

MADLOOP⁵

GOING BEYONDER

V A L E N T I N H I R S C H I
E P F L

4 T H S E P T E M B E R 2 0 1 2

P R E S E N T A T I O N
H P 2 ^ 4 @ M P I M Ü N I C H

OUTLINE

- NLO challenges and **aMC@NLO** philosophy
- **Implementation** details
- **Speed** and **stability** benchmark study
- **Future plans** and closing words

MADGRAPH@NLO

OVERVIEW

OBJECTIVES FOR MADGRAPH5 AT NLO

- **Automation** and **Flexibility**

Minimize hand work while maximizing applicability.
Also automation provides reliability by avoiding bugs.

- **Unique framework** and **user-friendly**

It only takes to know how to efficiently use one single program to do all NLO phenomenology.
User-guidance and on-the-fly checks insure reliable results.

- **Stable** and **fast** enough for relevant processes

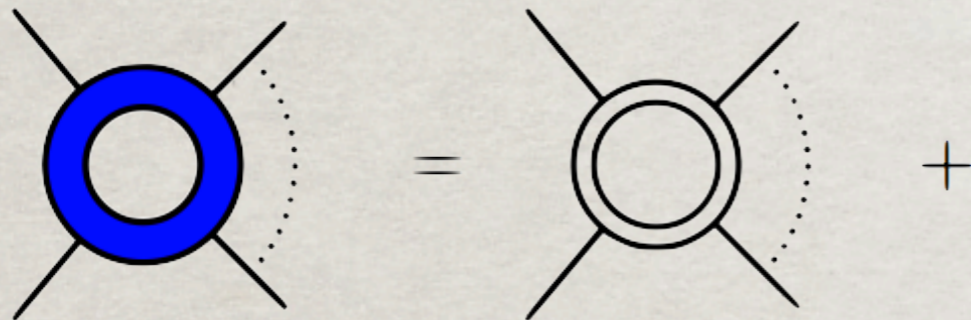
No huge cluster needed.
LesHouches wish list(s) covered.

NLO BASICS

Fixed-order **NLO** contributions have **two** parts

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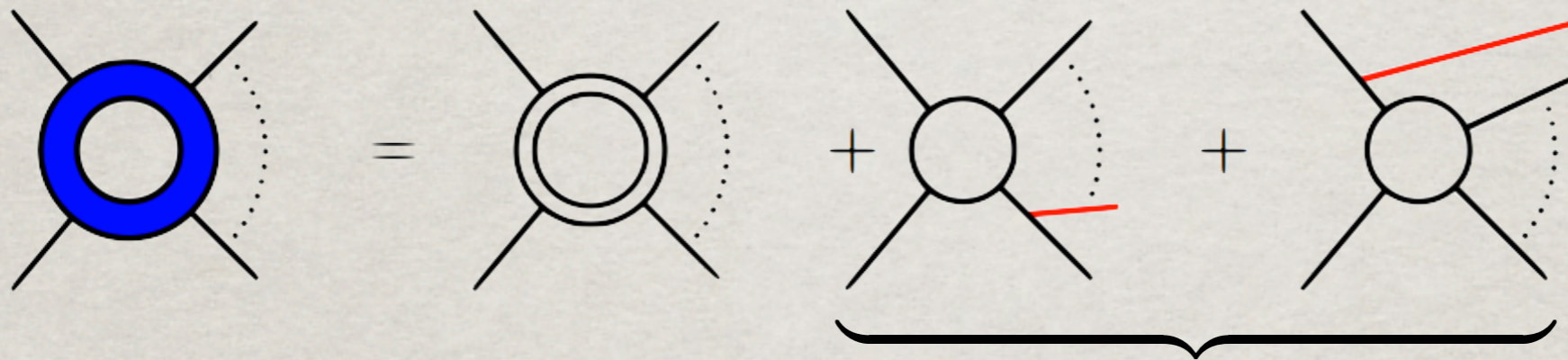
$$\sigma^{\text{NLO}} = \int_m d^{(d)} \sigma^V +$$

Virtual part

- Used to be **bottleneck** of NLO computations
- Algorithms for automation known in principle but needs to be **efficiently** implemented
- **MadLoop5** in MG5 takes care of this piece

NLO BASICS

Fixed-order **NLO** contributions have **two** parts



$$\sigma^{\text{NLO}} = \int_m d^{(d)} \sigma^V + \int_{m+1} d^{(d)} \sigma^R +$$

Virtual part

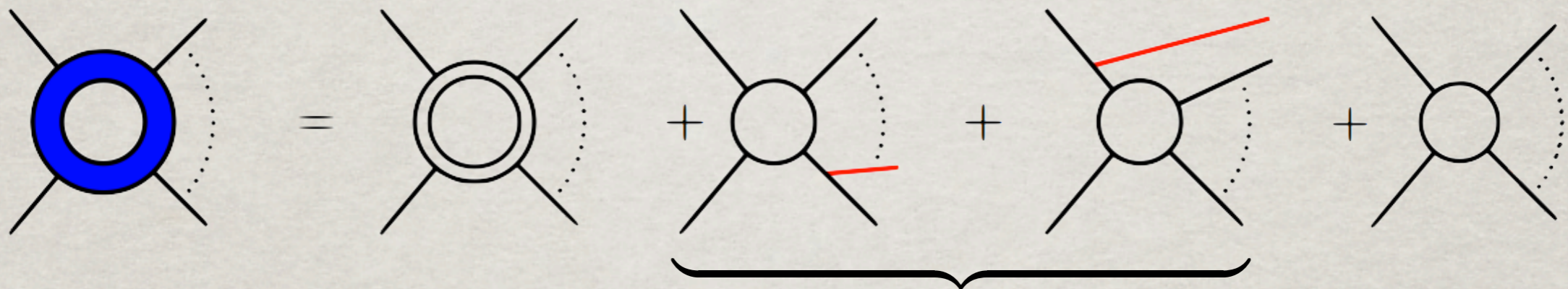
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Real emission part

- Automated for different methods
- Challenge is the systematic extraction of **singularities**
- **MadFKS5** in MG5 takes care of this piece

NLO BASICS

Fixed-order **NLO** contributions have **two** parts



$$\sigma^{\text{NLO}} = \int_m d^{(d)} \sigma^V + \underbrace{\int_{m+1} d^{(d)} \sigma^R + \int_m d^{(4)} \sigma^B}_{\text{Real emission part}}$$

Virtual part

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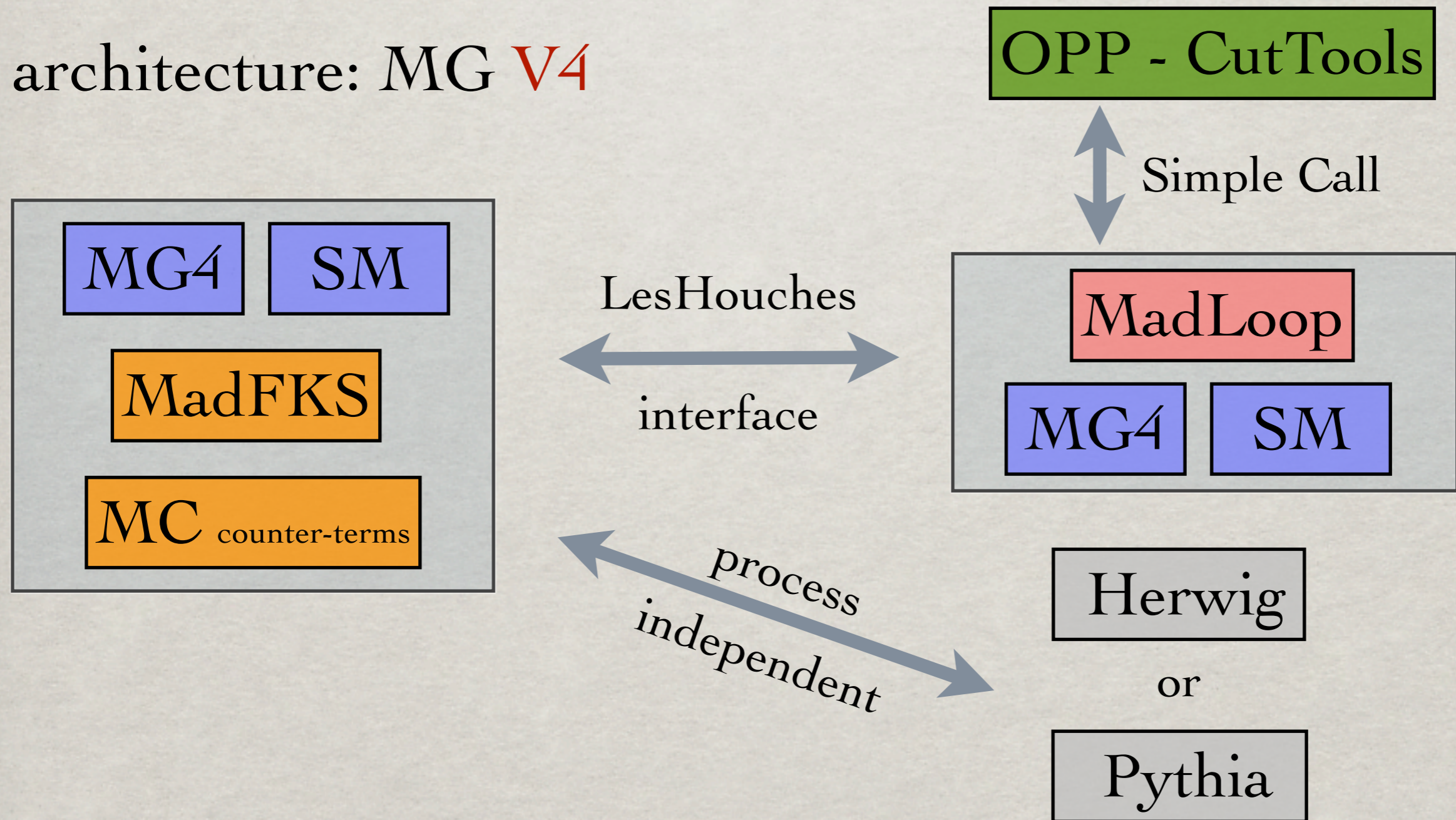
Real emission part

- Automated for different methods
- Challenge is the systematic extraction of **singularities**
- **MadFKS5** in MG5 takes care of this piece

AMC@NLO

TOWARDS FULL AUTOMATION

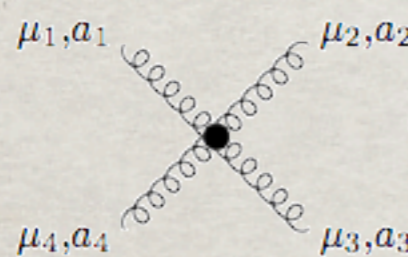
architecture: MG V4



MADLOOP IN MG4

WHAT IT COULD **NOT** DO

- ✓ No **four-gluon vertex** at **born level** :



$$\begin{aligned}
 &= -\frac{ig^4 N_{col}}{96\pi^2} \sum_{P(234)} \left\{ \left[\frac{\delta_{a_1 a_2} \delta_{a_3 a_4} + \delta_{a_1 a_3} \delta_{a_4 a_2} + \delta_{a_1 a_4} \delta_{a_2 a_3}}{N_{col}} \right. \right. \\
 &\quad \left. \left. + 4 \text{Tr}(t^{a_1} t^{a_3} t^{a_2} t^{a_4} + t^{a_1} t^{a_4} t^{a_2} t^{a_3}) (3 + \lambda_{HV}) \right. \right. \\
 &\quad \left. \left. - \text{Tr}(\{t^{a_1} t^{a_2}\} \{t^{a_3} t^{a_4}\}) (5 + 2\lambda_{HV}) \right] g_{\mu_1 \mu_2} g_{\mu_3 \mu_4} \right. \\
 &\quad \left. + 12 \frac{N_f}{N_{col}} \text{Tr}(t^{a_1} t^{a_2} t^{a_3} t^{a_4}) \left(\frac{5}{3} g_{\mu_1 \mu_3} g_{\mu_2 \mu_4} - g_{\mu_1 \mu_2} g_{\mu_3 \mu_4} - g_{\mu_2 \mu_3} g_{\mu_1 \mu_4} \right) \right\}
 \end{aligned}$$

- ✓ All born contribution must **factorize the same power of all coupling orders**.
- ✓ No **finite-width effects** of unstable massive particles also appearing in the loop.
- ✓ / ✗ Handle **BSM** model or/and **EW** corrections.

WHAT ML4 COULD DO

- Running time: **Two weeks** on a **150+ node cluster**
- Proof of efficient **EPS** handling with $Zt\bar{t}$
- Successful **cross-check** against known results
- Large **K-factors** sometimes
- No cuts on b, **robust** numerics with small P_T

Process	μ	n_{lf}	Cross section (pb)	
			LO	NLO
a.1 $pp \rightarrow t\bar{t}$	m_{top}	5	123.76 ± 0.05	162.08 ± 0.12
a.2 $pp \rightarrow tj$	m_{top}	5	34.78 ± 0.03	41.03 ± 0.07
a.3 $pp \rightarrow tjj$	m_{top}	5	11.851 ± 0.006	13.71 ± 0.02
a.4 $pp \rightarrow t\bar{b}j$	$m_{top}/4$	4	25.62 ± 0.01	30.96 ± 0.06
a.5 $pp \rightarrow t\bar{b}jj$	$m_{top}/4$	4	8.195 ± 0.002	8.91 ± 0.01
b.1 $pp \rightarrow (W^+ \rightarrow)e^+\nu_e$	m_W	5	5072.5 ± 2.9	6146.2 ± 9.8
b.2 $pp \rightarrow (W^+ \rightarrow)e^+\nu_e j$	m_W	5	828.4 ± 0.8	1065.3 ± 1.8
b.3 $pp \rightarrow (W^+ \rightarrow)e^+\nu_e jj$	m_W	5	298.8 ± 0.4	300.3 ± 0.6
b.4 $pp \rightarrow (\gamma^*/Z \rightarrow)e^+e^-$	m_Z	5	1007.0 ± 0.1	1170.0 ± 2.4
b.5 $pp \rightarrow (\gamma^*/Z \rightarrow)e^+e^- j$	m_Z	5	156.11 ± 0.03	203.0 ± 0.2
b.6 $pp \rightarrow (\gamma^*/Z \rightarrow)e^+e^- jj$	m_Z	5	54.24 ± 0.02	56.69 ± 0.07
c.1 $pp \rightarrow (W^+ \rightarrow)e^+\nu_e b\bar{b}$	$m_W + 2m_b$	4	11.557 ± 0.005	22.95 ± 0.07
c.2 $pp \rightarrow (W^+ \rightarrow)e^+\nu_e t\bar{t}$	$m_W + 2m_{top}$	5	0.009415 ± 0.000003	0.01159 ± 0.00001
c.3 $pp \rightarrow (\gamma^*/Z \rightarrow)e^+e^- b\bar{b}$	$m_Z + 2m_b$	4	9.459 ± 0.004	15.31 ± 0.03
c.4 $pp \rightarrow (\gamma^*/Z \rightarrow)e^+e^- t\bar{t}$	$m_Z + 2m_{top}$	5	0.0035131 ± 0.0000004	0.004876 ± 0.000002
c.5 $pp \rightarrow \gamma t\bar{t}$	$2m_{top}$	5	0.2906 ± 0.0001	0.4169 ± 0.0003
d.1 $pp \rightarrow W^+W^-$	$2m_W$	4	29.976 ± 0.004	43.92 ± 0.03
d.2 $pp \rightarrow W^+W^- j$	$2m_W$	4	11.613 ± 0.002	15.174 ± 0.008
d.3 $pp \rightarrow W^+W^- jj$	$2m_W$	4	0.07048 ± 0.00004	0.1377 ± 0.0005
e.1 $pp \rightarrow HW^+$	$m_W + m_H$	5	0.3428 ± 0.0003	0.4455 ± 0.0003
e.2 $pp \rightarrow HW^+ j$	$m_W + m_H$	5	0.1223 ± 0.0001	0.1501 ± 0.0002
e.3 $pp \rightarrow HZ$	$m_Z + m_H$	5	0.2781 ± 0.0001	0.3659 ± 0.0002
e.4 $pp \rightarrow HZ j$	$m_Z + m_H$	5	0.0988 ± 0.0001	0.1237 ± 0.0001
e.5 $pp \rightarrow Ht\bar{t}$	$m_{top} + m_H$	5	0.08896 ± 0.00001	0.09869 ± 0.00003
e.6 $pp \rightarrow Hb\bar{b}$	$m_b + m_H$	4	0.16510 ± 0.00009	0.2099 ± 0.0006
e.7 $pp \rightarrow Hjj$	m_H	5	1.104 ± 0.002	1.036 ± 0.002

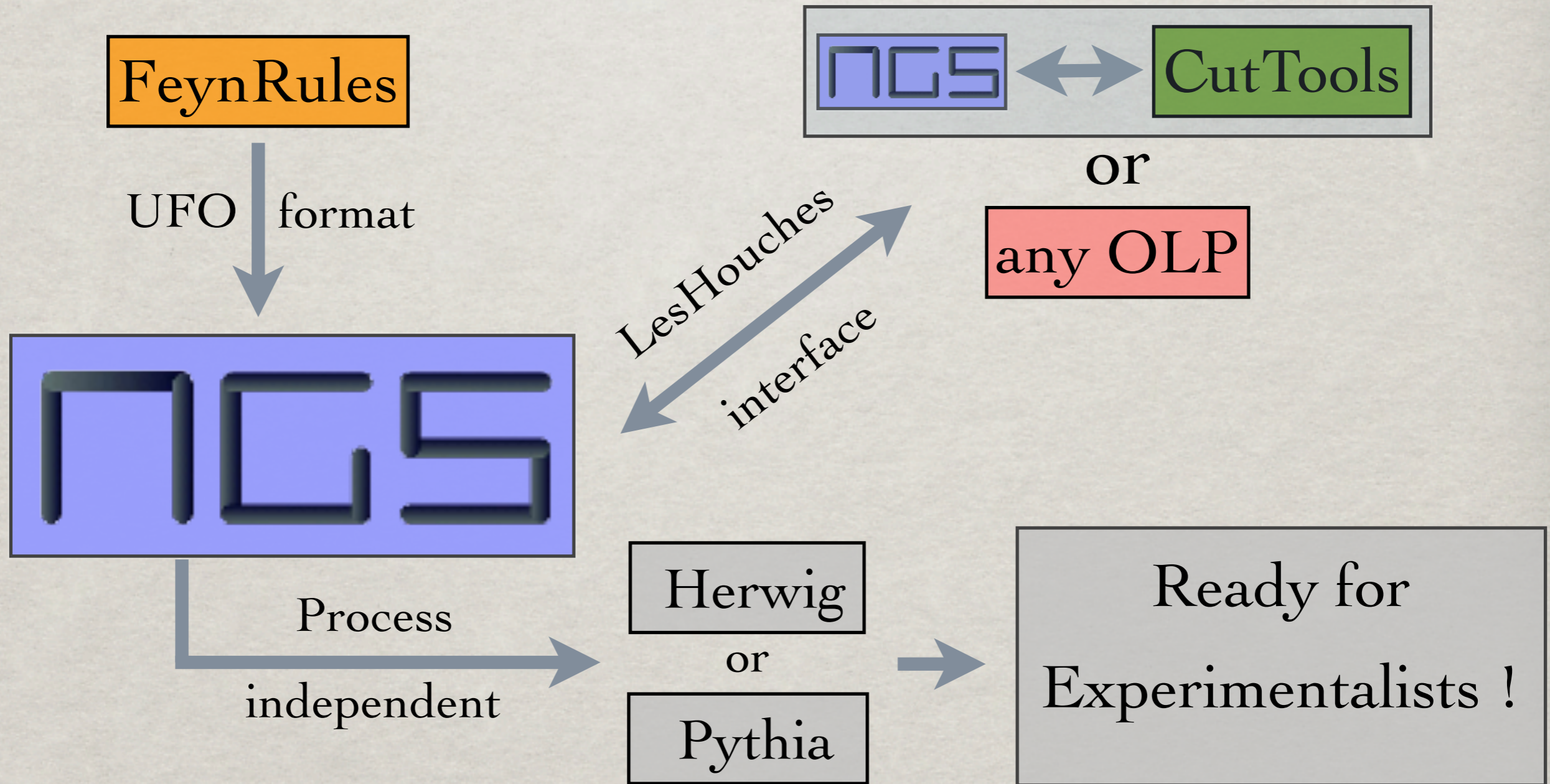
MADGRAPH 5 SPECS

- High-level language: **Python**
 - Complex data-structures allow for very **general objects** while keeping **speed** where needed.
 - Involved algorithms => **Performance increase**
- Built-in testing suite => **Reliability**
- User-interface and automatic doc. => **User friendly**
- Flexible and Modular => **Developer friendly**
All-in-one distribution

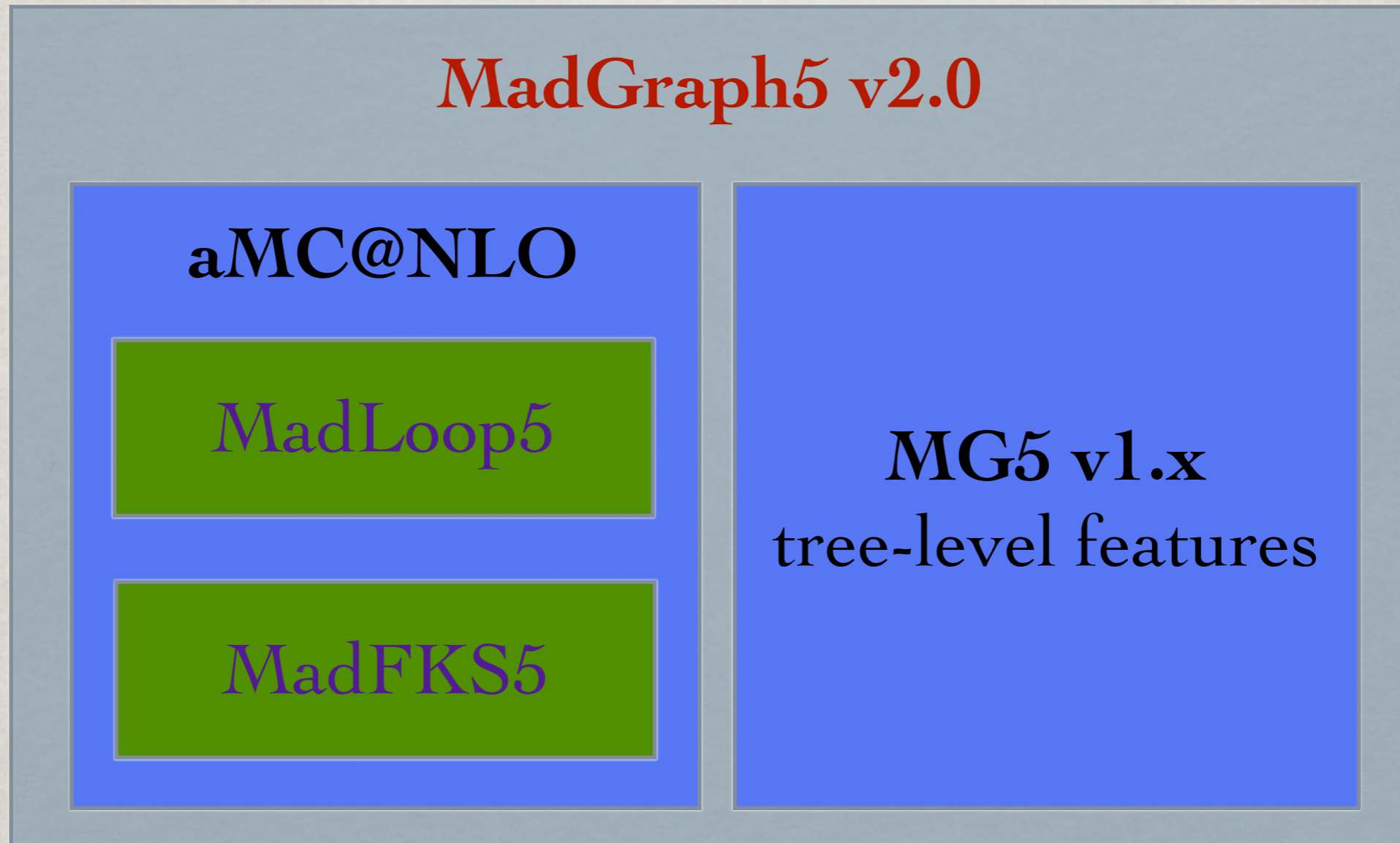
AMC@NLO

FULL AUTOMATION...

... in MadGraph5 v2.0!



NOMENCLATURE



But this separation is now **transparent** to the users!

IMPLEMENTATION

MADLOOP5 IN MG5 v2.0

FRIEND OF USERS

• Process generation

```
• import model <model_name>-<restrictions>
• generate <process> <amp;_orders_and_option> [<mode>=<pert_orders>] <squared_orders>
• output <format> <folder_name>
• launch
```

• Examples, starting from a blank MG5 interface.

• Very simple one:

```
[ 1.54s ] generate g g > t t~ [virt=QCD]
[ 1.18s ] output
[ 44 ms*] launch
```

• With options specified:

```
[ 0.01s ] import model loop_sm-no_bmass
[ 0.01s ] set complex_mass_scheme
[ 22.8s ] generate g g > W+ W- b b~ / z h a QED=2 [virt=QCD] QCD=6 WEIGHTED=14
[ 14.0s ] output standalone MyProc
[ 17.1s*] launch
```

* time per phase-space point, summed over helicities and colors.

CUT-LOOP DIAGRAMS

WITH A SPECIFIC EXAMPLE

Consider $e^+e^- \rightarrow \gamma \rightarrow u\bar{u}$:

- **Loop particles** are denoted with a star. When MG is asked for $e^+e^- \rightarrow u^*\bar{u}^*u\bar{u}$ it gives back eight diagrams. Two of them are:

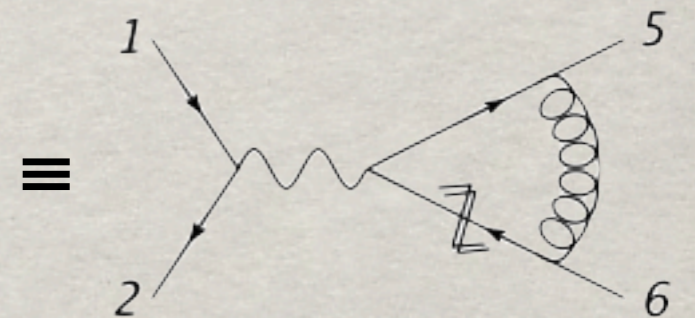
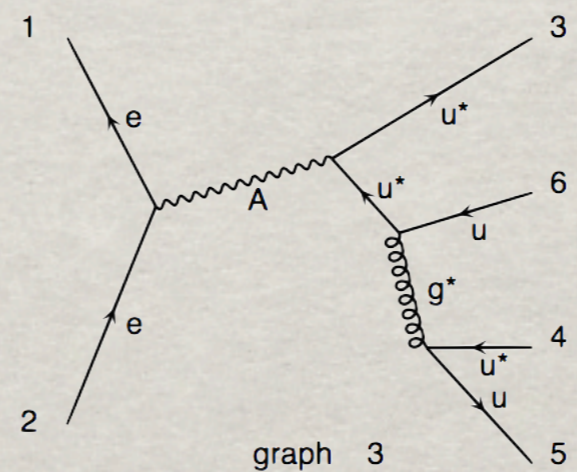
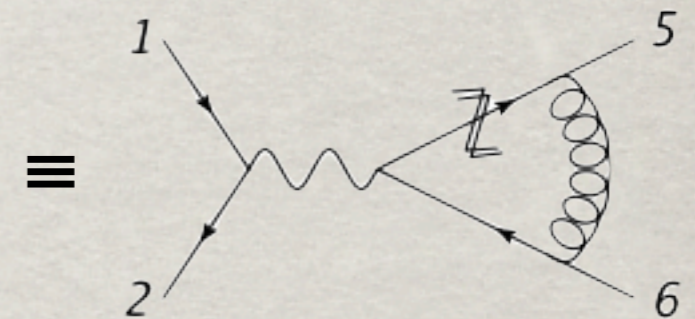
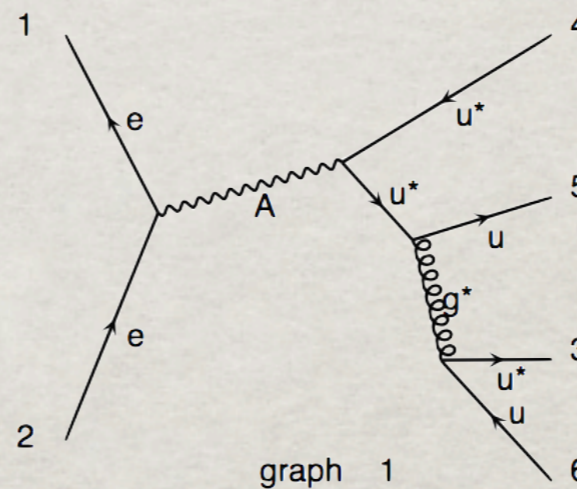
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• **Selection** is performed to keep only one cut-diagram per loop contributing in the process



CUT-LOOP DIAGRAMS

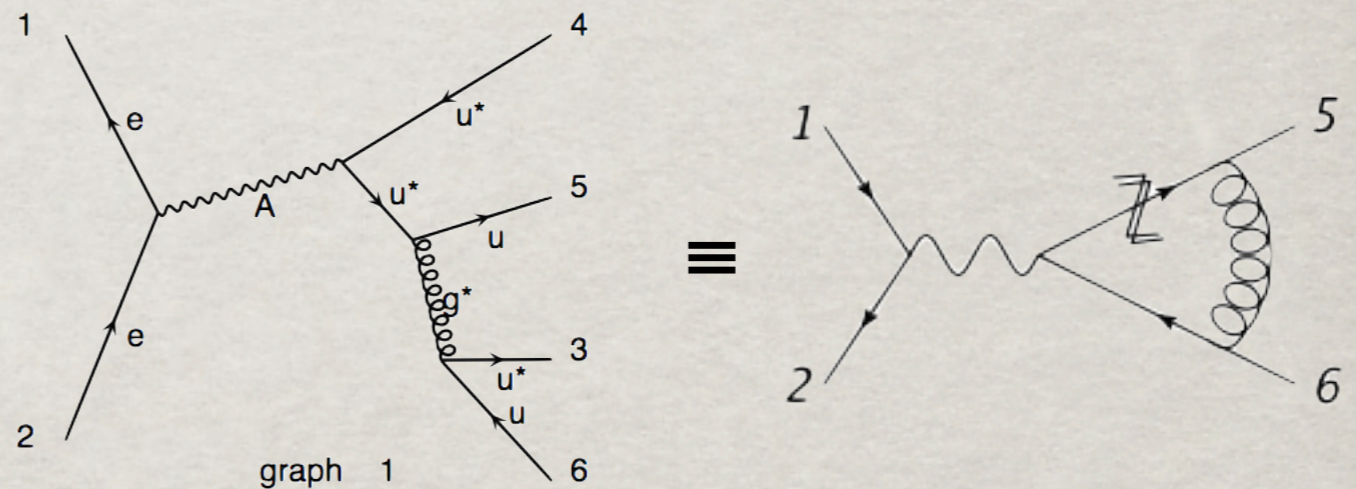
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Consider $e^+e^- \rightarrow \gamma \rightarrow u\bar{u}$:

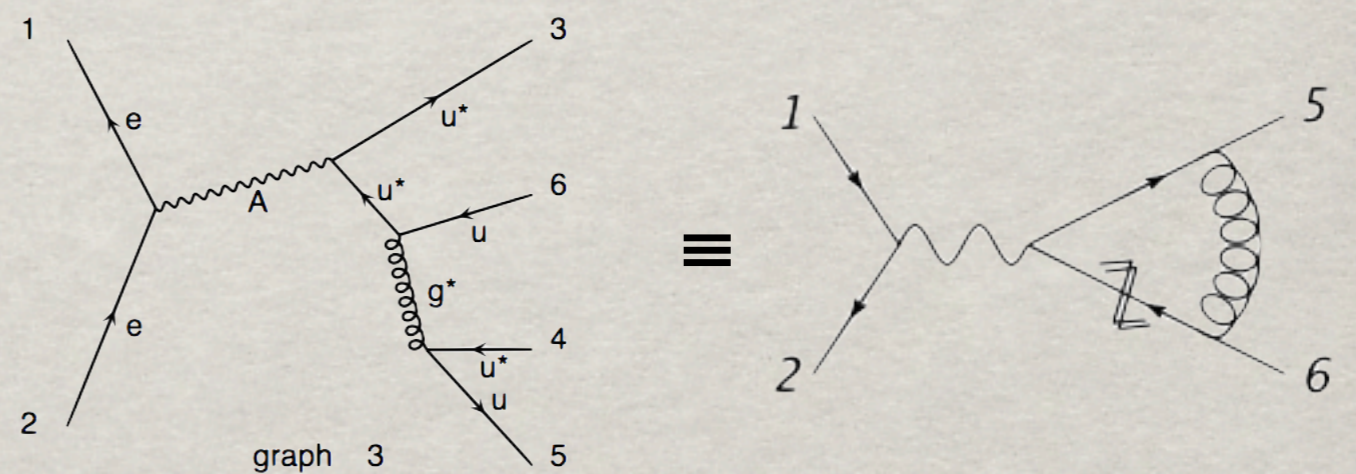
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- **Tags** are associated to each cut-diagram. Those whose tags are **mirror and/or cyclic permutations** of tags of diagram already in the **loop-basis** are taken out.



$$\text{Diag}_1 = [u^*(6)g^*(5)u^*(A)]$$



$$\text{Diag}_3 = [u^*(A)u^*(6)g^*(5)]$$

CUT-LOOP DIAGRAMS

WITH A SPECIFIC EXAMPLE

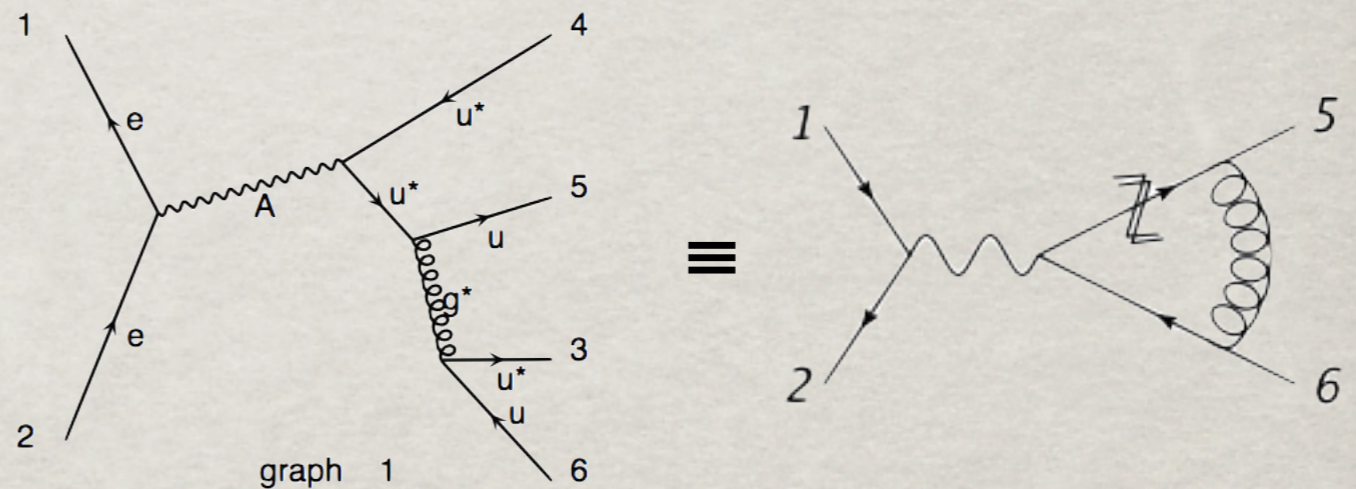
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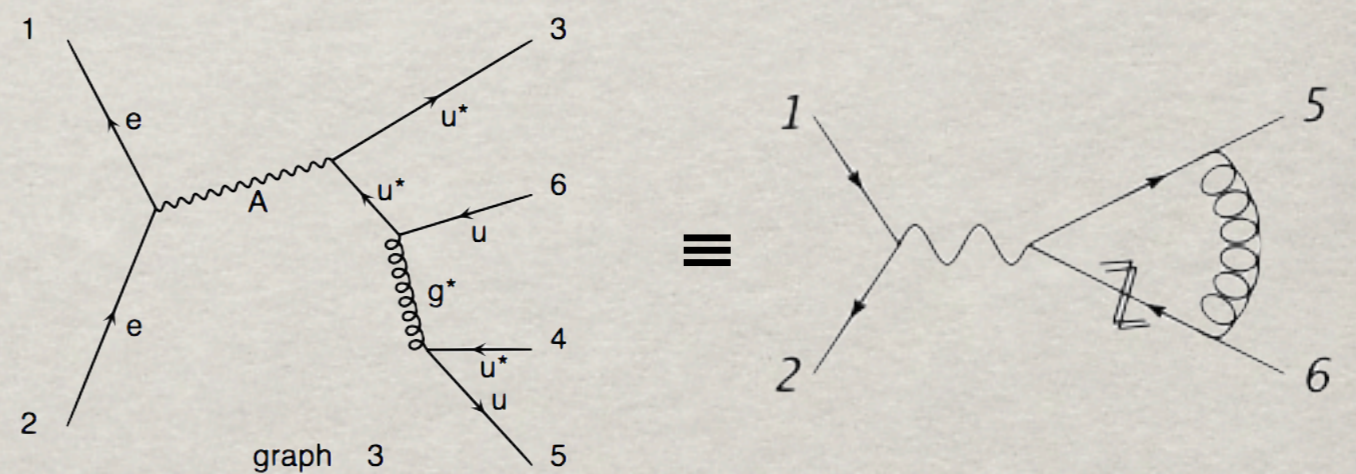
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- **Tags** are associated to each cut-diagram. Those whose tags are **mirror and/or cyclic permutations** of tags of diagram already in the **loop-basis** are taken out.

- Additional custom **filter** to eliminate **tadpoles** and **bubbles** attached to external legs.



$$\text{Diag}_1 = [u^*(6)g^*(5)u^*(A)]$$

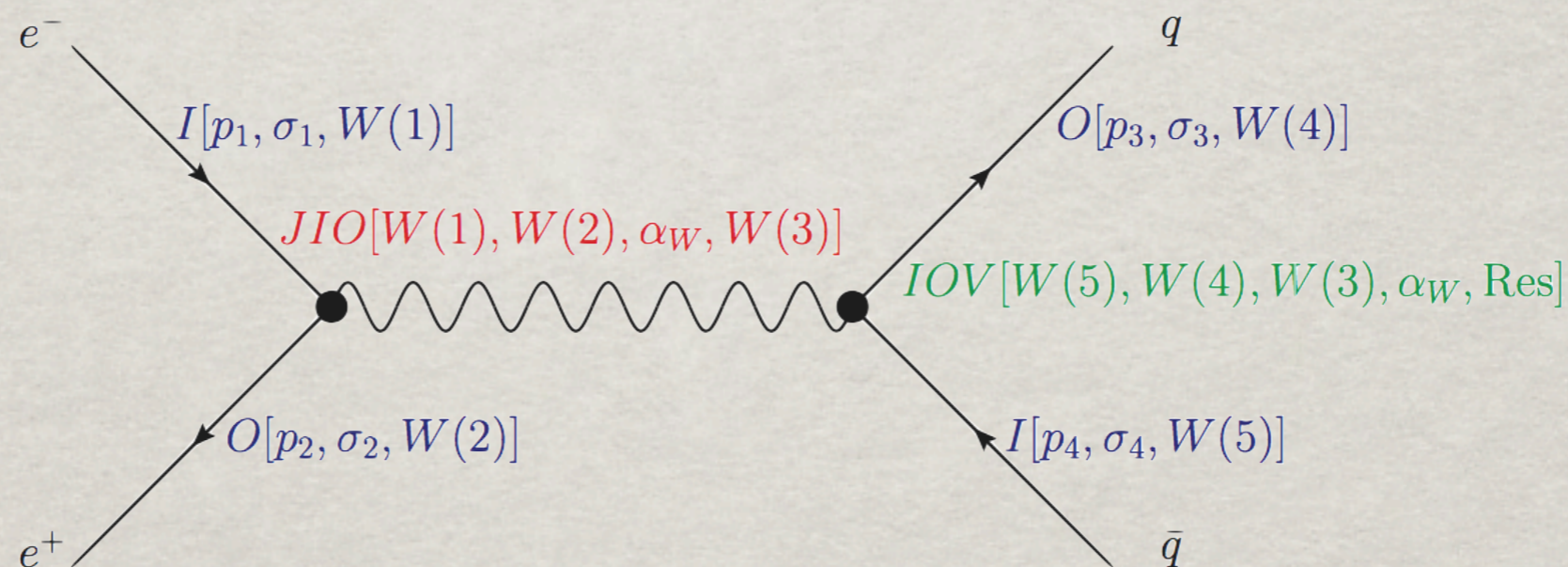


$$\text{Diag}_3 = [u^*(A)u^*(6)g^*(5)]$$

MADGRAPH

THE EVOLUTIVE WAY OF COMPUTING TREE-DIAGRAMS

- First generates all tree-level **Feynman Diagrams**
- Compute the **amplitude** of each diagram using a chain of calls to **HELAS** subroutines



- Finally **square** all the related amplitude with their right color factors to construct the **full LO amplitude**

CUTTOOLS

OR HOW TO COMPUTE LOOPS WITHOUT DOING SO

• **CutTools** uses the **OPP** method for loop reduction at the **integrand** level

$$\bar{q}^2 = q^2 + \tilde{q}^2 \quad (q \cdot \tilde{q}) = 0 \quad N(q) = \sum_{i_0 < i_1 < i_2 < i_3}^{m-1} \left[d(i_0 i_1 i_2 i_3) + \tilde{d}(q; i_0 i_1 i_2 i_3) \right] \prod_{i \neq i_0, i_1, i_2, i_3}^{m-1} D_i$$

$$\bar{D}_i = (\bar{q} + p_i)^2 - m_i^2, \quad p_0 \neq 0.$$

$$\int d^{(d)} \sigma^V = \int d^{(4+\epsilon)} \left(A(\bar{q}) + \tilde{A}(\bar{q}) \right)$$

$$A(\bar{q}) = \frac{N(q)}{\bar{D}_0 \bar{D}_1 \cdots \bar{D}_{m-1}} \quad \left(\tilde{A}(\bar{q}) \rightarrow \mathbf{R2} \right)$$

- R2 can be obtained with a tree-level-like computation with special Feynman-Rules.
- Evaluation of $N(q)$ for **different specific q 's** allows to algebraically obtain the coefficients a, b, c and d
- Reconstruction of the \tilde{q} dependance of the numerator gives the **cut-constructible part R1** of the finite part of the virtual amplitude

$$+ \sum_{i_0 < i_1 < i_2}^{m-1} \left[c(i_0 i_1 i_2) + \tilde{c}(q; i_0 i_1 i_2) \right] \prod_{i \neq i_0, i_1, i_2}^{m-1} D_i$$

$$+ \sum_{i_0 < i_1}^{m-1} \left[b(i_0 i_1) + \tilde{b}(q; i_0 i_1) \right] \prod_{i \neq i_0, i_1}^{m-1} D_i$$

$$+ \sum_{i_0}^{m-1} \left[a(i_0) + \tilde{a}(q; i_0) \right] \prod_{i \neq i_0}^{m-1} D_i$$

$$+ \tilde{P}(q) \prod_i^{m-1} D_i$$

$$\text{Finite part} = \mathbf{CC} + \mathbf{R1} + \mathbf{R2}$$

HANDLING BSM MODELS

UFO MODELS @ NLO

• Additional features in **UFO@NLO**:

CouplingOrder

- expansion_order
- perturbative_expansion
- hierarchy

CTVertices

```
V_GGZA = CTVertex(name = 'V_GGZA',  
                  particles = [P.G, P.G, P.Z, P.A],  
                  color = ['Tr(1, 2)'],  
                  lorentz = [L.R2_GGVV],  
                  loop_particles = [[[P.u], [P.c], [P.t]], [[P.d], [P.s], [P.b]]],  
                  couplings = {(0, 0, 0) : C.R2_GGZAup, (0, 0, 1) : C.R2_GGZAdown},  
                  type = 'R2')
```

CTParameters

```
MyCTParam = CTParameter(name = 'MyCTParam',  
                        type = 'real',  
                        value = {-1 : 'A', 0 : 'B'},  
                        texname = 'MadRules')
```

counterterm

attribute to Parameters and Particles

```
Param.GS.counterterm = {(1, 0, 0) : CTParam.G_UVq.value,  
                        (1, 0, 1) : CTParam.G_UVb.value,  
                        (1, 0, 2) : CTParam.G_UVt.value,  
                        (1, 0, 3) : CTParam.G_UVg.value}
```

AUTOMATIC LANGUAGE-INDEPENDENT OUTPUT OF HELICITY AMPLITUDE

O. Mattelaer *et al.* , [arXiv:1108.2041](https://arxiv.org/abs/1108.2041) [hep-ph]



FROM UFO TO MG5

ALOHA **translate** a UFO Lorentz structure

```
VVVV6 = Lorentz(name = 'VVVV6',  
                spins = [ 3, 3, 3, 3 ],  
                structure = 'Metric(1,4)*Metric(2,3) -Metric(1,3)*Metric(2,4)')
```

into pseudo-HELAS **subroutine** in a chosen language

```
VERTEX = COUP*( (V4(1)*( (V2(1)*( (0, -1)*(V3(2)*V1(2))  
$ +(0, -1)*(V3(3)*V1(3))+(0, -1)*(V3(4)*V1(4))))+(V1(1)*( (0, 1)  
$ *(V3(2)*V2(2))++(0, 1)*(V3(3)*V2(3))++(0, 1)*(V3(4)*V2(4))))))  
$ +( (V4(2)*( (V2(2)*( (0, -1)*(V3(1)*V1(1))++(0, 1)*(V3(3)*V1(3))  
$ +(0, 1)*(V3(4)*V1(4))))+(V1(2)*( (0, 1)*(V3(1)*V2(1))++(0,  
$ -1)*(V3(3)*V2(3))++(0, -1)*(V3(4)*V2(4)))))))+( (V4(3)*( (V2(3)  
$ *( (0, -1)*(V3(1)*V1(1))++(0, 1)*(V3(2)*V1(2))++(0, 1)*(V3(4)  
$ *V1(4))))+(V1(3)*( (0, 1)*(V3(1)*V2(1))++(0, -1)*(V3(2)*V2(2))  
$ +(0, -1)*(V3(4)*V2(4)))))))+(V4(4)*( (V2(4)*( (0, -1)*(V3(1)  
$ *V1(1))++(0, 1)*(V3(2)*V1(2))++(0, 1)*(V3(3)*V1(3))))+(V1(4)  
$ *( (0, 1)*(V3(1)*V2(1))++(0, -1)*(V3(2)*V2(2))++(0, -1)*(V3(3)  
$ *V2(3)))))))))  
END
```

Available in
Python, C++ and F77

ALOHA available as
a **standalone** release

NEW ON ALOHA

- **ALOHA** is **optimizing** the way it does analytical computation

Model name	Loading time, new ALOHA	Loading time, old ALOHA
SM	1.2 s	3 s
MSSM	1.4 s	5 s
Randall-Sundrum	90 s	15 min

- **Abbreviation** usage improves **compilation** and **running** time (up to **40%**)
- Possibility to create **ALOHA** subroutine **from the MG5 shell**

```
mg5> output aloha FFV1_3
```

- New **Outputs/Options** in progress (**Expected in the v2.0 public release**)

**Quadruple precision, Feynman Gauge, Spin 3/2,
Complex Mass Scheme, Open Loops techniques, anomalous couplings**

OPTIMIZATIONS

- **Summing over helicities first**, then reducing the **matrix element squared**.

$$\mathcal{M} = \sum_{l=loop} 2\Re\left(\sum_{h=hel} \underbrace{\text{CT}\left[\int \frac{d^D q \mathcal{N}_{l,h}}{D_0 D_1 \cdots D_{n-1}}\right]}_{\mathcal{A}_l} \mathcal{A}_h^*\right) \quad \Rightarrow \quad \mathcal{M} = \sum_{l=loop} 2\Re\left(\text{CT}\left[\int d^D q \frac{\sum_{h=hel} \sum_{b=born} \mathcal{N}_{l,h} \mathcal{A}_{b,h}^*}{D_0 D_1 \cdots D_{n-1}}\right]\right)$$

Also **grouping together** diagrams with the same denominator structures.

↳ **Result**: Number of OPP calls **decreases** from $N_{loops} \times N_{hels}$ to $N_{loop_topology}$!

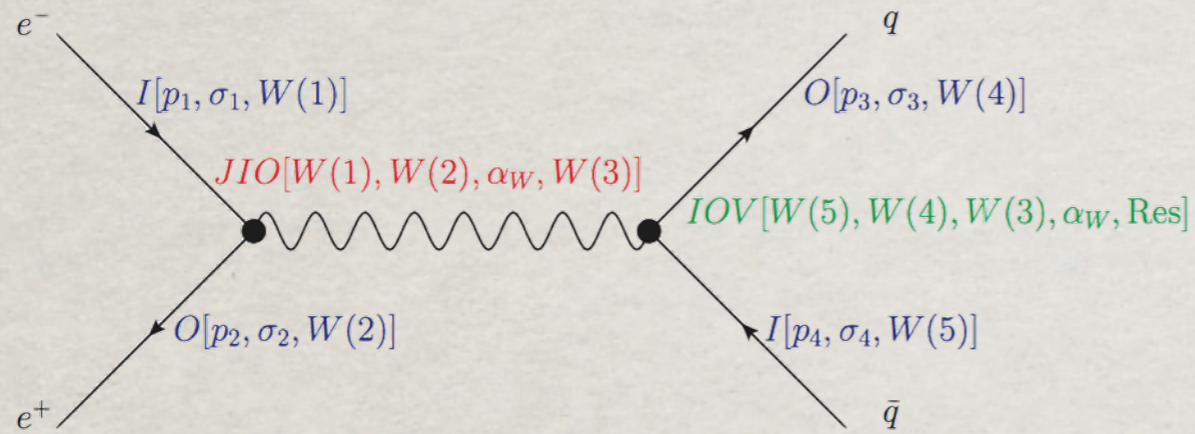
- Exploit the **open-loops**^[F.Cascioli,P.Maierhöfer,S.Pozzorini] technology.
 - ↳ **Faster** numerator evaluations.
 - ↳ **Optimal recycling** of the loop wavefunctions.
 - ↳ **Remains flexible** as ALOHA outputs the building blocks ^[Work by O.Mattelaer].
- Automatically **numerically** detect **zero** and **CP-dependent** helicity configurations.
- **Efficient reconstruction** the missing L-cut propagator. **Numerator 2 times faster** for the massless fermion loops and **3 times** for massive ones.

Overall speedup of a factor **10+** w.r.t **MLA**

FURTHER OPTIMIZATIONS

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- **Recycling** wavefunction accross helicity configurations

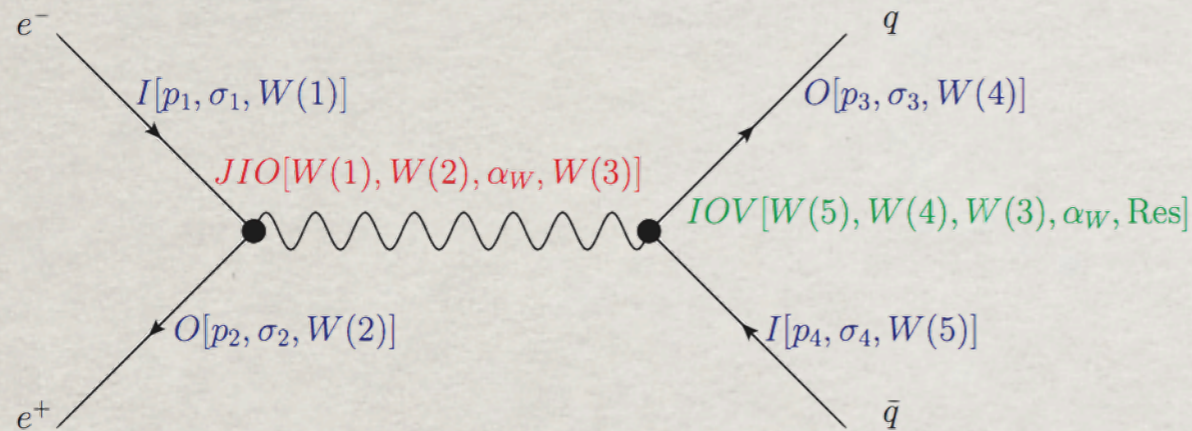


Ex. The same $JIO[e^+, e^-]$ can be used for the two helicity configs of $q \bar{q}$

Thanks to **open-loops**, the **loop wavefunctions** can also be **recycled**.

FURTHER OPTIMIZATIONS

- **Recycling** wavefunction accross helicity configurations



Ex. The same $JIO[e^+, e^-]$ can be used for the two helicity configs of $q \bar{q}$

Thanks to **open-loops**, the **loop wavefunctions** can also be **recycled**.

- **Grouping** diagrams with similar denominator structures

$$\int d^D q \frac{\mathcal{N}_A(q)}{\bar{D}_1 \bar{D}_{12} \bar{D}_{123} \bar{D}_{1234}} + \int d^D q \frac{\mathcal{N}_B(q)}{\bar{D}_1 \bar{D}_{12} \bar{D}_{1234}}$$

$$= \int d^D q \frac{\mathcal{N}_A(q) + \mathcal{N}_B(q) D_{123}}{\bar{D}_1 \bar{D}_{12} \bar{D}_{123} \bar{D}_{1234}}$$

A given triangle and its corresponding box can be **reduced at once!**

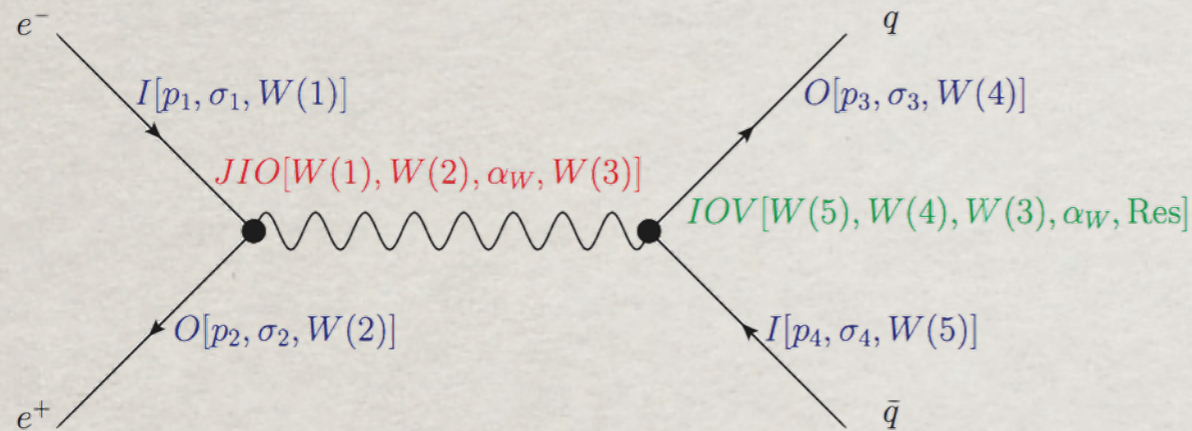
Ex: $g g > g g$ would require **only six** calls to **OPP**, one per box topology!

But tedious book-keeping and also needs care with dimensionality.

Only useful **if dominated by OPP!**

FURTHER OPTIMIZATIONS

- **Recycling** wavefunction accross helicity configurations



Ex. The same $JIO[e^+, e^-]$ can be used for the two helicity configs of $q \bar{q}$

Thanks to **open-loops**, the **loop wavefunctions** can also be **recycled**.

- **Grouping** diagrams with **similar denominator structures**

$$\int d^D q \frac{\mathcal{N}_A(q)}{\bar{D}_1 \bar{D}_{12} \bar{D}_{123} \bar{D}_{1234}} + \int d^D q \frac{\mathcal{N}_B(q)}{\bar{D}_1 \bar{D}_{12} \bar{D}_{1234}}$$

$$= \int d^D q \frac{\mathcal{N}_A(q) + \mathcal{N}_B(q) D_{123}}{\bar{D}_1 \bar{D}_{12} \bar{D}_{123} \bar{D}_{1234}}$$

A given triangle and its corresponding box can be **reduced at once!**

Ex: $g g > g g$ would require **only six** calls to **OPP**, one per box topology!

But tedious book-keeping and also needs care with dimensionality.

Only useful if dominated by OPP!

- Linking **MadLoop5** vs **Tensor Integral Reduction (TIR)**.

SPEED AND STABILITY

BENCHMARK WITH A CASE STUDY

Four families of $2 \rightarrow 2,3,4$ processes with $n=0,1,2$ gluons

- $u \bar{u} \rightarrow t \bar{t} + ng$
- $u \bar{u} \rightarrow W^+ W^- + ng$
- $u \bar{d} \rightarrow W^+ g + ng$
- $g g \rightarrow t \bar{t} + ng$

Same choice as in [arXiv:1111.5206](#)

Aim of the study

- Performance of **processes of interest** from LesHouches wish list
- Benchmark choice common among many codes: **easier comparison**
- Study of MadLoop5 **scaling** with leg multiplicity.

Running environment

- **Intel i5 2.8 GHz**, only one core exploited
- **gfortran -O0**, similar results with **gfortran -O5** and **ifort**

CODE GENERATION

Process	Exe. size [MB]	t_{code} [s]
$u \bar{u} \rightarrow t \bar{t}$	3.4	9.1
$u \bar{u} \rightarrow W^+ W^-$	3.5	12.4
$u \bar{d} \rightarrow W^+ g$	3.5	13.9
$g g \rightarrow t \bar{t}$	3.6	12.8
$u \bar{u} \rightarrow t \bar{t} g$	3.7	18
$u \bar{u} \rightarrow W^+ W^- g$	3.9	35
$u \bar{d} \rightarrow W^+ g g$	3.8	24
$g g \rightarrow t \bar{t} g$	4.2	62
$u \bar{u} \rightarrow t \bar{t} g g$	4.8	180
$u \bar{u} \rightarrow W^+ W^- g g$	4.8	204
$u \bar{d} \rightarrow W^+ g g g$	5.2	254
$g g \rightarrow t \bar{t} g g$	9.9*	1230
$u \bar{d} \rightarrow W^+ g g g g$	24**	9370

*,**: Color + helicity data = 25MB , 191 MB

Executable size: a few MB

Mild scaling with multiplicity.

Generation time < 1 hour

Not a limiting factor.

Could generate

$u \bar{d} \rightarrow W^+ g g g g$

or even

$g g \rightarrow g g g g$

SPEED OF ONE-LOOP AMPLITUDES

COLOR SUMMED, WITH OPP

Process	t_{pol} [ms]	n_{hel}	t_{unpol} [ms]
$u \bar{u} \rightarrow t \bar{t}$	0.52	3/16	0.72
$u \bar{u} \rightarrow W^+ W^-$	0.43	10/36	1.00
$u \bar{d} \rightarrow W^+ g$	0.87	6/24	1.51
$g g \rightarrow t \bar{t}$	2.51	6/16	5.42
$u \bar{u} \rightarrow t \bar{t} g$	7.44	16/32	27.5
$u \bar{u} \rightarrow W^+ W^- g$	9.3	36/72	81.8
$u \bar{d} \rightarrow W^+ g g$	13.5	12/48	36.9
$g g \rightarrow t \bar{t} g$	40.8	32/32	381
$u \bar{u} \rightarrow t \bar{t} g g$	142	32/64	1010
$u \bar{u} \rightarrow W^+ W^- g g$	166	72/144	2820
$u \bar{d} \rightarrow W^+ g g g$	260	24/96	1'310
$g g \rightarrow t \bar{t} g g$	826	64/64	16'900
$u \bar{d} \rightarrow W^+ g g g g$	9400	48/192	90'900

Polarized timing competitive

$$t_{2 \rightarrow 2} : t_{2 \rightarrow 3} : t_{2 \rightarrow 4} \lesssim 1 : 40 : 800 \text{ ms}$$

Unpolarized timing

Good enough for $2 \rightarrow 3$

Might need further improvement for $2 \rightarrow 4$

Higher multiplicity

$2 \rightarrow 5$ generation feasible

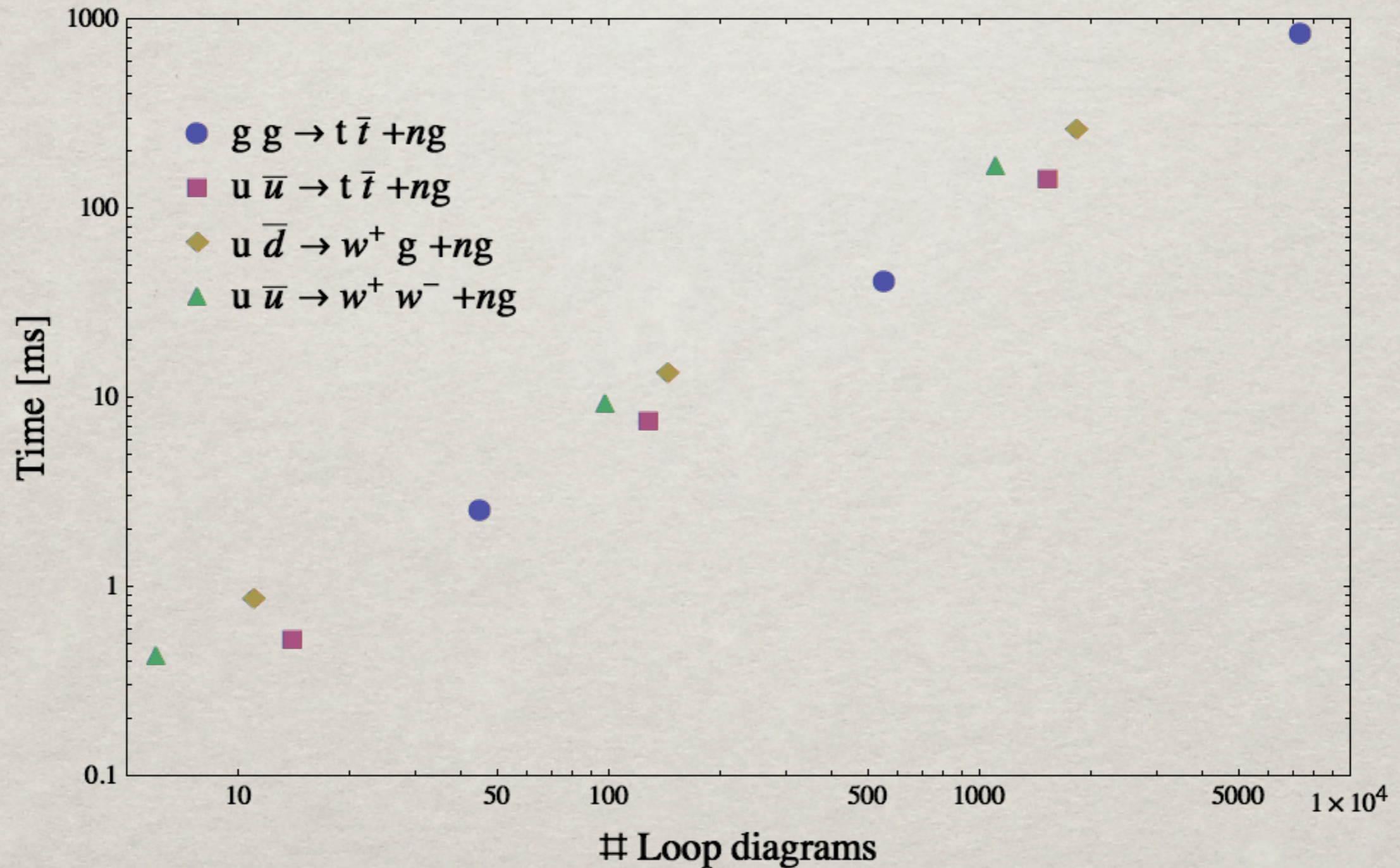
But evaluation is slow, so only useful to cross-check other codes

(Ex. $gg \rightarrow gggg$ successfully cross-checked vs NGLuon^[S. Badger])

LINEAR SCALING WITH # LOOP DIAGS

HIGHER RANK LOOPS APPEARING AT LARGER MULTIPLICITIES ARE NO OBSTACLE!

MadLoop5 polarized eval. time per PS point



NUMERICAL STABILITY WITH OPP

DOUBLE PRECISION IS NOT ALWAYS ENOUGH!

Stability probed by **two methods**:

- **Loop reading direction** : $D_0D_1\dots D_{n-1}D_n \rightarrow D_nD_{n-1}\dots D_1D_0$
↳ **Advantage**: The coefficients of $N(q)$ **need not be** recomputed.
- **Two PS point rotations** : $(E,x,y,z) \rightarrow (E,z,-x,-y)$ and $(E,x,y,z) \rightarrow (E,-z,y,x)$

Fraction of points with **less than 3 digits** accuracy:

$$2 \rightarrow 2 \quad << 10^{-3} \%$$

$$2 \rightarrow 3 \quad \sim 0.01 \%$$

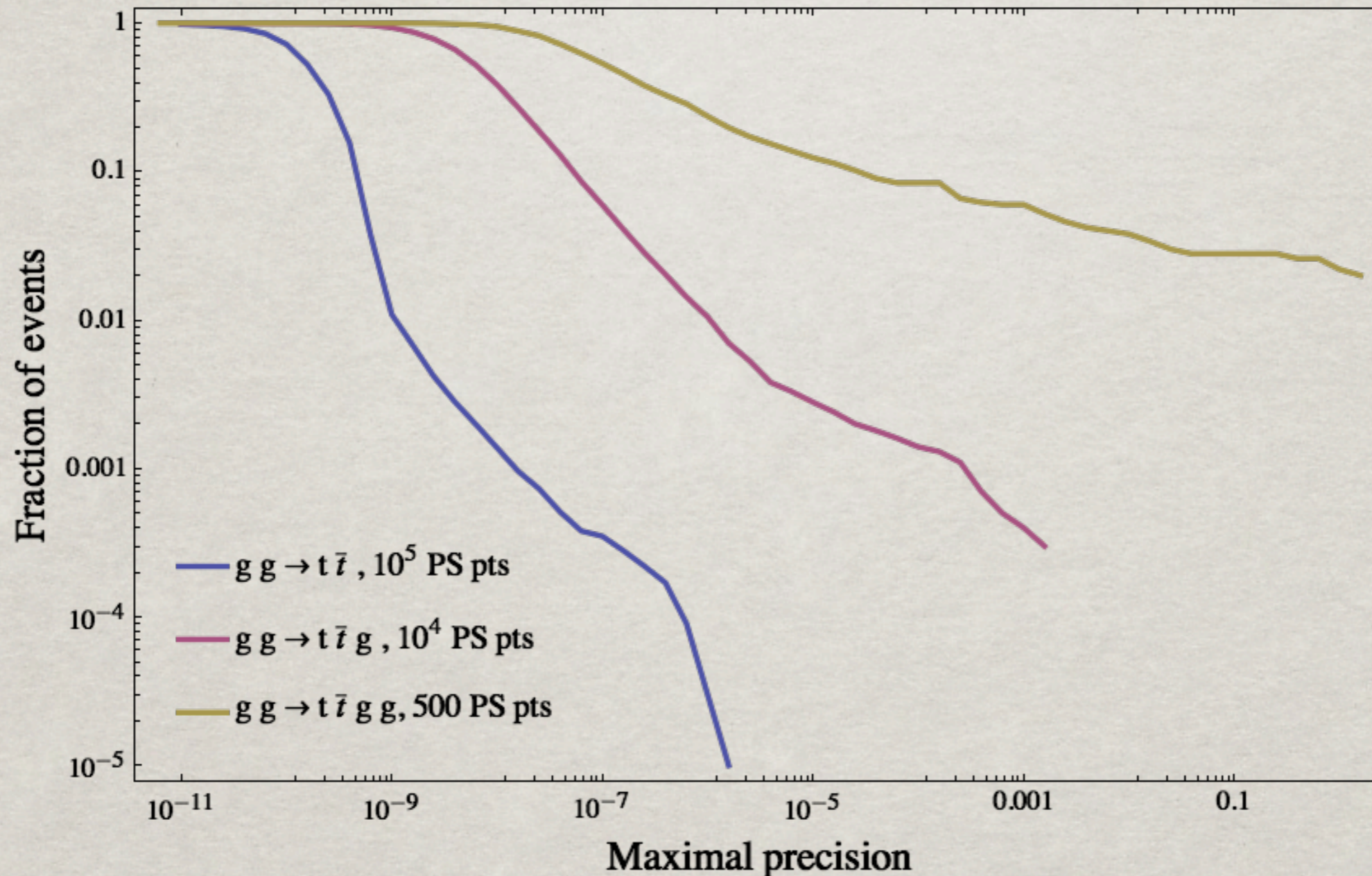
$$2 \rightarrow 4 \quad \sim 7 \% (!)$$

Further investigation necessary for **2 → 4**.

NUMERICAL STABILITY WITH OPP

2 > 4, PROBLEMS AHEAD...

Stability plot for $g g \rightarrow t \bar{t} + n g$



Uniformly distributed points with $\sqrt{s} = 1\text{TeV}$, $p_t > 50\text{ GeV}$ and $\Delta R_{ij} > 0.5$

NUMERICAL STABILITY WITH OPP

QUADRUPLE PRECISION SOLVES

- In general, accuracy is **worse** than with **Tensor Integral Reduction**
- Quadruple precision cures the **Unstable PS (UPS)** points but...
 - ... is **100 times slower!** (This is for complete qd, but double-double would be only 8 times slower)
 - ↳ So **1%** of UPS is already enough to **double** the integration time.
 - ... a very (very) small fraction of the points **will remain unstable.**
 - ↳ What to do with these **Exceptional PS points (EPS)**?
- Need to assess that the **stability tests** used are **accurate.**
- Also need to investigate possible **correlation** between **small weight of the ME** and the **unstability** of its evaluation.

MADLOOP V4 TO V5

GREAT IMPROVEMENTS

✓ = non-optimal | ✓ = done optimally | ✗ = not done | ✗ = not done YET

Task	MadLoop V4	MadLoop V5
Generation of L-Cut diagrams, loop-basis selection	✓-	✓++
Color Factor computation	✓-	✓
Counter-term (UV/R2) diagrams generation	✓-	✓
Mixed order perturbation (generation level)	✗	✓
File output and run-time speed	✓--	✓++
Drawing of Loop diagrams	✗	✓
4-gluon R2 computation	✗	✓
Automated parallel tests	✗	✓
Automatic output sanity checks (Ward, ϵ^2)	✓	✓
EPS handling	✓-- (no qp)	✓- (qp)
Virtual squared	✓-	✓
Decay Chains	✗	✗
Automatic loop-model creation	✗	✗
Complex mass scheme and massive bosons in the loop	✗	✓/✗

FUTURE PLANS AND CONCLUSION

NEXT ON PIPE-LINE

- Complete the **Stability study** of MadLoop5.
- **Publicly** release **MadGraph5 v2.0!**
- Exploit the tool for **phenomenology** studies.
- Implement a UFO loop model for **ElectroWeak corrections**.
- Implement some of the **further optimizations** discussed
- Automatic **Loop UFO Model** generation with **FeynRules**
- **Decay chains** specifications
- Case-study **SUSY** ? (If not already irrelevant by then)

THOUGHT-TO-BE FINAL WORD

BE READY TO TRY THE MADGRAPH V2.0 BY YOURSELF

MadLoop5 in MadGraph5 v2.0, a new 1-loop generator

- Numerical, diagrammatic, some recursive features
- Open-loops method exploited, *i.e.* loop-momentum polynomials
- PUBLIC release very soon (keep an eye on launchpad.net/madgraph5)

User-friendly, Automated, Flexible, Unique framework

- BSM model covered thanks to UFO and ALOHA flexibility.
- User-friendly thanks to MG5 interfaces.
- Fully automated, from the hard process output to event generation.

Fast, Stable

- Fast enough to cover today's processes of interest, 2 → 4 takes O(1s-3s)
- Stable thanks to quadruple precision when needed.

THANKS

MadGraph Home Page
madgraph.hep.uiuc.edu

NSF High Energy Physics Illinois
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Any opinions, findings, and conclusions or recommendations expressed in this material are those of the author(s) and do not necessarily reflect the views of the National Science Foundation

The MadGraph homepage
UCL UIUC Fermi
by the MG/ME Development team

Generate Process Register Tools My Database Cluster Status Downloads (needs registration) Wiki/Docs Admin

Generate processes online using MadGraph 5

To improve our web services we request that you register. Registration is quick and free. You may register for a password by clicking [here](#). Please note the correct reference for MadGraph 5, [JHEP 1106\(2011\)128](#), [arXiv:1106.0522 \[hep-ph\]](#). You can still use **MadGraph 4** [here](#).

Code can be generated either by:

I. Fill the form:

Model: LO [Model descriptions](#)
 NLO [Examples/format](#)

Input Process:

Example: $p p > w^+ j j$ QED=3, $w^+ > l^+ \nu_l$

p and j definitions:

sum over leptons:

We are very soon there!

ADDITIONAL SLIDES

PROCESS DETAILS

Process	unpol $t_{\text{coef}} / t_{\text{tot}}$	pol $t_{\text{coef}} / t_{\text{tot}}$	$n_{\text{loops}} / n_{\text{loop_groups}}$
$u \bar{u} \rightarrow t \bar{t}$	42%	20%	8 / 14
$u \bar{u} \rightarrow W^+ W^-$	69%	21%	5 / 6
$u \bar{d} \rightarrow W^+ g$	52%	16%	9 / 11
$g g \rightarrow t \bar{t}$	66%	25%	26 / 45
$u \bar{u} \rightarrow t \bar{t} g$	78%	18%	54 / 128
$u \bar{u} \rightarrow W^+ W^- g$	91%	24%	40 / 98
$u \bar{d} \rightarrow W^+ g g$	69%	17%	61 / 144
$g g \rightarrow t \bar{t} g$	92%	29%	164 / 556
$u \bar{u} \rightarrow t \bar{t} g g$	88%	22%	374 / 1530
$u \bar{u} \rightarrow W^+ W^- g g$	95%	25%	260 / 1108
$u \bar{d} \rightarrow W^+ g g g$	84%	20%	405 / 1827
$g g \rightarrow t \bar{t} g g$	97%	35%	1168 / 7356
$u \bar{d} \rightarrow W^+ g g g g$	94%	21%	3255 / 25666

DEFAULT VS OPEN-LOOP TIMINGS

MadLoop5 **opt vs default** polarized eval. time per PS point

