element.





Consider the integration of an amplitude |M|^2 at tree level which many contributing diagrams. We would like to have a basis of functions,

$$f = \sum_{i=1}^{n} f_i$$
 with $f_i \ge 0$, $\forall i$,

such that:

- I. we know how to integrate each one of them,
- 2. they describe all possible peaks,

giving us the combined integral

$$I = \int d\vec{\Phi} f(\vec{\Phi}) = \sum_{i=1}^{n} \int d\vec{\Phi} g_i(\vec{\Phi}) \frac{f_i(\vec{\Phi})}{g_i(\vec{\Phi})} = \sum_{i=1}^{n} I_i,$$





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Does such a basis exist?



■ Multi-channel based on single diagrams* Durham University



*Method used in MadGraph

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YES!
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Multi-channel based on single diagrams* **Durham



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Key Idea

- Any single diagram is "easy" to integrate (pole structures/ suitable integration variables known from the propagators)
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- All other peaks taken care of by denominator sum

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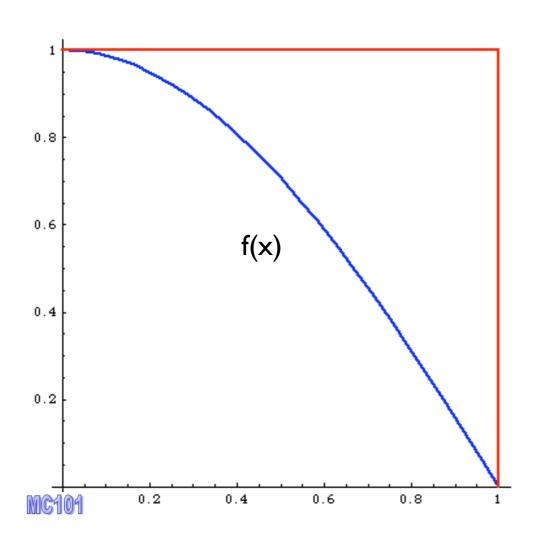
N Integral

- Errors add in quadrature so no extra cost
- "Weight" functions already calculated during M^2 calculation
- Parallel in nature



Event generation

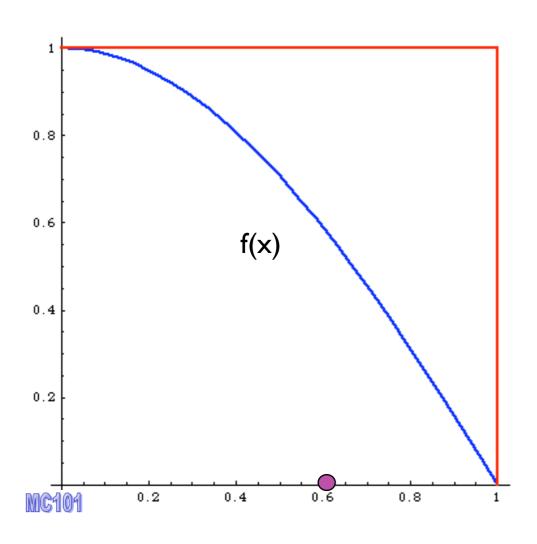






Event generation

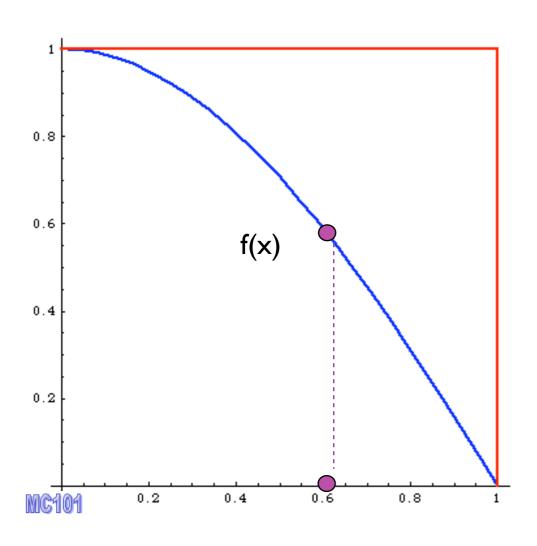




I. pick x



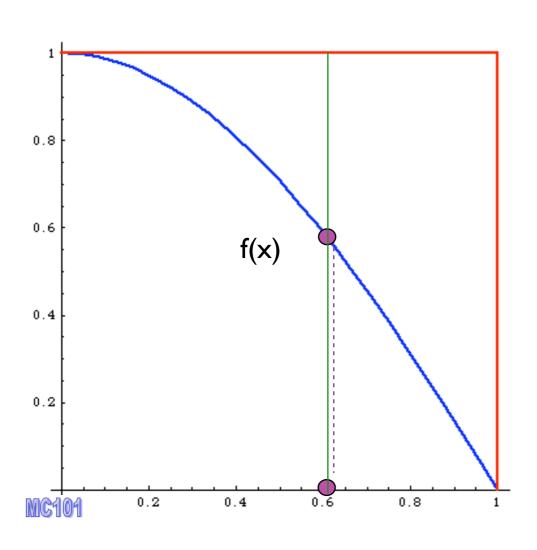




- I. pick x
- 2. calculate f(x)



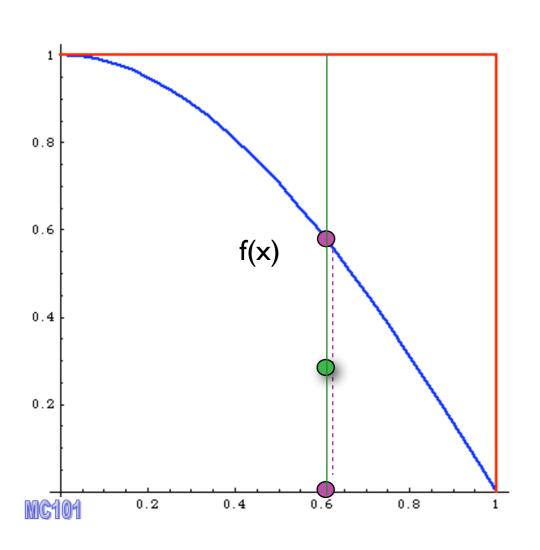




- I. pick x
- 2. calculate f(x)
- 3. pick 0<y<fmax



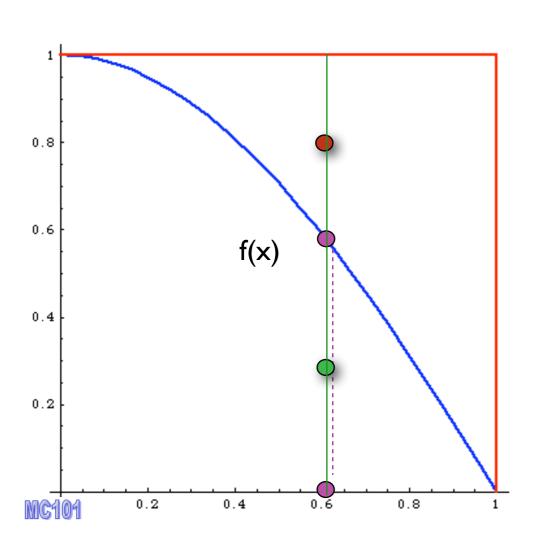




- I. pick x
- 2. calculate f(x)
- 3. pick 0<y<fmax
- 4. Compare:
 if f(x)>y accept event,





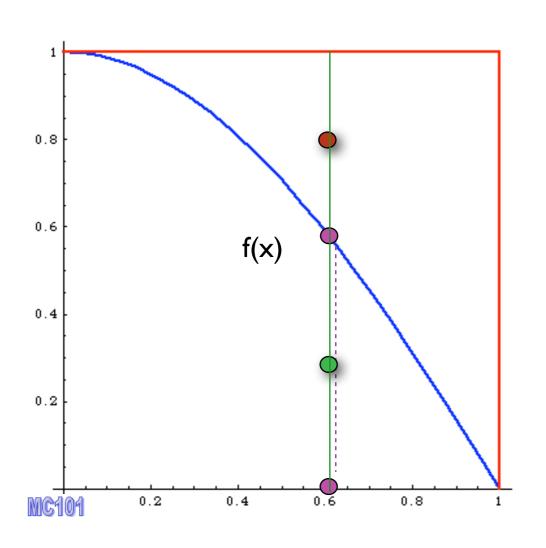


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 if f(x)>y accept event,

else reject it.



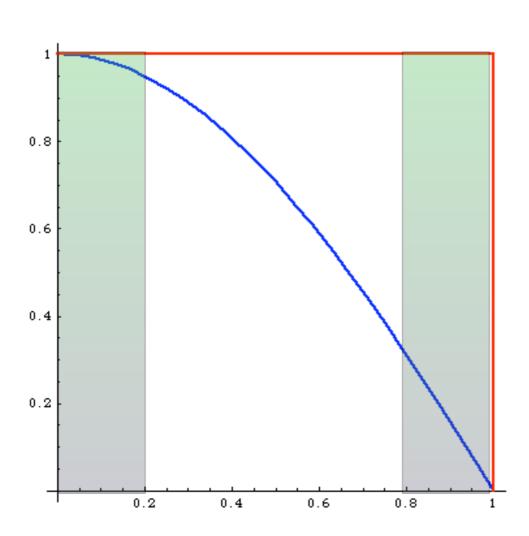




- I. pick x
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- 4. Compare:
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What's the difference between weighted and unweighted?

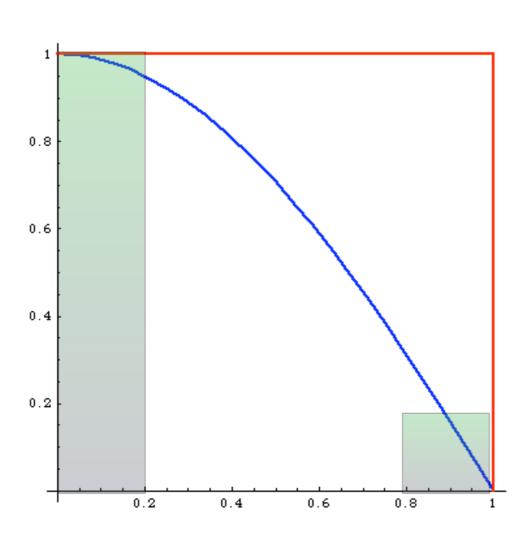
Weighted:

Same # of events in areas of phase space with very different probabilities: events must have different weights

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What's the difference between weighted and unweighted?

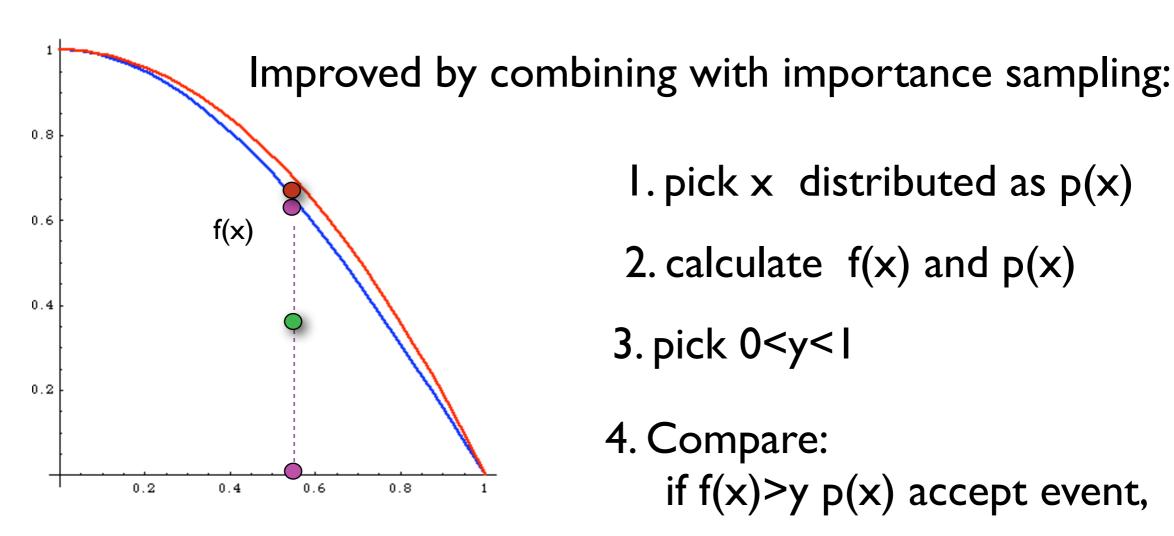
Unweighted:

events is proportional to the probability of areas of phase space: events have all the same weight ("unweighted")

Events distributed as in nature







- - I. pick x distributed as p(x)
 - 2. calculate f(x) and p(x)
- 3. pick 0<y<1
- 4. Compare: if f(x)>y p(x) accept event,

else reject it.

much better efficiency!!!



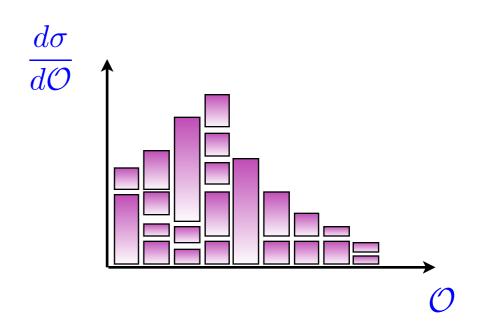


MC integrator



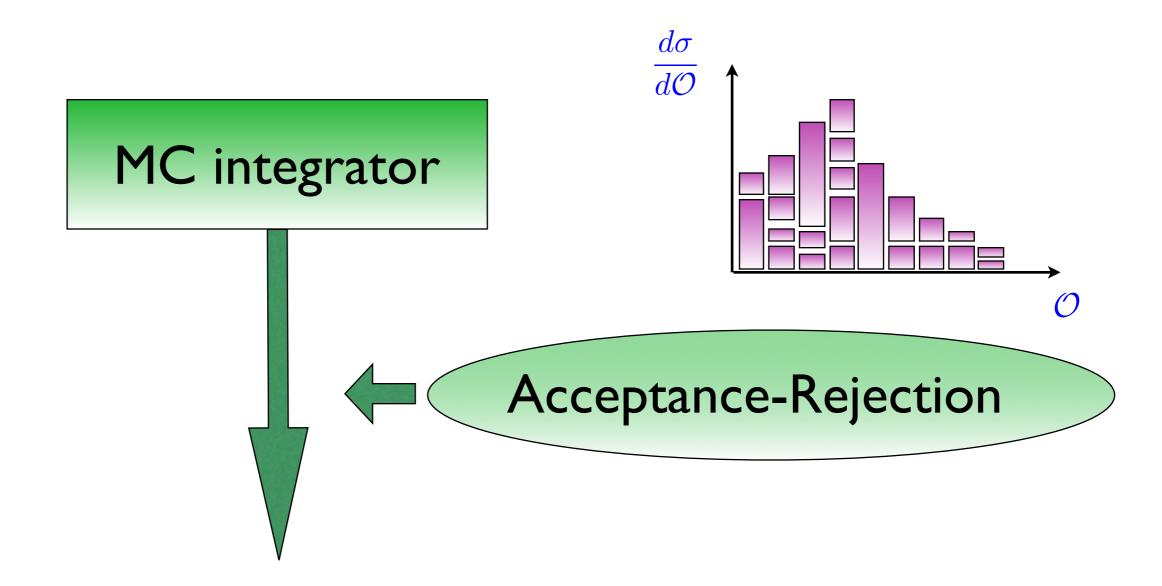


MC integrator



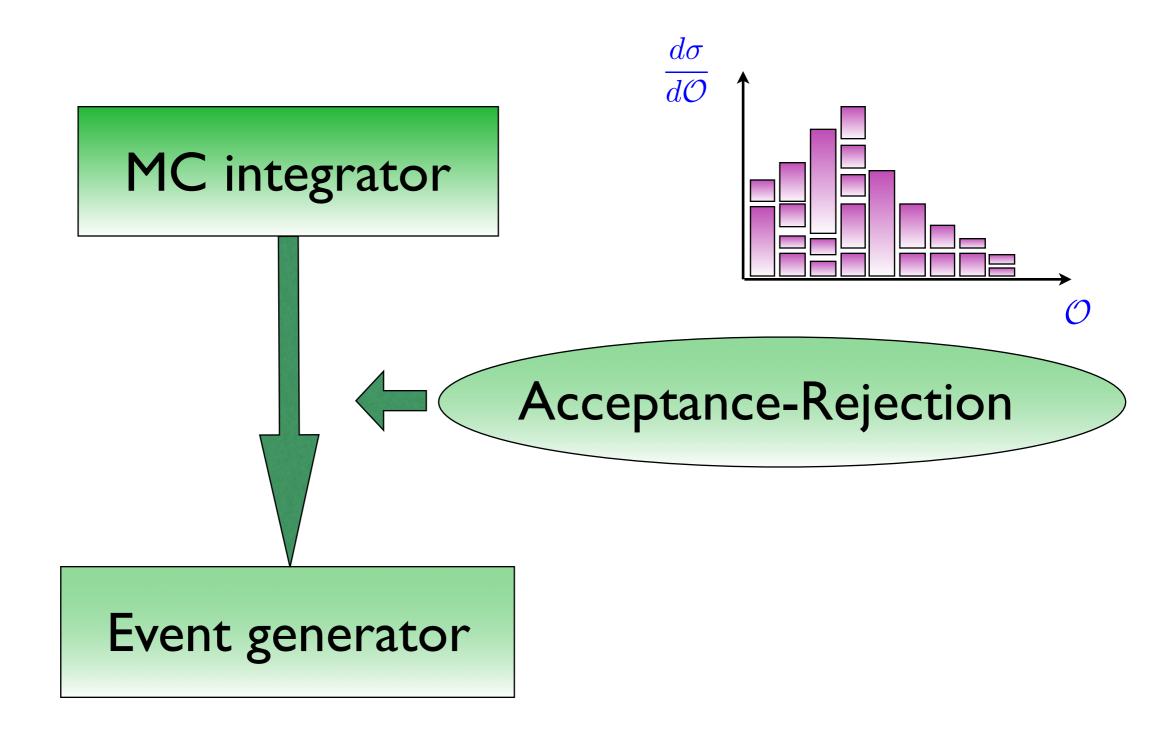






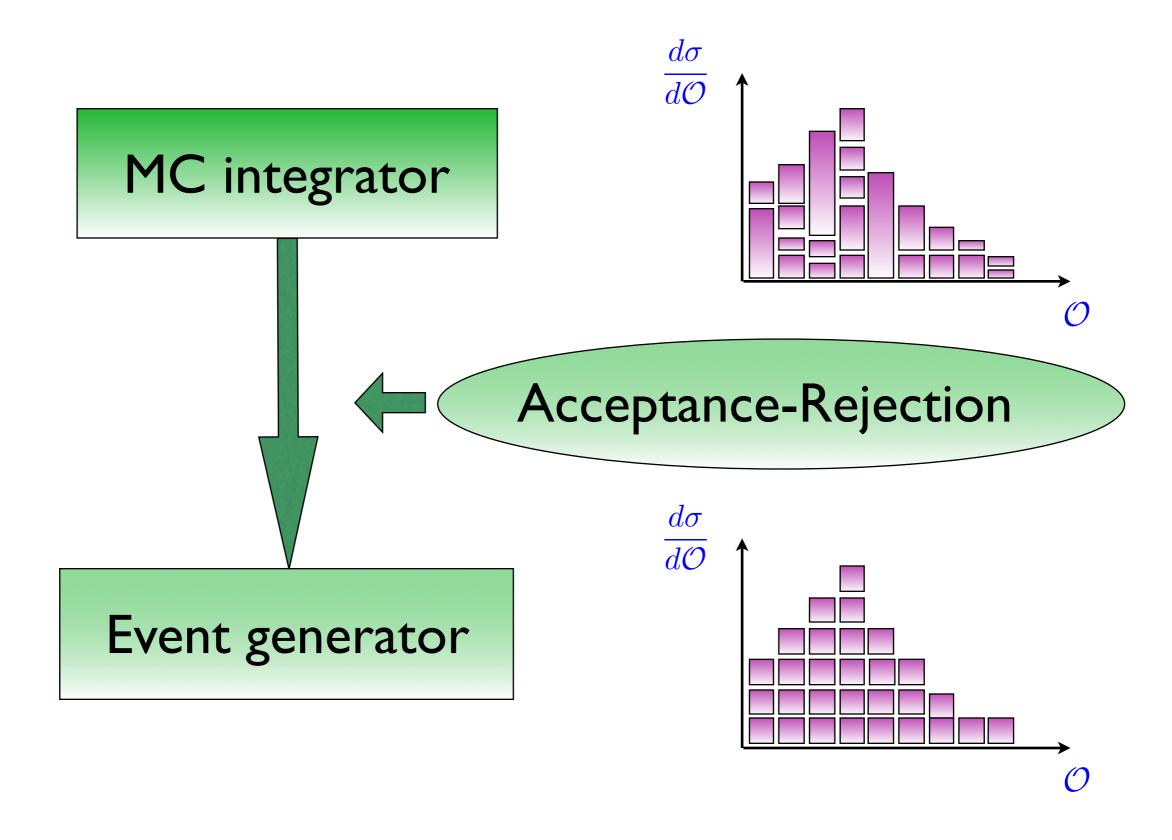






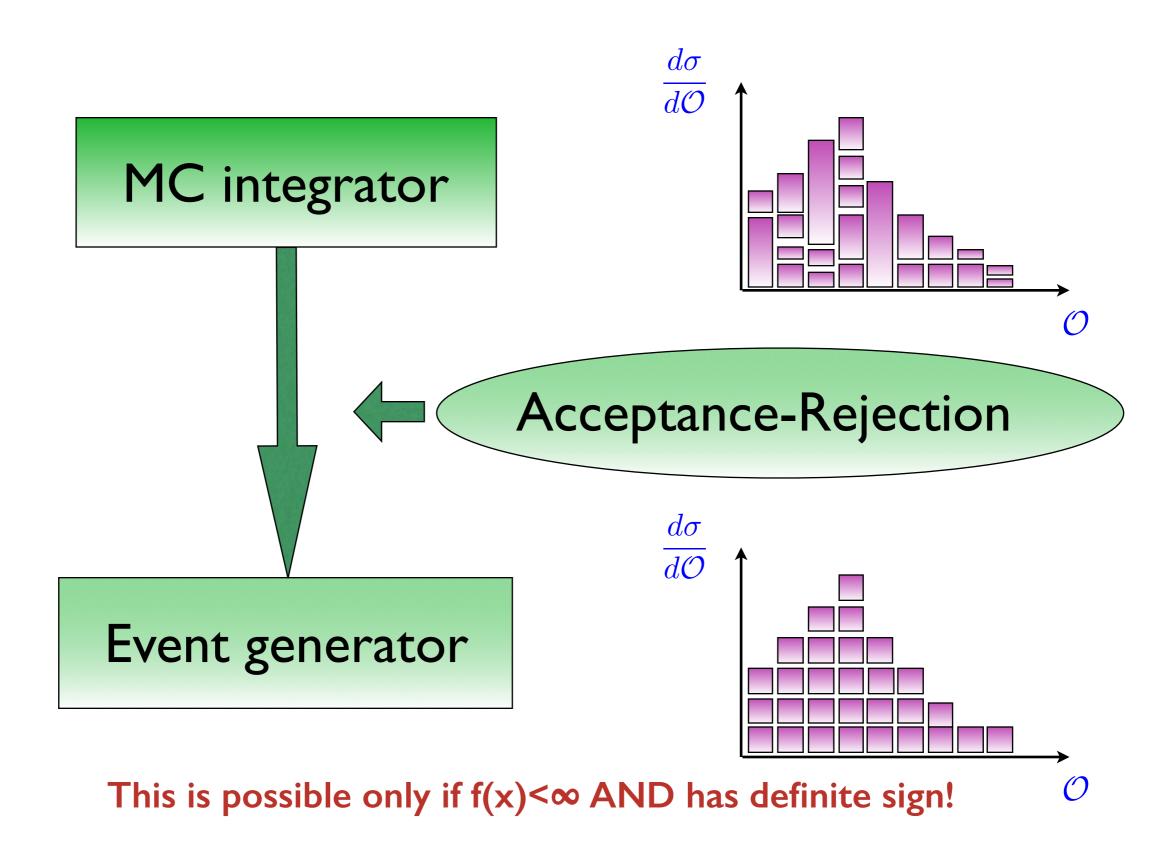












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Con-





MadGraph5_aMC@NLO

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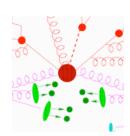








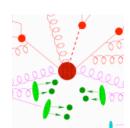




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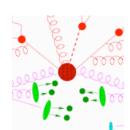


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 hep-ph/0208156







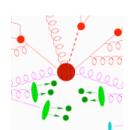


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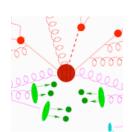




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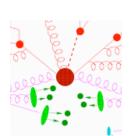
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arXiv:1106.0522

arXiv:1405.0301









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hep-ph/0208156 1000
arXiv:0706.2334 1400

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arXiv:1106.0522 1250

arXiv:1405.0301 10





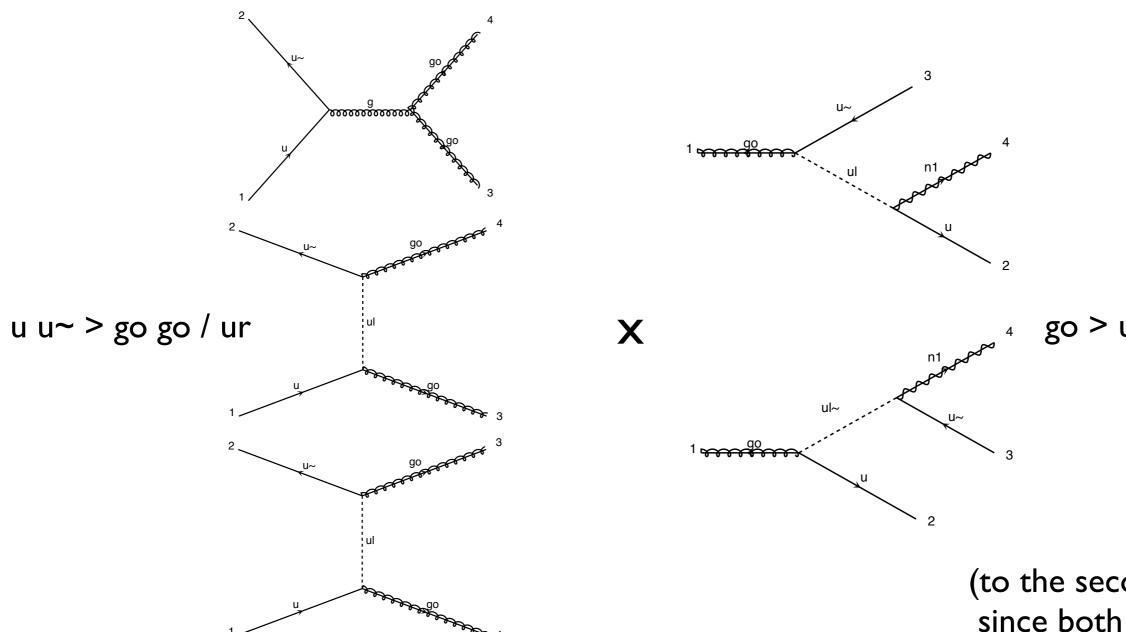
- $p p > t t \sim w+, (t > w+ b, w+ > l+ vl), \$ $(t\sim > w- b\sim, w- > i i), \$ w+ > |+ v|
- Separately generate core process and each decay
 - Decays generated with the decaying particle as resulting wavefunction
- Iteratively combine decays and core processes
- Difficulty: Multiple diagrams in decays

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If multiple diagrams in decays, need to multiply together core process and decay diagrams:



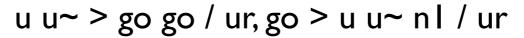
go > u u~ nI / ur

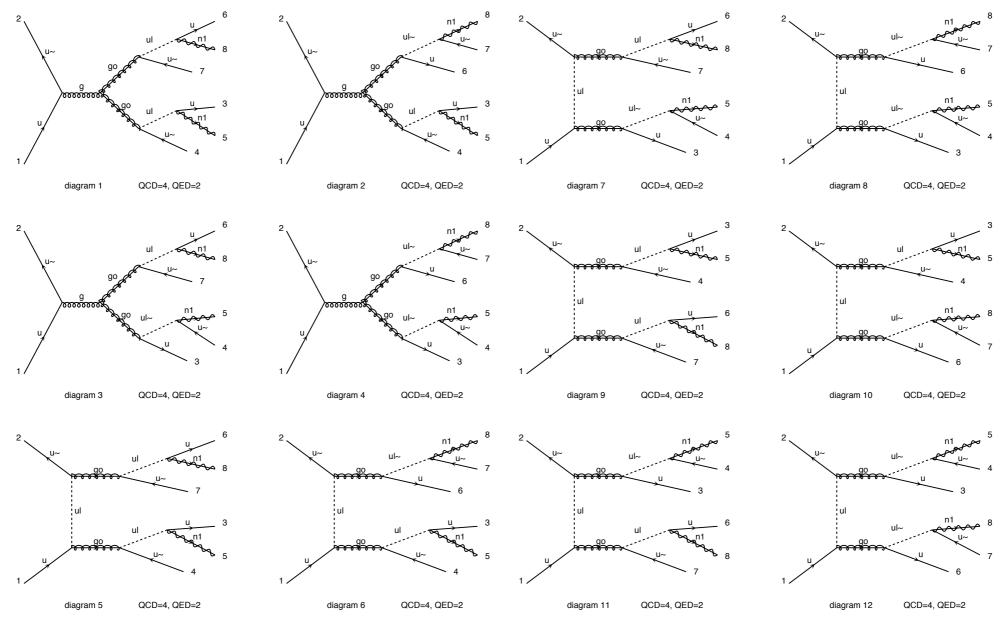
(to the second power since both gluinos decay)





• If multiple diagrams in decays, need to multiply together core process and decay diagrams:





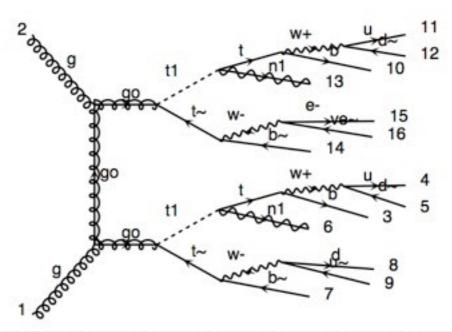


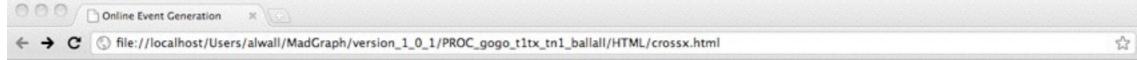


- Decay chains retain full matrix element for the diagrams compatible with the decay
- Full spin correlations (within and between decays)
- Full width effects
- However, no interference with non-resonant diagrams
 - → Description only valid close to pole mass
 - \rightarrow Cutoff at $|m \pm n\Gamma|$ where n is set in run_card.









Results for g g > go go , (go > t1 t~, t~> b~ all all / h+ , (t1 > t n1 , t > b all all / h+)) in the mssm

Available Results

Links	Events	Tag	Run	Collider	Cross section (pb)	Events
results banner	Parton-level LHE	fermi	test	p p 7000 x 7000 GeV	.33857E-03	10000

Main Page

Thanks to developments in MadEvent, also (very) long decay chains possible to simulate directly in MadGraph!





Output formats in MadGraph 5

- Thanks to UFO/ALOHA, we now have automatic helicity amplitude routines in any language
 - So it makes sense to have also matrix element output in multiple languages!
- Presently implemented: Fortran, C++, Python
 - → Fortran for MadEvent and Standalone
 - → C++ for Pythia 8 and Standalone
 - → Python for internal use in MG5 (checks of gauge, perturbation and Lorentz invariance)

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Life Demo





Examples shown

- p p > t t~
 This gives only (the dominant) QCD vertices, and ignores (the negligible) QED vertices.
- p p > t t~ QED=2
 This gives both QED and QCD vertices.
- p p > w+ j j, w+ > l+ vl
 More complicated example.

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More syntax examples

- p p > t t~ j QED=2: Generate all combinations of processes for particles defined in multiparticle labels p / j, including up to two QED vertices (and unlimited QCD vertices)
- $p p > t t \sim$, $(t > b w +, w + > l + vl), t \sim > b \sim j j$:
 - Only diagrams compatible with given decay
 - Only t / t~ and W+ close to mass shell in event generation
- p p > w+ w- / h : Exclude any diagrams with h
- p p > w+ w- \$ h : Exclude on-shell h in event generation (but retain interference effects)

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Summary



$$\int \hat{\sigma}_{ab\to X}(\hat{s},\ldots) f_a(x_1) f_b(x_2) dx_1 dx_2 d\Phi_{FS}$$

cross section

Parton level Parton density Phase space functions

integral

- MadGraph use Numerical method for the matrix element
 - → Faster than analytical formula
 - → Available For ANY BSM (thanks to UFO/ALOHA)
- Numerical integration is not trivial
 - → We use Monte-Carlo integration
 - → Return physical sample of events!
- MG5
 - → decay chains
 - → nice interface
 - → several output formats