

The MadGraph5 Framework

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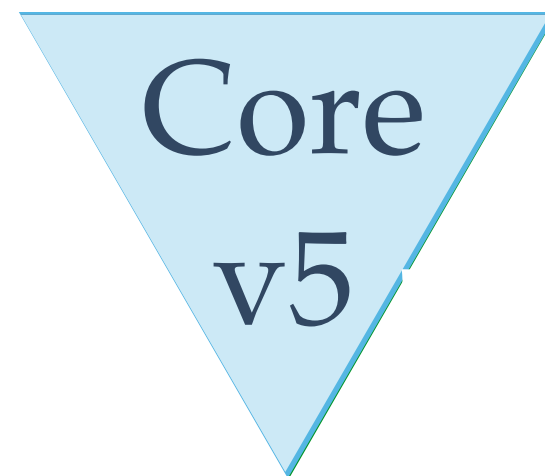
Plan

- MadGraph5
 - Status
 - Plan

Recap: “What is MG5”

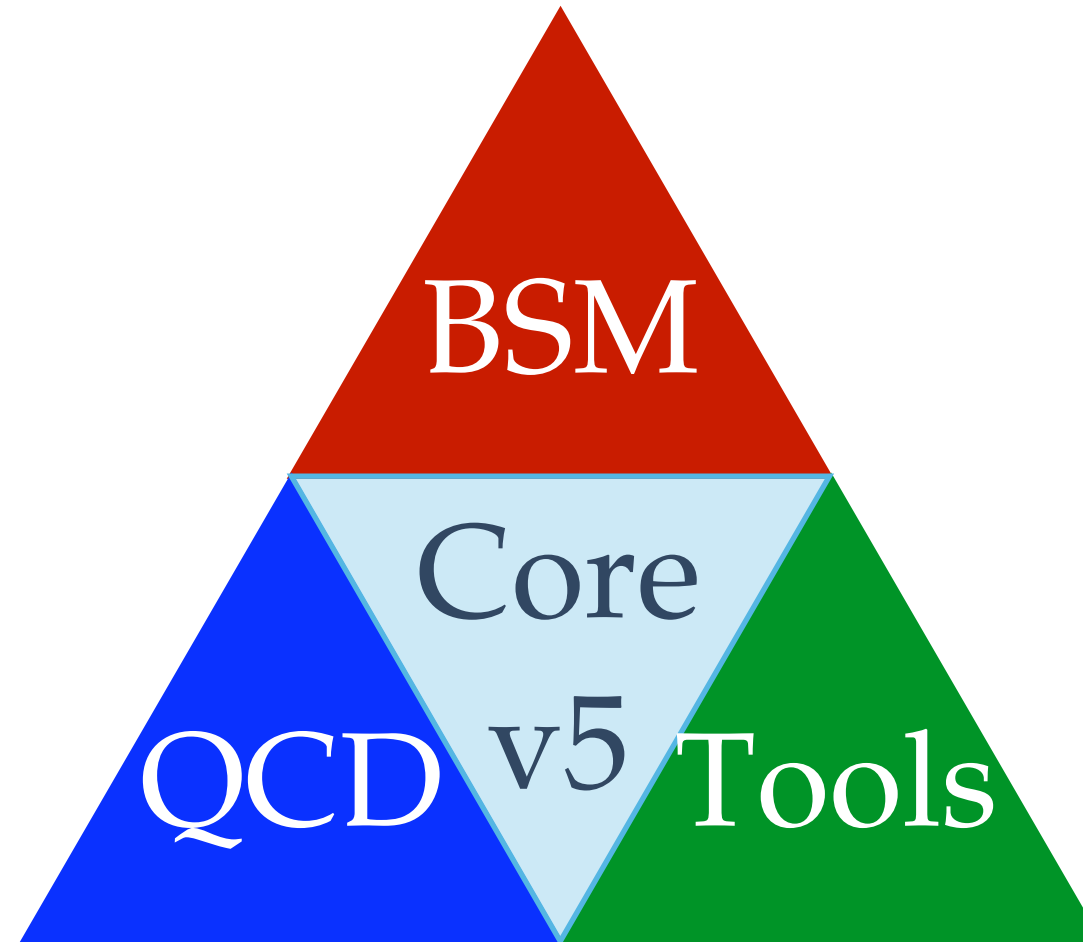
- MadGraph 5 is a completely new (released spring 2011) matrix element generator written in Python
- Can handle ANY model (that can be written as a Lagrangian), conveniently output by FeynRules
 - Any Lorentz structure for any spin (up to 2) and color (6tets, ϵ^{ijk})
 - Multiparticle vertices for any multiplicity, multifermion vertices
- Super fast process generation
- Unlimited-length decay chains with full BW and spin effects
- Event generation speedups by orders of magnitude
- Output in multiple languages and formats (including Pythia 8)
- Super-user-friendly command line interfaces

MadGraph 5



MadGraph 5

UFO / ALOHA



MADLOOP
MADFKS
aMC@NLO

MadSpin
MADWEIGHT
MadAnalysis5

MG Core

generate

Functionalities

Output

Tools

launch

MadGraph
StandAlone

UFO / ALOHA

MadLoop
StandAlone

Leading Order

- ☞ MadEvent
- ☞ MadWeight*
- ☞ To Pythia 8
- ☞ DarkMatter*

NLO

- ☞ MadKFS
- ☞ aMC@NLO

- ☞ MadAnalysis5
- ☞ MC@NLO
- ☞ MadSpin
- ☞ pythia-pgs
- ☞ Delphes

They are space for more !!

A Set of Tools



A Set of Tools



A Set of Tools



The perfect Tool box

- Need Modular Code (OO / Python)
 - Easy to add new features
- Use Launchpad to save progress
- Need **Extensive** test suite
 - If the tests **passes** the code **should** be stable
 - The **FIRST** debugging step is to add a new tests!
- Think as a **USER**

Command Interface

- Nice **Interactive** session
 - Auto-completion
 - Tutorial
 - interactive help
- Simple command set
 - **import** model sm
 - **generate** p p > e+ e-
 - **output** FORMAT MY_DIR
 - **launch** (-i)

```

*****
*
*           W E L C O M E  t o  M A D G R A P H  5
*
*           *                   *
*           *       * *       *
*           *   * * * 5 * * *
*           *       * *       *
*           *                   *
*
*           VERSION 1.3.16                2011-09-11
*
*           The MadGraph Development Team - Please visit us at
*           https://server06.fynu.ucl.ac.be/projects/madgraph
*
*           Type 'help' for in-line help.
*           Type 'tutorial' to learn how MG5 works
*
*****
load MG5 configuration from /Users/omatt/.mg5_config
Loading default model: sm
models.import_ufo: Restrict model sm with file models/sm/rest
models.import_ufo: Run "set stdout_level DEBUG" before import
INFO: Change particles name to pass to MG5 convention
Defined multiparticle p = g u c d s u~ c~ d~ s~
Defined multiparticle j = g u c d s u~ c~ d~ s~
Defined multiparticle l+ = e+ mu+
Defined multiparticle l- = e- mu-
Defined multiparticle vl = ve vm vt
Defined multiparticle vl~ = ve~ vm~ vt~
mg5>help

```

Core news since MG5 release - Quick list

- Lots of speedups and improvements, including
 - Vast speedup for long decay chains with multiparticle decays
 - Huge improvements in user interface
 - Multi cluster support
- MadSpin (**TODAY!!**) -- See next talk
- New 4-flavor matching and VBF-type matching
- 4 fermion vertices in FR+MG5 (except Majorana)
- Spin 3/2 particles in FR+MG5
- Complex mass scheme
- Feynman gauge
- Handling of negative weights
- On-the-fly 2-body decay width calculations (“Auto width”)

“LO” upcoming developments - Quick list

- Automatic matching to Pythia 8 (S. Pretzel et al)
 - CKKW-L matching
- Automatic scale/PDF/matching systematics (A. Kalogeropoulos et al)
- Fast multiparton processes using color-ordered recursion (J. Alwall et al)
- MadDecay: Automatic BSM decay width suite (including needed 3- and 4-body widths and decay of event file) (with C-H Shen et al)
- MadDM: Relic density calculations and direct detection limits for any BSM model (K.C. Kong et al)
- MadWeight5: Matrix-Element Method (P. Artoisenet, OM)

“NLO” upcoming developments - Quick list

- More Flexibility at Leading Order
- Interface to Pythia 8
- Automation of FxFx merging
- EW corrections (matched to the shower)
- Loop-induced
- UFO@NLO
- MadAnalysis5
- Loop BSM Library

See Other Talks !!!

Idea / Request

- BSM / SM Extension
 - Arbitrary gauge
 - Form Factor
 - arbitrary propagator
 - Majorana fermion in 4 Fermion interactions
- LHE Events Reweighting
- UserMod

Arbitrary Gauge

$$\eta_{\mu\nu} + \xi \frac{p_\mu p_\nu}{m^2}$$

- Current Status: Feynman/Unitary
- Do we need more?
 - Useful for test
- Need modification in the UFO
 - include the gauge parameter
- Need to modify the way to import model in MG5

Arbitrary propagator

- Interesting for Spin 2 and Spin 3/2
- Interesting for Gluon / Photon in unitary gauge
 - Allow to have a specialized propagator
- Interesting for some specific model
- Needed for open-loop
- Need an extension of UFO And ALOHA
- Need to modify the `helas_call_writer`

Form Factor

- Extend the valid input to ALOHA:
 - Example : HZA form factor interaction

```
HZA = FormFactor(name = 'HZA',
                 type = 'complex',
                 value = '2./3.*(3.-8.*SW2)/4./SW/CW*(1./2./((MH**2)/4./MT/MT-(P(-1,1)*P(-1,1))/4./MT/MT)+(1./2.*(1.-(MH**2)/4./MT/MT+(P(-1,1)*P(-1,1))/4./MT/MT)*(theta_function((P(-2,1)*P(-2,1))/4./MT/MT-1.,-1./4.*(cmath.log((1.+cmath.sqrt(1.-4.*MT*MT/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MT*MT/(P(-2,1)*P(-2,1)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((P(-2,1)*P(-2,1))/4./MT/MT)**2.))-theta_function((MH**2)/4./MT/MT-1.,-1./4.*(cmath.log((1.+cmath.sqrt(1.-4.*MT*MT/(MH**2))))/(1.-cmath.sqrt(1.-4.*MT*MT/(MH**2)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((MH**2)/4./MT/MT)**2.)))+(P(-1,1)*P(-1,1))/4./MT/MT*(theta_function((P(-2,1)*P(-2,1))/4./MT/MT-1.,1./2.*cmath.sqrt(1.-4.*MT*MT/(P(-2,1)*P(-2,1))))*(cmath.log((1.+cmath.sqrt(1.-4.*MT*MT/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MT*MT/(P(-2,1)*P(-2,1)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MT*MT/(P(-2,1)*P(-2,1))-1.)*cmath.asin(cmath.sqrt((P(-1,1)*P(-1,1))/4./MT/MT))-theta_function((MH**2)/4./MT/MT-1.,1./2.*cmath.sqrt(1.-4.*MT*MT/(MH**2)))*(cmath.log((1.+cmath.sqrt(1.-4.*MT*MT/(MH**2))))/(1.-cmath.sqrt(1.-4.*MT*MT/(MH**2)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MT*MT/(MH**2)-1.)*cmath.asin(cmath.sqrt((MH**2)/4./MT/MT)))/(MH**2)/4./MT/MT-(P(-1,1)*P(-1,1))/4./MT/MT**2)-1./3.*(4.*SW2-3.)/4./SW/CW*(1./2./((MH**2)/4./MB/MB-(P(-1,1)*P(-1,1))/4./MB/MB)+(1./2.*(1.-(MH**2)/4./MB/MB+(P(-1,1)*P(-1,1))/4./MB/MB)*(theta_function((P(-2,1)*P(-2,1))/4./MB/MB-1.,-0.25*(cmath.log((1.+cmath.sqrt(1.-4.*MB*MB/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MB*MB/(P(-2,1)*P(-2,1)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((P(-2,1)*P(-2,1))/4./MB/MB)**2.))-theta_function((MH**2)/4./MB/MB-1.,-0.25*(cmath.log((1.+cmath.sqrt(1.-4.*MB*MB/(MH**2))))/(1.-cmath.sqrt(1.-4.*MB*MB/(MH**2)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((MH**2)/4./MB/MB)**2.)))+(P(-1,1)*P(-1,1))/4./MB/MB*(theta_function((P(-2,1)*P(-2,1))/4./MB/MB-1.,1./2.*cmath.sqrt(1.-4.*MB*MB/(P(-2,1)*P(-2,1))))*(cmath.log((1.+cmath.sqrt(1.-4.*MB*MB/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MB*MB/(P(-2,1)*P(-2,1)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MB*MB/(P(-2,1)*P(-2,1))-1.)*cmath.asin(cmath.sqrt((P(-2,1)*P(-2,1))/4./MB/MB))-theta_function((MH**2)/4./MB/MB-1.,0.50*cmath.sqrt(1.-4.*MB*MB/(MH**2)))*(cmath.log((1.+cmath.sqrt(1.-4.*MB*MB/(MH**2))))/(1.-cmath.sqrt(1.-4.*MB*MB/(MH**2)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MB*MB/(MH**2)-1.)*cmath.asin(cmath.sqrt((MH**2)/4./MB/MB)))/(P(-5,3)**2)/4./MB/MB-(P(-1,1)*P(-1,1))/4./MB/MB**2.-CW/SW/8./((MH**2)/4./MW/MW - (P(-2,1)*P(-2,1))/4./MW/MW)*(5.-SW2/CW**2+2.*(MH**2)/4./MW/MW*(1.-SW2/CW**2))*(1.+2.*(P(-2,1)*P(-2,1))/4./MW/MW/(MH**2)/4./MW/MW-(P(-2,1)*P(-2,1))/4./MW/MW*(theta_function((P(-2,1)*P(-2,1))/4./MW/MW-1.,0.50*cmath.sqrt(1.-4.*MW*MW/(P(-2,1)*P(-2,1))))*(cmath.log((1.+cmath.sqrt(1.-4.*MW*MW/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MW*MW/(P(-2,1)*P(-2,1)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MW*MW/(P(-2,1)*P(-2,1))-1.)*cmath.asin(cmath.sqrt((P(-2,1)*P(-2,1))/4./MW/MW))-theta_function((MH**2)/4./MW/MW-1.,0.50*cmath.sqrt(1.-4.*MW*MW/(MH**2)))*(cmath.log((1.+cmath.sqrt(1.-4.*MW*MW/(MH**2))))/(1.-cmath.sqrt(1.-4.*MW*MW/(MH**2)))))-complex(0,1)*cmath.pi), cmath.sqrt(4.*MW*MW/(MH**2)-1.)*cmath.asin(cmath.sqrt((MH**2)/4./MW/MW)))+1./((MH**2)/4./MW/MW-(P(-2,1)*P(-2,1))/4./MW/MW*(4.*(P(-2,1)*P(-2,1))/4./MW/MW*(3.-SW2/CW**2)-(2.*(MH**2)/4./MW/MW-1.)*(5.-SW2/CW**2)))*(theta_function((P(-2,1)*P(-2,1))/4./MW/MW-1.,-0.25*(cmath.log((1.+cmath.sqrt(1.-4.*MW*MW/(P(-2,1)*P(-2,1))))/(1.-cmath.sqrt(1.-4.*MW*MW/(P(-1,1)*P(-1,1)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((P(-1,1)*P(-1,1))/4./MW/MW)**2.))-theta_function((MH**2)/4./MW/MW-1.,-0.25*(cmath.log((1.+cmath.sqrt(1.-4.*MW*MW/(MH**2))))/(1.-cmath.sqrt(1.-4.*MW*MW/(MH**2)))))-complex(0,1)*cmath.pi)**2., cmath.asin(cmath.sqrt((MH**2)/4./MW/MW)**2.))'
```

- Validated on this example (and on h g g)
- fast (0.36 s to 0.75 s)



```

TMP1 = (PI(0)*V2(3)-PI(1)*V2(4)-PI(2)*V2(5)-
PI(3)*V2(6))
TMP0 = (PI(0)*PI(0)-PI(1)*PI(1)-PI(2)*PI(2)-
PI(3)*PI(3))
TMP3 = (V2(3)*V1(3)-V2(4)*V1(4)-V2(5)*V1(5)-
V2(6)*V1(6))
TMP2 = (V1(3)*P2(0)-V1(4)*P2(1)-V1(5)*P2(2)-
V1(6)*P2(3))
FCT0 = ID0/(SW)
FCT1 = ID0/(CW)
FCT2 = (MH)**(2D0)
FCT3 = ID0/(MT)
FCT4 = ID0/(ID0/4D0 * FCT3*FCT3*(FCT2-TMP0))
FCT5 = ID0/(TMP0)
FCT6 = SQRT(DBLE(-ID0*(+4D0*(MT*MT*FCT5)+
-ID0)))
FCT7 = ID0/((-FCT6+ ID0))
FCT8 = LOG(DBLE(FCT7*(FCT6+ ID0)))
FCT9 = (-ID0*(+CI*(PI)-FCT8)**(2D0)
FCT10 = SQRT(DBLE(ID0/4D0 *
TMP0*FCT3*FCT3))
FCT11 = ASIN(DBLE(FCT10))
FCT12 = (FCT11)**(2D0)
FCT13 =
THETA_FUNCTION((+ID0/4D0*(FCT3*FCT3*TMP0)+
-ID0),
$ -ID0/4D0 * FCT9,FCT12)
FCT14 = ID0/(FCT2)
FCT15 =
SQRT(DBLE(-ID0*(+4D0*(MT*MT*FCT14)+ -ID0)))
FCT16 = ID0/((-FCT15+ ID0))
FCT17 = LOG(DBLE(FCT16*(FCT15+ ID0)))
FCT18 = (-ID0*(+CI*(PI)-FCT17)**(2D0)
FCT19 = SQRT(DBLE(ID0/4D0 *
FCT3*FCT3*FCT2))
FCT20 = ASIN(DBLE(FCT19))
FCT21 = (FCT20)**(2D0)
FCT22 =
THETA_FUNCTION((+ID0/4D0*(FCT3*FCT3*FCT2)+
-ID0),
$ -ID0/4D0 * FCT18,FCT21)
FCT23 =
THETA_FUNCTION((+ID0/4D0*(FCT3*FCT3*TMP0)+
-ID0),ID0
$ /2D0 * FCT6*(FCT8-CI*(PI)),FCT11*FCT6)
FCT24 =
THETA_FUNCTION((+ID0/4D0*(FCT3*FCT3*FCT2)+
-ID0),ID0
$ /2D0 * FCT15*(FCT17-CI*(PI)),FCT20*FCT15)
FCT25 = (ID0/4D0 * FCT3*FCT3*(FCT2-
TMP0)**(2D0)
FCT26 = ID0/(FCT25)
FCT27 = ID0/(MB)
FCT28 = ID0/(ID0/4D0 * FCT27*FCT27*(FCT2-
TMP0))
FCT29 = SQRT(DBLE(-ID0*(+4D0*(FCT5*MB*MB)+
-ID0)))
FCT30 = ID0/((-FCT29+ ID0))
FCT31 = LOG(DBLE(FCT30*(FCT29+ ID0)))
FCT32 = (-ID0*(+CI*(PI)-FCT31)**(2D0)
FCT33 = SQRT(DBLE(ID0/4D0 *
TMP0*FCT27*FCT27))
FCT34 = ASIN(DBLE(FCT33))
FCT35 = (FCT34)**(2D0)
FCT36 =
THETA_FUNCTION((+ID0/4D0*(TMP0*FCT27*FCT27)
+ -ID0),
$ -ID0/4D0 * FCT32,FCT35)
FCT37 = SQRT(DBLE(-ID0*(+4D0*(FCT14*MB*MB)
+ -ID0)))
FCT38 = ID0/((-FCT37+ ID0))
FCT39 = LOG(DBLE(FCT38*(FCT37+ ID0)))
FCT40 = (-ID0*(+CI*(PI)-FCT39)**(2D0)
FCT41 = SQRT(DBLE(ID0/4D0 *
FCT27*FCT27*FCT2))
FCT42 = ASIN(DBLE(FCT41))
FCT43 = (FCT42)**(2D0)
FCT44 =
THETA_FUNCTION((+ID0/4D0*(FCT2*FCT27*FCT27)
+ -ID0),
$ -ID0/4D0 * FCT40,FCT43)
FCT45 =
THETA_FUNCTION((+ID0/4D0*(TMP0*FCT27*FCT27)
+ -ID0),ID0
$ /2D0 * FCT29*(FCT31-CI*(PI)),FCT34*FCT29)
FCT46 =
THETA_FUNCTION((+ID0/4D0*(FCT2*FCT27*FCT27)
+ -ID0),ID0
$ /2D0 * FCT37*(FCT39-CI*(PI)),FCT42*FCT37)
FCT47 = (P3(0))**(2D0)
FCT48 = (ID0/4D0 * FCT27*FCT27*(FCT47-
TMP0)**(2D0)
FCT49 = ID0/(FCT48)
FCT50 = ID0/(MW)
FCT51 = ID0/(ID0/4D0 * FCT50*FCT50*(FCT2-
TMP0))
FCT52 = (CW)**(2D0)
FCT53 = ID0/(FCT52)
FCT54 =
SQRT(DBLE(-ID0*(+4D0*(FCT5*MW*MW)+ -ID0)))
FCT55 = ID0/((-FCT54+ ID0))
FCT56 = LOG(DBLE(FCT55*(FCT54+ ID0)))
FCT57 = SQRT(DBLE(ID0/4D0 *
TMP0*FCT50*FCT50))
FCT58 = ASIN(DBLE(FCT57))
FCT59 =
THETA_FUNCTION((+ID0/4D0*(TMP0*FCT50*FCT50)
+ -ID0),ID0
$ /2D0 * FCT54*(FCT56-CI*(PI)),FCT58*FCT54)
FCT60 =
SQRT(DBLE(-ID0*(+4D0*(FCT14*MW*MW)+ -ID0)))
FCT61 = ID0/((-FCT60+ ID0))
FCT62 = LOG(DBLE(FCT61*(FCT60+ ID0)))
FCT63 = SQRT(DBLE(ID0/4D0 *
FCT50*FCT50*FCT2))
FCT64 = ASIN(DBLE(FCT63))
FCT65 =
THETA_FUNCTION((+ID0/4D0*(FCT2*FCT50*FCT50)
+ -ID0),ID0
$ /2D0 * FCT60*(FCT62-CI*(PI)),FCT64*FCT60)
FCT66 = (-ID0*(+CI*(PI)-FCT56)**(2D0)
FCT67 = (FCT58)**(2D0)
FCT68 =
THETA_FUNCTION((+ID0/4D0*(TMP0*FCT50*FCT50)
+ -ID0),
$ -ID0/4D0 * FCT66,FCT67)
FCT69 = (-ID0*(+CI*(PI)-FCT62)**(2D0)
FCT70 = (FCT64)**(2D0)
FCT71 =
THETA_FUNCTION((+ID0/4D0*(FCT2*FCT50*FCT50)
+ -ID0),
$ -ID0/4D0 * FCT69,FCT70)
VERTEX = COUP*ID0/16D0 *
FCT0*S3(3)*(FCT1*(TMP1*TMP2*(SW2*(FCT26
*(FCT3*FCT3*(TMP0*8D0/3D0*(-
CI*(FCT22)+CI*(FCT13)-2D0 * CI
*(FCT24)+2D0 * CI*(FCT23))+8D0/3D0*(FCT2*(-
CI*(FCT13)+CI
*(FCT22)))))+(-32D0/3D0 * CI*(FCT22)+32D0/3D0 *
CI*(FCT13)))
$ +(FCT49*(FCT27*FCT27*(TMP0*2D0/3D0*(-
CI*(FCT44)+CI*(FCT36)
-2D0 * CI*(FCT46)+2D0 * CI*(FCT45))
+2D0/3D0*(FCT2*(-CI*(FCT36)
+CI*(FCT44)))))+(-8D0/3D0 * CI*(FCT44)+8D0/3D0
* CI*(FCT36)))+(
$ +8D0/3D0 * CI*(FCT28)+32D0/3D0 * CI*(FCT4)))
+(FCT26*(FCT3*FCT3
*(TMP0*(-CI*(FCT13)+CI*(FCT22)-2D0 *
CI*(FCT23)+2D0 * CI
*(FCT24))+FCT2*(-CI*(FCT22)+CI*(FCT13)))+(
+4D0 * CI*(FCT22)
$ -4D0 * CI*(FCT13)))+(FCT49*(FCT27*ID0/2D0 *
FCT27*(FCT2*(-
CI*(FCT44)+CI*(FCT36))+2D0*(TMP0*ID0/2D0*(-
CI*(FCT36)
$ +CI*(FCT44)-2D0 * CI*(FCT45)+2D0 *
CI*(FCT46)))+(-2D0 * CI
*(FCT36)+2D0 * CI*(FCT44)))+(-2D0 *
CI*(FCT28)-4D0 * CI
*(FCT4))))
+TMP3*TMP4*(SW2*(FCT26*(FCT3*FCT3*(TMP0*8D0/3
D0*(-
CI*(FCT13)+CI*(FCT22)-2D0 * CI*(FCT23)+2D0 *
CI*(FCT24)
$ +8D0/3D0*(FCT2*(-CI*(FCT22)+CI*(FCT13))))+
(-32D0/3D0 * CI
*(FCT13)+32D0/3D0 * CI*(FCT22)))+(
FCT49*(FCT27*FCT27*(TMP0
$ 2D0/3D0*(-CI*(FCT36)+CI*(FCT44)-2D0 *
CI*(FCT45)+2D0 * CI
*(FCT46))+2D0/3D0*(FCT2*(-
CI*(FCT44)+CI*(FCT36)))+(-8D0/3D0
$ * CI*(FCT36)+8D0/3D0 * CI*(FCT44)))+(
(-32D0/3D0 * CI*(FCT4)
$ -8D0/3D0 * CI*(FCT28))))+(
(FCT26*(FCT3*FCT3*(TMP0*(-CI*(FCT22)
$ +CI*(FCT13)-2D0 * CI*(FCT24)+2D0 * CI*(FCT23))
+FCT2*(-CI

```

4 Fermion with Majorana

- IOIO convention didn't work for 4 fermion vertex with identical particles.
- how distinguish $e^+ e^- e^+ e^-$ and $e^+ e^- e^+ e^-$
- IOIO is needed for defining the conjugate routine.
- Need to modify the flow information in MG5

LHE Reweighting

- Taking a LHE event (unweighted or not)
 - assign a weight to each event according to a new theoretical hypothesis
- Nothing deep is needed (just an interface)

UserMod

- usermod V4 is still use A LOT
 - Do we want to keep v4 model for ever?
- Do we want to give a easy frameworks to customize a model?

Conclusion

- MG5 is a Framework for Matrix Element Work
- Waiting for **YOUR** idea / implementation
- Lot of development going on.
- <https://launchpad.net/madgraph5>

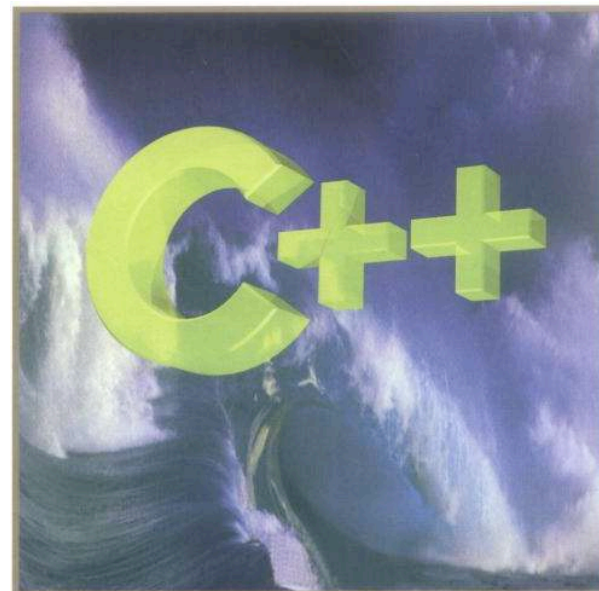
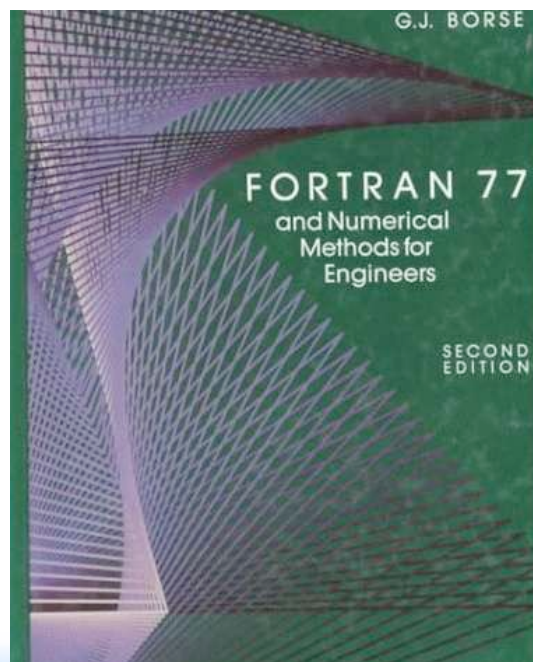


ALOHA

~~ALOHA
Google translate~~

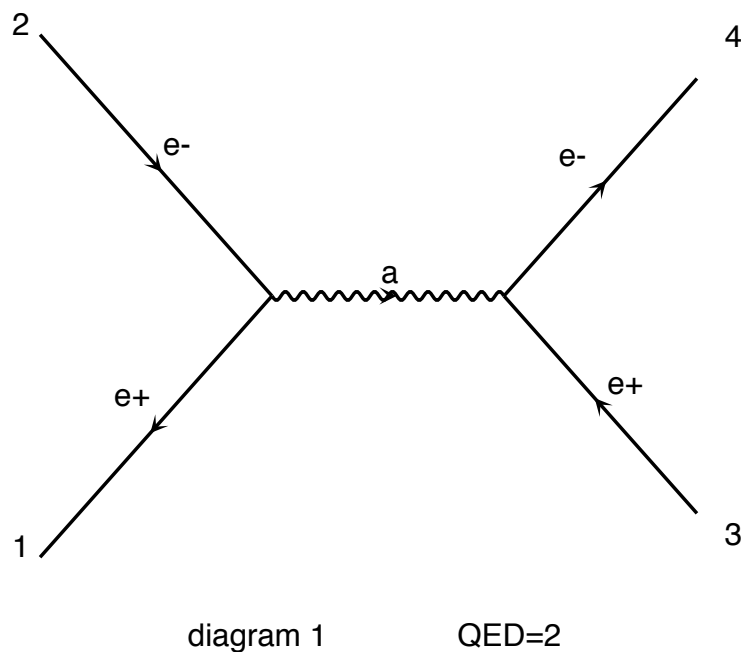
From: [UFO] To: Helicity [Translate]

Type text or a website address or translate a document.



HELAS

- **Idea:** Evaluate m for fixed helicity of external particles.



$$M = \bar{u}\gamma^\mu v P_{\mu\nu} \bar{u}\gamma^\nu v$$

HELAS

- **Idea:** Evaluate m for fixed helicity of external particles.

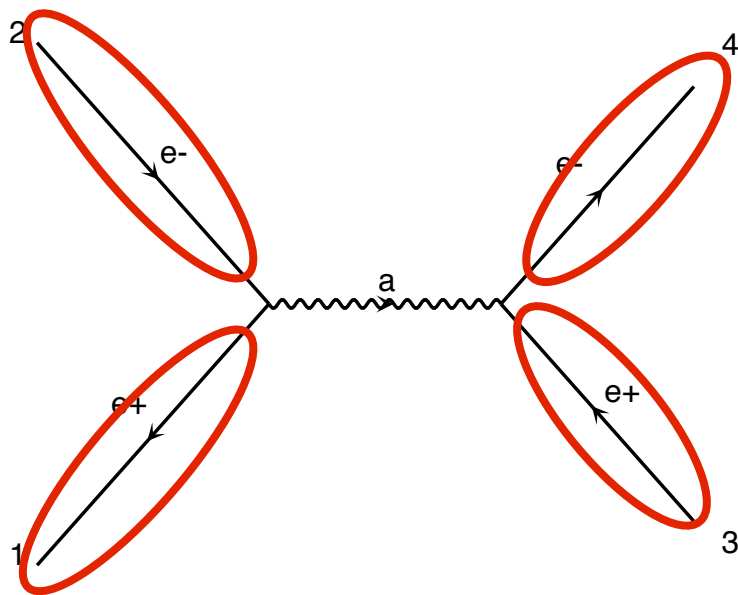


diagram 1

QED=2

$$M = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

→ Number for a given helicity

```
CALL IXXXXX(P(0,1),ZERO,NHEL(1),+1*IC(1),W(1,1))
CALL OXXXXX(P(0,2),ZERO,NHEL(2),-1*IC(2),W(1,2))
CALL OXXXXX(P(0,3),MT,NHEL(3),+1*IC(3),W(1,3))
CALL IXXXXX(P(0,4),MT,NHEL(4),-1*IC(4),W(1,4))
```

HELAS

- **Idea:** Evaluate m for fixed helicity of external particles.

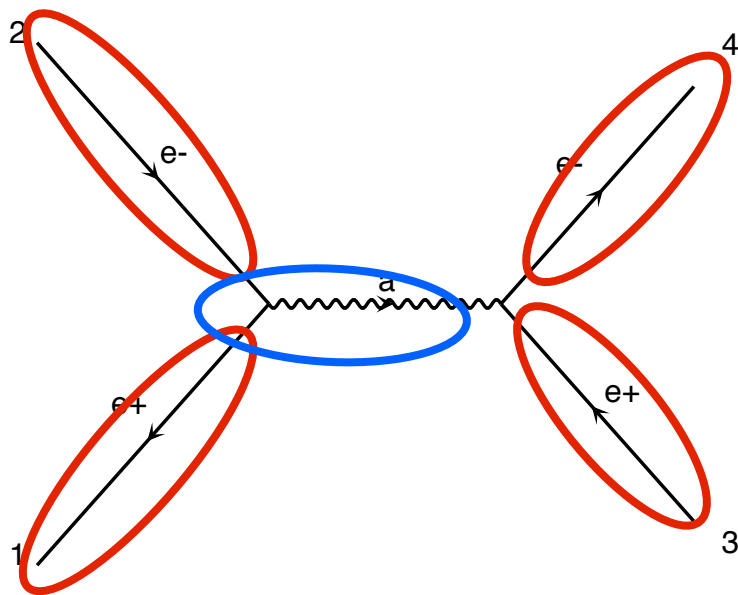


diagram 1

QED=2

$$M = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

→ Number for a given helicity

→ Evaluate interaction by
interaction

```
CALL IXXXXX(P(0,1),ZERO,NHEL(1),+1*IC(1),W(1,1))
CALL OXXXXX(P(0,2),ZERO,NHEL(2),-1*IC(2),W(1,2))
CALL OXXXXX(P(0,3),MT,NHEL(3),+1*IC(3),W(1,3))
CALL IXXXXX(P(0,4),MT,NHEL(4),-1*IC(4),W(1,4))
CALL JIXXXX(W(1,1),W(1,2),GG,ZERO,ZERO,W(1,5))
```

HELAS

- **Idea:** Evaluate m for fixed helicity of external particles.

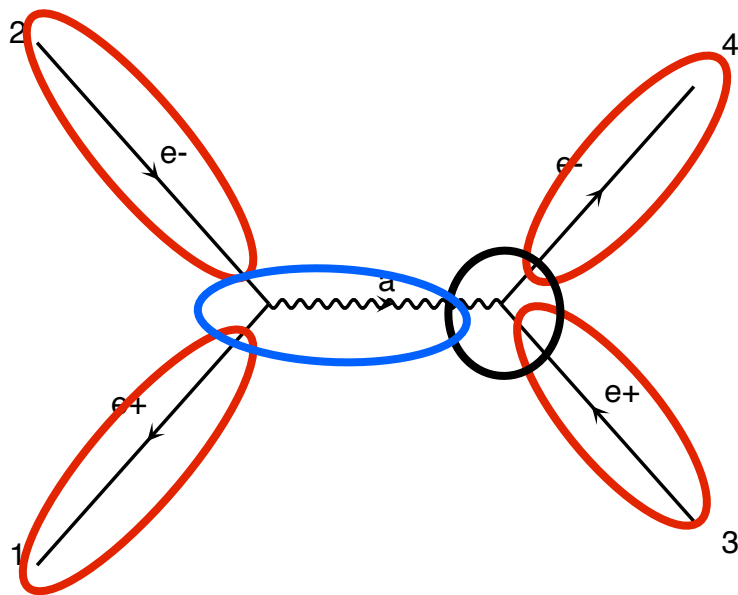


diagram 1

QED=2

$$M = \bar{u} \gamma^\mu v P_{\mu\nu} \bar{u} \gamma^\nu v$$

→ Number for a given helicity

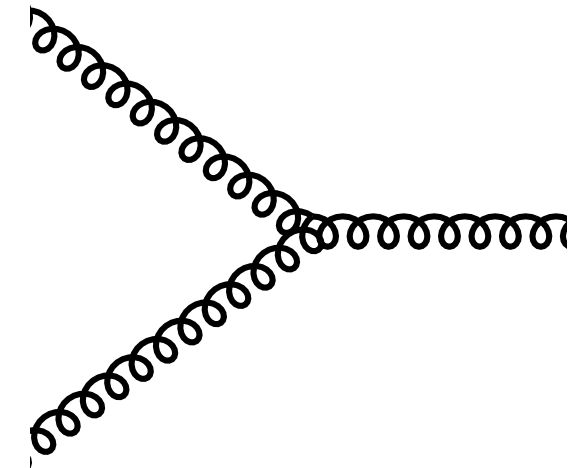
→ Evaluate interaction by
interaction

```
CALL IXXXXX(P(0,1),ZERO,NHEL(1),+1*IC(1),W(1,1))
CALL OXXXXX(P(0,2),ZERO,NHEL(2),-1*IC(2),W(1,2))
CALL OXXXXX(P(0,3),MT,NHEL(3),+1*IC(3),W(1,3))
CALL IXXXXX(P(0,4),MT,NHEL(4),-1*IC(4),W(1,4))
CALL JIXXXX(W(1,1),W(1,2),GG,ZERO,ZERO,W(1,5))
CALL IOVXXX(W(1,4),W(1,3),W(1,5),GG,AMP(1))
```



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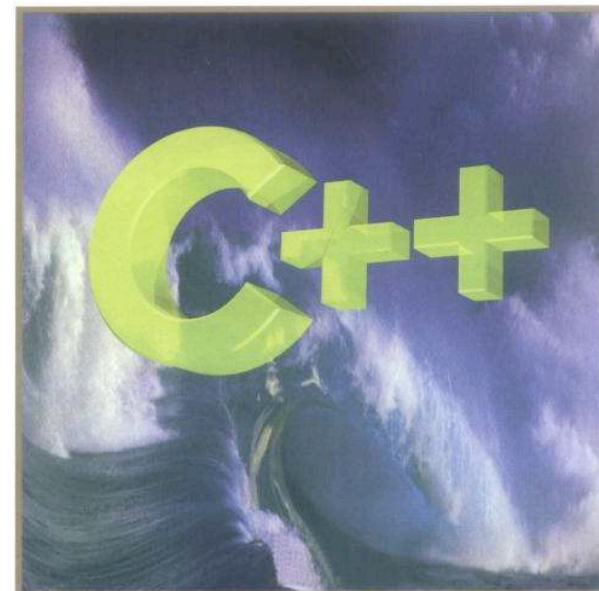
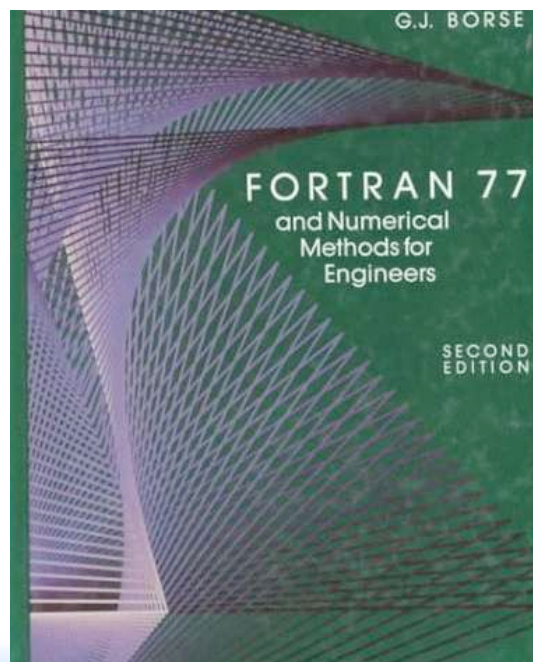
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From: [UFO] To: Helicity [Translate]

$$\begin{aligned}
 &P(3,1)*Metric(1,2) - P(3,2)*Metric(1,2) - \\
 &P(2,1)*Metric(1,3) + P(2,3)*Metric(1,3) + \\
 &P(1,2)*Metric(2,3) - P(1,3)*Metric(2,3)'
 \end{aligned}$$

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Amplitude

$$\begin{aligned}
 \text{TMP8} &= (V1(3)*P3(0)-V1(4)*P3(1)-V1(5)*P3(2)-V1(6)*P3(3)) \\
 \text{TMP5} &= (V2(3)*P3(0)-V2(4)*P3(1)-V2(5)*P3(2)-V2(6)*P3(3)) \\
 \text{TMP4} &= (P1(0)*V2(3)-P1(1)*V2(4)-P1(2)*V2(5)-P1(3)*V2(6)) \\
 \text{TMP7} &= (V1(3)*P2(0)-V1(4)*P2(1)-V1(5)*P2(2)-V1(6)*P2(3)) \\
 \text{TMP6} &= (V3(3)*V2(3)-V3(4)*V2(4)-V3(5)*V2(5)-V3(6)*V2(6)) \\
 \text{TMP1} &= (V2(3)*V1(3)-V2(4)*V1(4)-V2(5)*V1(5)-V2(6)*V1(6)) \\
 \text{TMP0} &= (V3(3)*P1(0)-V3(4)*P1(1)-V3(5)*P1(2)-V3(6)*P1(3)) \\
 \text{TMP3} &= (V3(3)*V1(3)-V3(4)*V1(4)-V3(5)*V1(5)-V3(6)*V1(6)) \\
 \text{TMP2} &= (V3(3)*P2(0)-V3(4)*P2(1)-V3(5)*P2(2)-V3(6)*P2(3)) \\
 \text{VERTEX} &= \text{COUP}*(\text{TMP1}*(-\text{CI}*(\text{TMP0})+\text{CI}*(\text{TMP2}))+(\text{TMP3}*(-\text{CI}*(\text{TMP5}) \\
 &\$ +\text{CI}*(\text{TMP4}))+\text{TMP6}*(-\text{CI}*(\text{TMP7})+\text{CI}*(\text{TMP8}))))
 \end{aligned}$$

Wave-function

$$\begin{aligned}
 \text{TMP5} &= (P1(0)*P2(0)-P1(1)*P2(1)-P1(2)*P2(2)-P1(3)*P2(3)) \\
 \text{TMP4} &= (V3(3)*V2(3)-V3(4)*V2(4)-V3(5)*V2(5)-V3(6)*V2(6)) \\
 \text{TMP6} &= (P1(0)*P3(0)-P1(1)*P3(1)-P1(2)*P3(2)-P1(3)*P3(3)) \\
 \text{TMP1} &= (P1(0)*V2(3)-P1(1)*V2(4)-P1(2)*V2(5)-P1(3)*V2(6)) \\
 \text{TMP0} &= (V3(3)*P1(0)-V3(4)*P1(1)-V3(5)*P1(2)-V3(6)*P1(3)) \\
 \text{TMP3} &= (V2(3)*P3(0)-V2(4)*P3(1)-V2(5)*P3(2)-V2(6)*P3(3)) \\
 \text{TMP2} &= (V3(3)*P2(0)-V3(4)*P2(1)-V3(5)*P2(2)-V3(6)*P2(3)) \\
 \text{DENOM} &= \text{COUP}/(P1(0)**2-P1(1)**2-P1(2)**2-P1(3)**2 - M1 * (M1 \\
 &\$ -\text{CI} * W1)) \\
 V1(3) &= \text{DENOM}*(\text{OM1}*P1(0)*(\text{TMP4}*(-\text{CI}*(\text{TMP6})+\text{CI}*(\text{TMP5}))+(-\text{CI}*(\text{TMP1} \\
 &\$ * \text{TMP2})+\text{CI}*(\text{TMP0}*\text{TMP3}))+(\text{TMP4}*(-\text{CI}*(P2(0))+\text{CI}*(P3(0)))) \\
 &\$ +(V2(3)*(-\text{CI}*(\text{TMP0})+\text{CI}*(\text{TMP2}))+V3(3)*(-\text{CI}*(\text{TMP3})+\text{CI}*(\text{TMP1)))))) \\
 V1(4) &= \text{DENOM}*(\text{OM1}*P1(1)*(\text{TMP4}*(-\text{CI}*(\text{TMP6})+\text{CI}*(\text{TMP5}))+(-\text{CI}*(\text{TMP1} \\
 &\$ * \text{TMP2})+\text{CI}*(\text{TMP0}*\text{TMP3}))+(\text{TMP4}*(-\text{CI}*(P2(1))+\text{CI}*(P3(1)))) \\
 &\$ +(V2(4)*(-\text{CI}*(\text{TMP0})+\text{CI}*(\text{TMP2}))+V3(4)*(-\text{CI}*(\text{TMP3})+\text{CI}*(\text{TMP1)))))) \\
 V1(5) &= \text{DENOM}*(\text{OM1}*P1(2)*(\text{TMP4}*(-\text{CI}*(\text{TMP6})+\text{CI}*(\text{TMP5}))+(-\text{CI}*(\text{TMP1} \\
 &\$ * \text{TMP2})+\text{CI}*(\text{TMP0}*\text{TMP3}))+(\text{TMP4}*(-\text{CI}*(P2(2))+\text{CI}*(P3(2)))) \\
 &\$ +(V2(5)*(-\text{CI}*(\text{TMP0})+\text{CI}*(\text{TMP2}))+V3(5)*(-\text{CI}*(\text{TMP3})+\text{CI}*(\text{TMP1)))))) \\
 V1(6) &= \text{DENOM}*(\text{OM1}*P1(3)*(\text{TMP4}*(-\text{CI}*(\text{TMP6})+\text{CI}*(\text{TMP5}))+(-\text{CI}*(\text{TMP1} \\
 &\$ * \text{TMP2})+\text{CI}*(\text{TMP0}*\text{TMP3}))+(\text{TMP4}*(-\text{CI}*(P2(3))+\text{CI}*(P3(3)))) \\
 &\$ +(V2(6)*(-\text{CI}*(\text{TMP0})+\text{CI}*(\text{TMP2}))+V3(6)*(-\text{CI}*(\text{TMP3})+\text{CI}*(\text{TMP1))))))
 \end{aligned}$$

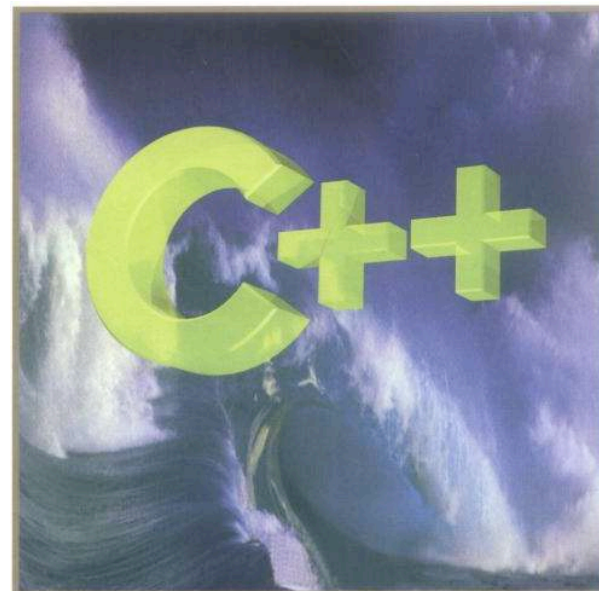
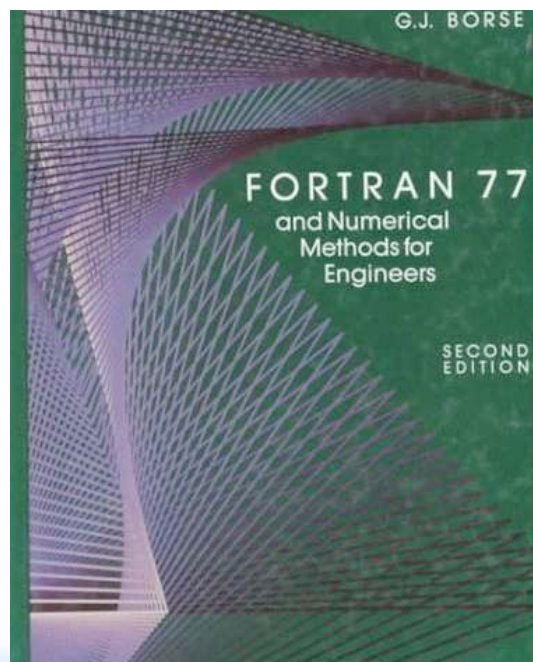


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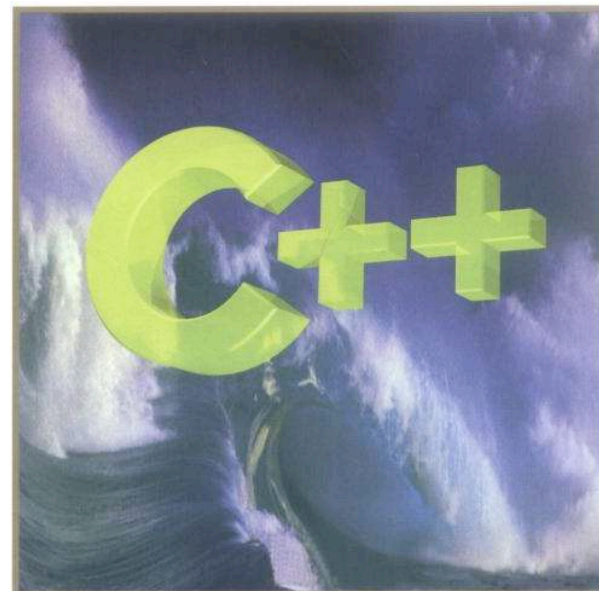
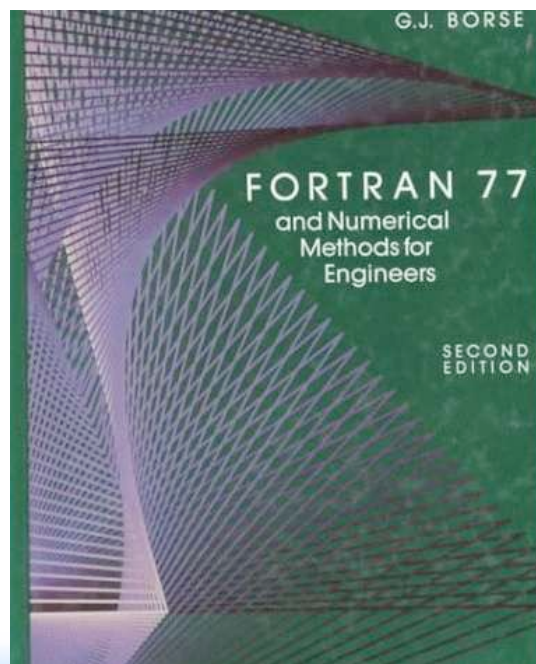
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From: [UFO] To: Helicity [Translate]

Options: Standard (HELAS)
Feynman gauge
Complex-mass scheme
Loop
Open Loop

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Wavefunction (Unitary)

$$\eta_{\mu\nu} + \frac{p_{\mu}p_{\nu}}{m^2}$$

Wavefunction (Feynman)

$$\eta_{\mu\nu}$$

```

TMP5 = (P1(0)*P2(0)-P1(1)*P2(1)-P1(2)*P2(2)-P1(3)*P2(3))
TMP4 = (V3(3)*V2(3)-V3(4)*V2(4)-V3(5)*V2(5)-V3(6)*V2(6))
TMP6 = (P1(0)*P3(0)-P1(1)*P3(1)-P1(2)*P3(2)-P1(3)*P3(3))
TMP1 = (P1(0)*V2(3)-P1(1)*V2(4)-P1(2)*V2(5)-P1(3)*V2(6))
TMP0 = (V3(3)*P1(0)-V3(4)*P1(1)-V3(5)*P1(2)-V3(6)*P1(3))
TMP3 = (V2(3)*P3(0)-V2(4)*P3(1)-V2(5)*P3(2)-V2(6)*P3(3))
TMP2 = (V3(3)*P2(0)-V3(4)*P2(1)-V3(5)*P2(2)-V3(6)*P2(3))
DENOM = COUP/(P1(0)**2-P1(1)**2-P1(2)**2-P1(3)**2 - M1 * (M1
$ -CI* W1))
V1(3)= DENOM*(OM1*P1(0)*(TMP4*(-CI*(TMP6)+CI*(TMP5)))+(-CI*(TMP1
$ *TMP2)+CI*(TMP0*TMP3)))+(TMP4*(-CI*(P2(0))+CI*(P3(0))))
$ +(V2(3)*(-CI*(TMP0)+CI*(TMP2))+V3(3)*(-CI*(TMP3)+CI*(TMP1))))
V1(4)= DENOM*(OM1*P1(1)*(TMP4*(-CI*(TMP6)+CI*(TMP5)))+(-CI*(TMP1
$ *TMP2)+CI*(TMP0*TMP3)))+(TMP4*(-CI*(P2(1))+CI*(P3(1))))
$ +(V2(4)*(-CI*(TMP0)+CI*(TMP2))+V3(4)*(-CI*(TMP3)+CI*(TMP1))))
V1(5)= DENOM*(OM1*P1(2)*(TMP4*(-CI*(TMP6)+CI*(TMP5)))+(-CI*(TMP1
$ *TMP2)+CI*(TMP0*TMP3)))+(TMP4*(-CI*(P2(2))+CI*(P3(2))))
$ +(V2(5)*(-CI*(TMP0)+CI*(TMP2))+V3(5)*(-CI*(TMP3)+CI*(TMP1))))
V1(6)= DENOM*(OM1*P1(3)*(TMP4*(-CI*(TMP6)+CI*(TMP5)))+(-CI*(TMP1
$ *TMP2)+CI*(TMP0*TMP3)))+(TMP4*(-CI*(P2(3))+CI*(P3(3))))
$ +(V2(6)*(-CI*(TMP0)+CI*(TMP2))+V3(6)*(-CI*(TMP3)+CI*(TMP1))))

```

```

TMP4 = (V3(3)*V2(3)-V3(4)*V2(4)-V3(5)*V2(5)-V3(6)*V2(6))
TMP1 = (V3(3)*P2(0)-V3(4)*P2(1)-V3(5)*P2(2)-V3(6)*P2(3))
TMP0 = (V3(3)*P1(0)-V3(4)*P1(1)-V3(5)*P1(2)-V3(6)*P1(3))
TMP3 = (V2(3)*P3(0)-V2(4)*P3(1)-V2(5)*P3(2)-V2(6)*P3(3))
TMP2 = (P1(0)*V2(3)-P1(1)*V2(4)-P1(2)*V2(5)-P1(3)*V2(6))
DENOM = COUP/(P1(0)**2-P1(1)**2-P1(2)**2-P1(3)**2 - M1 * (M1
$ -CI* W1))
V1(3)= DENOM*(TMP4*(-CI*(P2(0))+CI*(P3(0)))+(V2(3)*(-CI*(TMP0)
$ +CI*(TMP1))+V3(3)*(-CI*(TMP3)+CI*(TMP2))))
V1(4)= DENOM*(TMP4*(-CI*(P2(1))+CI*(P3(1)))+(V2(4)*(-CI*(TMP0)
$ +CI*(TMP1))+V3(4)*(-CI*(TMP3)+CI*(TMP2))))
V1(5)= DENOM*(TMP4*(-CI*(P2(2))+CI*(P3(2)))+(V2(5)*(-CI*(TMP0)
$ +CI*(TMP1))+V3(5)*(-CI*(TMP3)+CI*(TMP2))))
V1(6)= DENOM*(TMP4*(-CI*(P2(3))+CI*(P3(3)))+(V2(6)*(-CI*(TMP0)
$ +CI*(TMP1))+V3(6)*(-CI*(TMP3)+CI*(TMP2))))

```

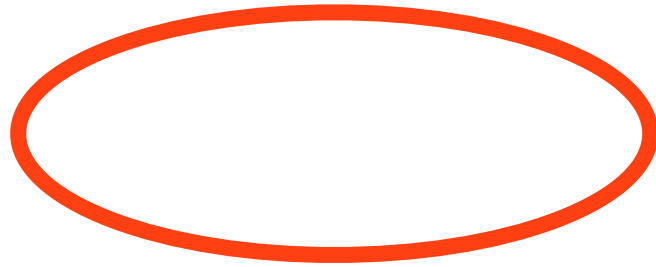
- Improvement: Have a **Two** distinct routines for massive and massless vector. (crucial for open loop)



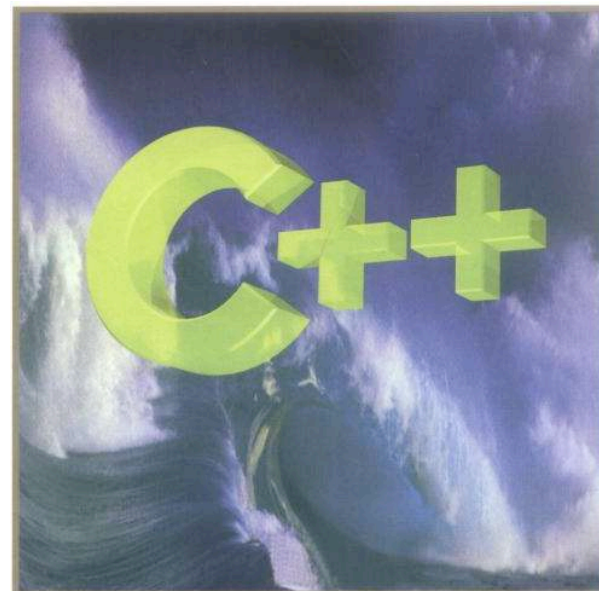
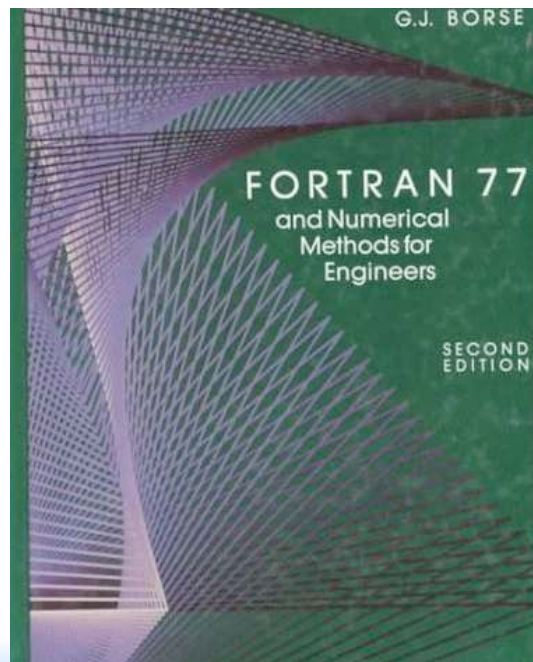
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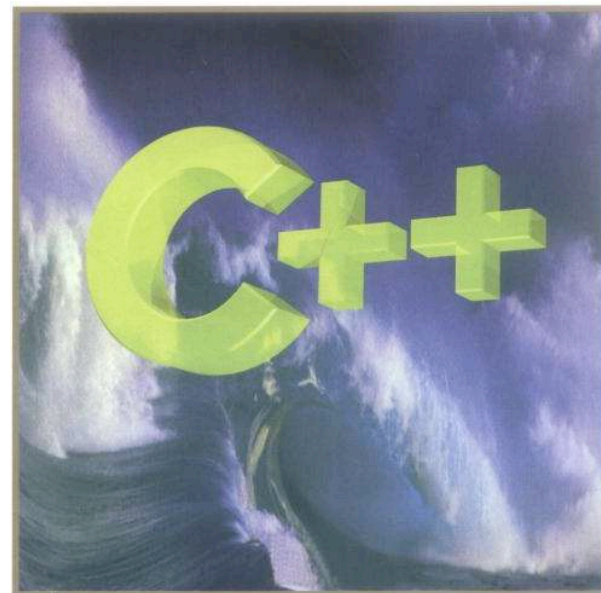
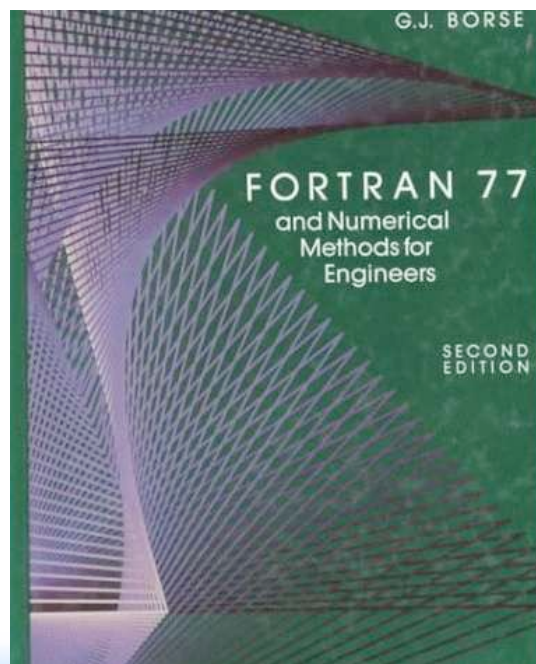
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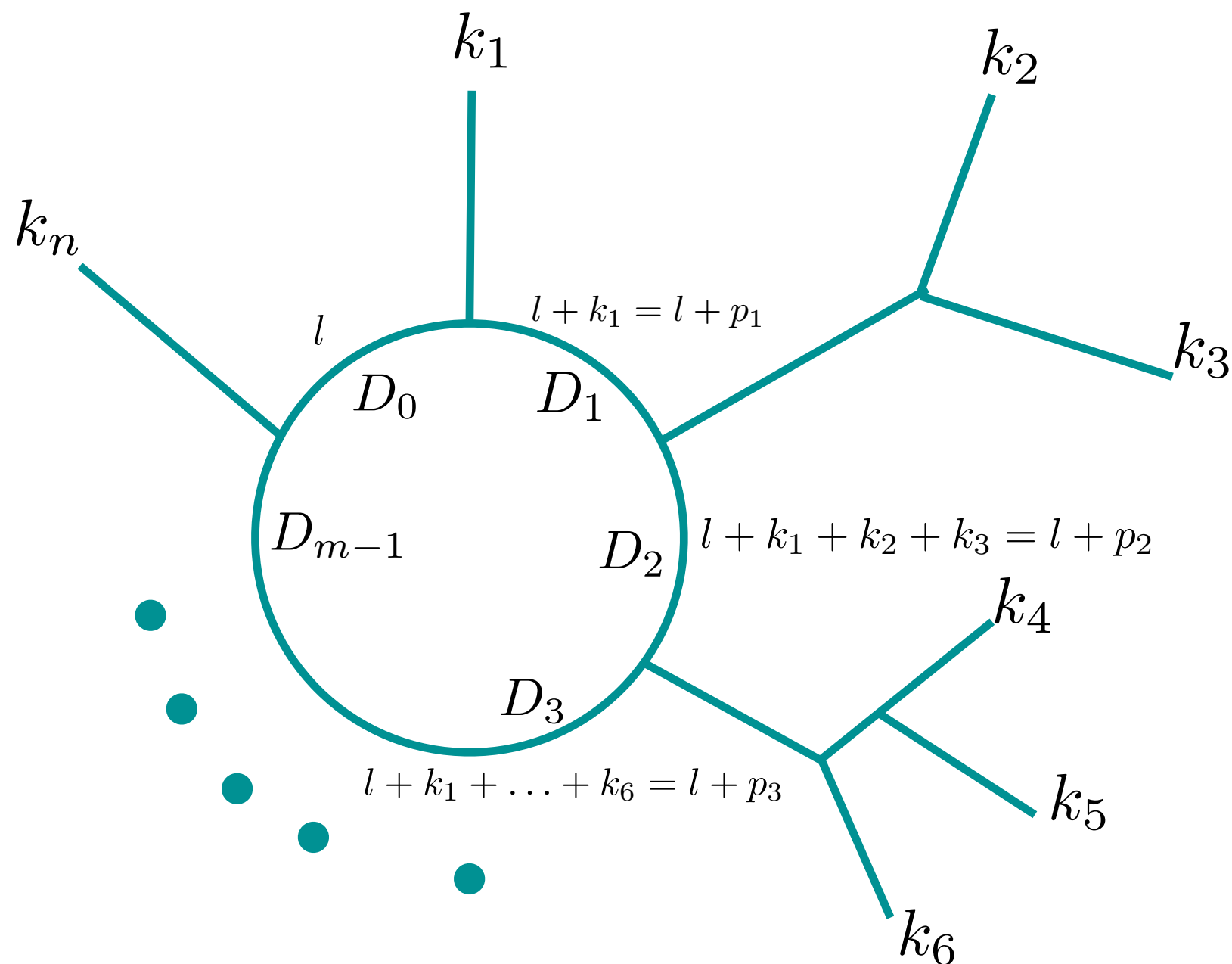
- Options:
- Standard (HELAS)
 - Feynman gauge
 - Complex mass scheme
 - Loop
 - Open Loop

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one-loop integral



- Consider this m -point loop diagram with n external momenta
- The integral to compute is

$$\int d^d l \frac{N(l)}{D_0 D_1 D_2 \cdots D_{m-1}}$$

$$D_i = (l + p_i)^2 - m_i^2$$

Open Loop

$$\mathcal{N}(l^\mu) = \sum_{r=0}^{r_{max}} C_{\mu_0 \mu_1 \dots \mu_r}^{(r)} l^{\mu_0} l^{\mu_1} \dots l^{\mu_r}$$

$$V_j^{(r=0,1)} = \sum_{i=0}^r v_j^i l^i$$

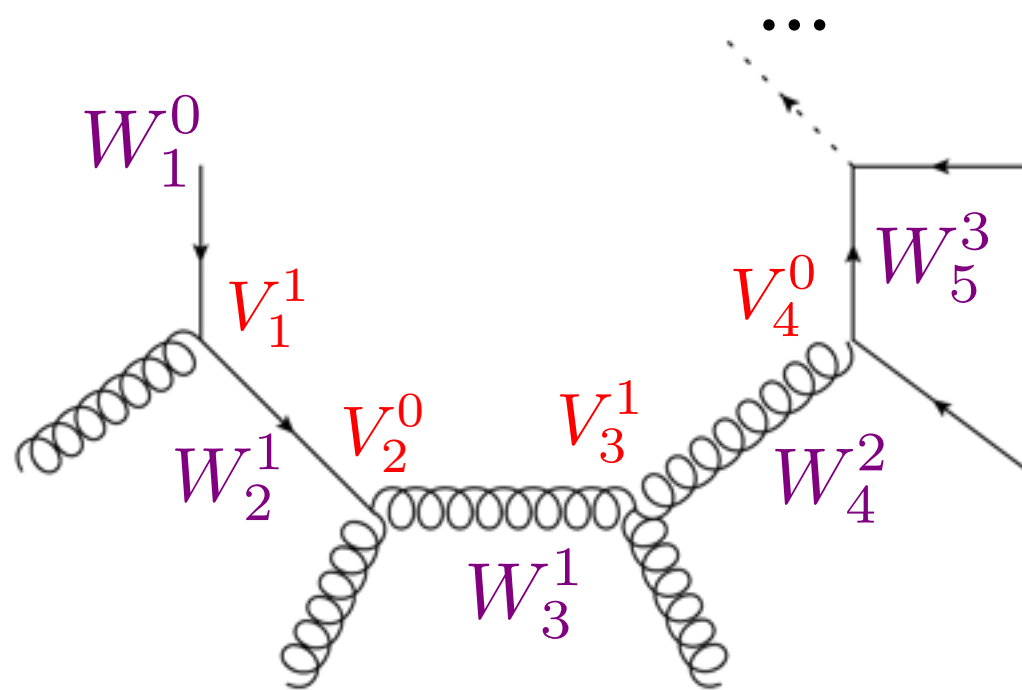
Computed by
aloha



Open Loop

$$\mathcal{N}(l^\mu) = \sum_{r=0}^{r_{max}} C_{\mu_0 \mu_1 \dots \mu_r}^{(r)} l^{\mu_0} l^{\mu_1} \dots l^{\mu_r}$$

- How to get these coefficients? (Wavefunction and 4-momenta indices now omitted)



$$V_j^{(r=0,1)} = \sum_{i=0}^r v_j^i l^i$$

Computed by
aloha



```

TMP1 = (V3(5)*P2(0)-V3(6)*P2(1)-V3(7)*P2(2)-V3(8)*P2(3))
TMP0 = (V3(5)*P1(0)-V3(6)*P1(1)-V3(7)*P1(2)-V3(8)*P1(3))
COEFF(1,0,1)= COUP*(V3(5)*(+CI*(P1(0)+P2(0)))+(-CI*(TMP0+TMP1)))
COEFF(2,0,1)= COUP*(V3(5)*(-CI*(P3(1))+CI*(P1(1)))+V3(6)*
$ +CI*(P2(0)+P3(0)))
COEFF(3,0,1)= COUP*(V3(5)*(-CI*(P3(2))+CI*(P1(2)))+V3(7)*
$ +CI*(P2(0)+P3(0)))
COEFF(4,0,1)= COUP*(V3(5)*(-CI*(P3(3))+CI*(P1(3)))+V3(8)*
$ +CI*(P2(0)+P3(0)))
COEFF(1,1,1)= 0D0
COEFF(2,1,1)= COUP*CI * V3(6)
COEFF(3,1,1)= COUP*CI * V3(7)
COEFF(4,1,1)= COUP*CI * V3(8)
COEFF(1,2,1)= COUP*2D0 * CI * V3(6)
COEFF(2,2,1)= COUP*CI * V3(5)
COEFF(3,2,1)= 0D0
COEFF(4,2,1)= 0D0
COEFF(1,3,1)= COUP*2D0 * CI * V3(7)
COEFF(2,3,1)= 0D0
COEFF(3,3,1)= COUP*CI * V3(5)
COEFF(4,3,1)= 0D0
COEFF(1,4,1)= COUP*2D0 * CI * V3(8)
COEFF(2,4,1)= 0D0
COEFF(3,4,1)= 0D0
COEFF(4,4,1)= COUP*CI * V3(5)
COEFF(1,0,2)= COUP*-1D0*(V3(5)*(+CI*(P2(1)+P3(1)))+V3(6)*
$ -CI*(P3(0))+CI*(P1(0)))
COEFF(2,0,2)= COUP*-1D0*(V3(6)*(+CI*(P1(1)+P2(1)))+(CI*(TMP0
$ +TMP1)))
COEFF(3,0,2)= COUP*-1D0*(V3(6)*(-CI*(P3(2))+CI*(P1(2)))+V3(7)*
$ +CI*(P2(1)+P3(1)))
COEFF(4,0,2)= COUP*-1D0*(V3(6)*(-CI*(P3(3))+CI*(P1(3)))+V3(8)*
$ +CI*(P2(1)+P3(1)))
COEFF(1,1,2)= COUP*-CI * V3(6)
COEFF(2,1,2)= COUP*-2D0 * CI * V3(5)
COEFF(3,1,2)= 0D0
COEFF(4,1,2)= 0D0
COEFF(1,2,2)= COUP*-CI * V3(5)
COEFF(2,2,2)= 0D0
COEFF(3,2,2)= COUP*-CI * V3(7)
COEFF(4,2,2)= COUP*-CI * V3(8)
COEFF(1,3,2)= 0D0
COEFF(2,3,2)= COUP*2D0 * CI * V3(7)
COEFF(3,3,2)= COUP*-CI * V3(6)
COEFF(4,3,2)= 0D0
COEFF(1,4,2)= 0D0
COEFF(2,4,2)= COUP*2D0 * CI * V3(8)
COEFF(3,4,2)= 0D0
COEFF(4,4,2)= COUP*-CI * V3(6)
COEFF(1,0,3)= COUP*-1D0*(V3(5)*(+CI*(P2(2)+P3(2)))+V3(7)*
$ -CI*(P3(0))+CI*(P1(0)))

```

```

COEFF(2,0,3)= COUP*-1D0*(V3(6)*(+CI*(P2(2)+P3(2)))+V3(7)*
$ -CI*(P3(1))+CI*(P1(1)))
COEFF(3,0,3)= COUP*-1D0*(V3(7)*(+CI*(P1(2)+P2(2)))+(CI*(TMP0
$ +TMP1)))
COEFF(4,0,3)= COUP*-1D0*(V3(7)*(-CI*(P3(3))+CI*(P1(3)))+V3(8)*
$ +CI*(P2(2)+P3(2)))
COEFF(1,1,3)= COUP*-CI * V3(7)
COEFF(2,1,3)= 0D0
COEFF(3,1,3)= COUP*-2D0 * CI * V3(5)
COEFF(4,1,3)= 0D0
COEFF(1,2,3)= 0D0
COEFF(2,2,3)= COUP*-CI * V3(7)
COEFF(3,2,3)= COUP*2D0 * CI * V3(6)
COEFF(4,2,3)= 0D0
COEFF(1,3,3)= COUP*-CI * V3(5)
COEFF(2,3,3)= COUP*-CI * V3(6)
COEFF(3,3,3)= 0D0
COEFF(4,3,3)= COUP*-CI * V3(8)
COEFF(1,4,3)= 0D0
COEFF(2,4,3)= 0D0
COEFF(3,4,3)= COUP*2D0 * CI * V3(8)
COEFF(4,4,3)= COUP*-CI * V3(7)
COEFF(1,0,4)= COUP*-1D0*(V3(5)*(+CI*(P2(3)+P3(3)))+V3(8)*
$ -CI*(P3(0))+CI*(P1(0)))
COEFF(2,0,4)= COUP*-1D0*(V3(6)*(+CI*(P2(3)+P3(3)))+V3(8)*
$ -CI*(P3(1))+CI*(P1(1)))
COEFF(3,0,4)= COUP*-1D0*(V3(7)*(+CI*(P2(3)+P3(3)))+V3(8)*
$ -CI*(P3(2))+CI*(P1(2)))
COEFF(4,0,4)= COUP*-1D0*(V3(8)*(+CI*(P1(3)+P2(3)))+(CI*(TMP0
$ +TMP1)))
COEFF(1,1,4)= COUP*-CI * V3(8)
COEFF(2,1,4)= 0D0
COEFF(3,1,4)= 0D0
COEFF(4,1,4)= COUP*-2D0 * CI * V3(5)
COEFF(1,2,4)= 0D0
COEFF(2,2,4)= COUP*-CI * V3(8)
COEFF(3,2,4)= 0D0
COEFF(4,2,4)= COUP*2D0 * CI * V3(6)
COEFF(1,3,4)= 0D0
COEFF(2,3,4)= 0D0
COEFF(3,3,4)= COUP*-CI * V3(8)
COEFF(4,3,4)= COUP*2D0 * CI * V3(7)
COEFF(1,4,4)= COUP*-CI * V3(5)
COEFF(2,4,4)= COUP*-CI * V3(6)
COEFF(3,4,4)= COUP*-CI * V3(7)
COEFF(4,4,4)= 0D0
END

```