# MG5\_aMC@NLO looping up to be mad!

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based on 1401.7340 and 1405.0301 Work in progress with V. Hirschi



### Plan





- Loop-Induced processes
  - →LO re-weighting
  - PS integration



### Plan



































MadGraph StandAlone

MadLoop StandAlone































Process Synta		Syntax	Cross section (pb)			
Vector	-boson pair +jets		LO 13 T	°eV	NLO 13 7	ΓeV
b.1	$pp \rightarrow W^+W^-$ (4f)	p p > w+ w-	$7.355 \pm 0.005 \cdot 10^{1}$	+5.0% +2.0% -6.1% -1.5%	$1.028 \pm 0.003\cdot 10^2$	$^{+4.0\%}_{-4.5\%}$ $^{+1.9\%}_{-1.4\%}$
b.2	$pp \rightarrow ZZ$	p p > z z	$1.097 \pm 0.002 \cdot 10^{1}$	$^{+4.5\%}_{-5.6\%}$ $^{+1.9\%}_{-1.5\%}$	$1.415 \pm 0.005 \cdot 10^{1}$	$^{+3.1\%}_{-3.7\%}$ $^{+1.8\%}_{-1.4\%}$
b.3	$pp \rightarrow ZW^{\pm}$	p p > z wpm	$2.777 \pm 0.003 \cdot 10^{1}$	+3.6% +2.0% -4.7% -1.5%	$4.487 \pm 0.013 \cdot 10^{1}$	+4.4% +1.7% -4.4% -1.3%
b.4	$pp \rightarrow \gamma \gamma$	pp>aa	$2.510 \pm 0.002 \cdot 10^{1}$	+22.1% +2.4% -22.4% -2.1%	$6.593 \pm 0.021 \cdot 10^{1}$	+17.6% +2.0% -18.8% -1.9%
b.5	$pp \rightarrow \gamma Z$	p p > a z	$2.523 \pm 0.004 \cdot 10^{1}$	+9.9% +2.0% -11.2% -1.6%	$3.695 \pm 0.013 \cdot 10^{1}$	+5.4% +1.8% -7.1% -1.4%
b.6	$pp\!\rightarrow\!\gamma W^{\pm}$	pp>awpm	$2.954 \pm 0.005 \cdot 10^{1}$	$^{+9.5\%}_{-11.0\%}$ $^{+2.0\%}_{-1.7\%}$	$7.124 \pm 0.026 \cdot 10^{1}$	$^{+9.7\%}_{-9.9\%}$ $^{+1.5\%}_{-1.3\%}$
b.7	$pp \rightarrow W^+W^-j$ (4f)	p p > w+ w- j	$2.865 \pm 0.003 \cdot 10^{1}$	+11.6% +1.0%	$3.730 \pm 0.013 \cdot 10^{1}$	+4.9% +1.1% -4.9% -0.8%
b.8	$pp \rightarrow ZZj$	p p > z z j	$3.662 \pm 0.003 \cdot 10^{0}$	+10.9% +1.0% -9.3% -0.8%	$4.830 \pm 0.016 \cdot 10^{0}$	+5.0% +1.1% -4.8% -0.9%
b.9	$pp \!  ightarrow \! ZW^{\pm}j$	p p > z wpm j	$1.605 \pm 0.005 \cdot 10^{1}$	+11.6% +0.9% -10.0% -0.7%	$2.086 \pm 0.007 \cdot 10^{1}$	+4.9% +0.9% -4.8% -0.7%
b.10	$pp \rightarrow \gamma \gamma j$	pp>aaj	$1.022 \pm 0.001 \cdot 10^{1}$	+20.3% +1.2% -17.7% -1.5%	$2.292 \pm 0.010 \cdot 10^{1}$	+17.2% +1.0% -15.1% -1.4%
b.11*	$pp \rightarrow \gamma Z j$	p p > a z j	$8.310 \pm 0.017 \cdot 10^{0}$	$^{+14.5\%}_{-12.8\%}$ $^{+1.0\%}_{-1.0\%}$	$1.220 \pm 0.005 \cdot 10^{1}$	+7.3% +0.9% -7.4% -0.9%
b.12*	$pp \!  ightarrow \! \gamma W^{\pm} j$	p p > a wpm j	$2.546 \pm 0.010 \cdot 10^{1}$	$^{+13.7\%}_{-12.1\%}$ $^{+0.9\%}_{-1.0\%}$	$3.713 \pm 0.015 \cdot 10^{1}$	$^{+7.2\%}_{-7.1\%}$ $^{+0.9\%}_{-1.0\%}$
b.13	$pp \rightarrow W^+W^+jj$	p p > w+ w+ j j	$1.484 \pm 0.006 \cdot 10^{-1}$	$^{+25.4\%}_{-18.9\%}$ $^{+2.1\%}_{-1.5\%}$	$2.251 \pm 0.011 \cdot 10^{-1}$	$^{+10.5\%}_{-10.6\%}$ $^{+2.2\%}_{-1.6\%}$
b.14	$pp \rightarrow W^-W^-jj$	p p > w- w- j j	$6.752 \pm 0.007 \cdot 10^{-2}$	+25.4% +2.4% -18.9% -1.7%	$1.003 \pm 0.003 \cdot 10^{-1}$	$^{+10.1\%}_{-10.4\%}$ $^{+2.5\%}_{-1.8\%}$
b.15	$pp \rightarrow W^+W^-jj$ (4f)	p p > w+ w- j j	$1.144 \pm 0.002 \cdot 10^{1}$	+27.2% +0.7% -19.9% -0.5%	$1.396 \pm 0.005 \cdot 10^{1}$	+5.0% +0.7% -6.8% -0.6%
b.16	$pp \rightarrow ZZjj$	p p > z z j j	$1.344 \pm 0.002 \cdot 10^{0}$	+26.6% +0.7% -19.6% -0.6%	$1.706 \pm 0.011 \cdot 10^{0}$	+5.8% +0.8% -7.2% -0.6%
b.17	$pp \!  ightarrow \! ZW^{\pm} jj$	p p > z wpm j j	$8.038 \pm 0.009 \cdot 10^{0}$	+26.7% +0.7% -19.7% -0.5%	$9.139 \pm 0.031 \cdot 10^{0}$	$^{+3.1\%}_{-5.1\%}$ $^{+0.7\%}_{-0.5\%}$
b.18	$pp \rightarrow \gamma \gamma j j$	pp>aajj	$5.377 \pm 0.029 \cdot 10^{0}$	$^{+26.2\%}_{-19.8\%}$ $^{+0.6\%}_{-1.0\%}$	$7.501 \pm 0.032 \cdot 10^{0}$	$^{+8.8\%}_{-10.1\%}$ $^{+0.6\%}_{-1.0\%}$
b.19*	$pp \rightarrow \gamma Z j j$	pp>azjj	$3.260 \pm 0.009 \cdot 10^{0}$	$^{+24.3\%}_{-18.4\%}$ $^{+0.6\%}_{-0.6\%}$	$4.242 \pm 0.016 \cdot 10^{0}$	$^{+6.5\%}_{-7.3\%}$ $^{+0.6\%}_{-0.6\%}$
b.20*	$pp \!  ightarrow \! \gamma W^{\pm} j j$	pp>awpmjj	$1.233 \pm 0.002 \cdot 10^{1}$	$^{+24.7\%}_{-18.6\%}$ $^{+0.6\%}_{-0.6\%}$	$1.448 \pm 0.005 \cdot 10^{1}$	$^{+3.6\%}_{-5.4\%}$ $^{+0.6\%}_{-0.7\%}$



1	Process Syntax		Cross section (pb)			
Th	ree vector bosons +jet		LO 13 Te	N.	NLO 13 T	eV
c.1	$pp \rightarrow W^+W^-W^{\pm}$ (4f)	p p > v+ v- vpa	$1.307 \pm 0.003 \cdot 10^{-1}$	+0.0% +9.0%	$2.109 \pm 0.006 \cdot 10^{-1}$	+5-15 +1-65
c.2	$pp \rightarrow ZW^+W^-$ (4f)	p p > z ** *-	$9.658 \pm 0.065 \cdot 10^{-2}$	+0.83 +0.13	$1.679 \pm 0.005 \cdot 10^{-1}$	+6.35 +1.65
c.3	$pp \rightarrow ZZW^{\pm}$	p p > z z vpa	$2.996 \pm 0.016 \cdot 10^{-2}$	+1.0% +5.0%	$5.550 \pm 0.020 \cdot 10^{-2}$	+6.8% +1.5%
c.4	$pp \rightarrow ZZZ$	pp>zzz	$1.085 \pm 0.002 \cdot 10^{-2}$	+0.03 +1.93	$1.417 \pm 0.005 \cdot 10^{-2}$	+5.7% +1.9%
e.5	$pp \rightarrow \gamma W^+W^-$ (4f)	p p > a u+ u-	$1.427 \pm 0.011 \cdot 10^{-1}$	+1.9% +5.0%	$2.581 \pm 0.008 \cdot 10^{-1}$	+5.4% +1.4%
c.6	$pp \rightarrow \gamma \gamma W^{\perp}$	p p ≻ a a vpn	$2.681 \pm 0.007 \cdot 10^{-2}$	14.4% 11.9%	$8.251 \pm 0.032 \cdot 10^{-2}$	+7.4% +1.6%
c.7	$pp \rightarrow \gamma ZW^{\pm}$	p p > a z vpn	$4.994 \pm 0.011 \cdot 10^{-2}$	+0.855 +1.955	$1.117 \pm 0.004 \cdot 10^{-1}$	+2.2% +1.2%
c.8	$pp \rightarrow \gamma ZZ$	pp>azz	$2.320 \pm 0.005 \cdot 10^{-2}$	+2.0% +1.9%	$3.118 \pm 0.012 \cdot 10^{-2}$	+2.8% +1.8%
c.9	$pp \rightarrow \gamma \gamma Z$	pp>aaz	$3.078\pm0.007\cdot10^{-2}$	10.00 +1.9%	$4.634\pm0.020\cdot10^{-2}$	+4.4% +1.2%
c.10	$pp \rightarrow \gamma \gamma \gamma$	pp>aaa	$1.269\pm0.003\cdot10^{-9}$	+9.8% +2.0% -11.0% -1.8%	$3.441 \pm 0.012 \cdot 10^{-9}$	+11.8% $+1.4%-11.6%$ $-1.5%$
c.11	$pp \rightarrow W^+W^-W^{\pm}j$ (4f)	pp>v+v-vpnj	$9.167 \pm 0.010 \cdot 10^{-2}$	+15.0% +1.0%	$1.197 \pm 0.004 \cdot 10^{-1}$	+5.2% +1.0%
c.12"	$pp \rightarrow ZW^+W^-j$ (4f)	p p > z ++ +- j	$8.340 \pm 0.010 \cdot 10^{-2}$	+15.8% +1.6%	$1.066 \pm 0.003 \cdot 10^{-1}$	+135 +185
c.13*	$pp \rightarrow ZZW^{\perp}j$	p p > z z vpn j	$2.810 \pm 0.004 \cdot 10^{-2}$	+16.1% +1.0%	$3.660 \pm 0.013\cdot 10^{-2}$	+1.8% +1.0%
c.14"	$pp \rightarrow ZZZj$	pp>zzzj	$4.823 \pm 0.011 \cdot 10^{-3}$	+14.8% +1.4%	$6.341 \pm 0.025 \cdot 10^{-3}$	+4.9% +1.4%
c.15*	$pp \rightarrow \gamma W^+W^-j$ (4f)	pp>au+u-j	$1.182 \pm 0.004 \cdot 10^{-1}$	+12.4% +0.8%	$1.233 \pm 0.004 \cdot 10^3$	+18.9% +1.0%
c.16	$PP \rightarrow \gamma \gamma W^{\pm} j$	p p > a a vpn j	$4.107\pm0.015\cdot10^{-2}$	+11.8% +0.6%	$5.807 \pm 0.023 \cdot 10^{-2}$	13.8% 10.2%
c.17*	$pp \rightarrow \gamma ZW^{\pm}j$	p p > a z vpn j	$5.833 \pm 0.023 \cdot 10^{-9}$	+14.4% +0.7%	$7.764 \pm 0.025 \cdot 10^{-9}$	+5.7K +0.8K
c.18*	$pp \rightarrow \gamma ZZj$	pp>azzj	$9.995 \pm 0.013 \cdot 10^{-3}$	+12.5% +1.2%	$1.371 \pm 0.005 \cdot 10^{-9}$	+5.8% +1.2%
c.19*	$pp \rightarrow \gamma \gamma Z j$	pp>aazj	$1.372\pm0.003\cdot10^{-2}$	+10.9% +1.0%	$2.051\pm0.011\cdot10^{-2}$	+7.0% +1.0%
c.20*	pp→111j	pp>aaaj	$1.031 \pm 0.006 \cdot 10^{-9}$	+54.3% +0.9%	$2.020 \pm 0.008 \cdot 10^{-5}$	+12.8% +0.8%

Process	Syntax	Cross se	ction (pb)
Four vector bosons		LO 13 TeV	NLO 13 TeV
c.21* $pp \rightarrow W^+W^-W^+W^-$ (4f)	p p > w+ w- w+ w-	$5.721 \pm 0.014 \cdot 10^{-4}$ $^{+3.7\%}_{-3.5\%}$ $^{+2.3\%}_{-1.7\%}$	$9.959 \pm 0.035 \cdot 10^{-4}$ $^{+7.4\%}_{-6.0\%}$ $^{+1.7\%}_{-1.2\%}$
c.22 <sup>*</sup> $pp \rightarrow W^+W^-W^{\pm}Z$ (4f)	p p > w+ w- wpm z	$6.391 \pm 0.076 \cdot 10^{-4}$ $^{+4.4\%}_{-4.1\%}$ $^{+2.4\%}_{-1.8\%}$	$1.188 \pm 0.004 \cdot 10^{-3}$ $^{+8.4\%}_{-6.8\%}$ $^{+1.7\%}_{-1.2\%}$
c.23 <sup>*</sup> $pp \rightarrow W^+W^-W^{\pm}\gamma$ (4f)	p p > w+ w- wpm a	$8.115 \pm 0.064 \cdot 10^{-4}$ $^{+2.5\%}_{-2.5\%}$ $^{+2.2\%}_{-1.7\%}$	$1.546 \pm 0.005 \cdot 10^{-3}$ $^{+7.9\%}_{-6.3\%}$ $^{+1.5\%}_{-1.1\%}$
c.24 <sup>*</sup> $pp \rightarrow W^+W^-ZZ$ (4f)	p p > w+ w- z z	$4.320 \pm 0.013 \cdot 10^{-4}$ $^{+4.4\%}_{-4.1\%}$ $^{+2.4\%}_{-1.7\%}$	$7.107 \pm 0.020 \cdot 10^{-4}$ $^{+7.0\%}_{-5.7\%}$ $^{+1.8\%}_{-1.3\%}$
c.25 <sup>*</sup> $pp \rightarrow W^+W^-Z\gamma$ (4f)	p p > w+ w- z a	$8.403 \pm 0.016 \cdot 10^{-4}$ $^{+3.0\%}_{-2.9\%}$ $^{+2.3\%}_{-1.7\%}$	$1.483 \pm 0.004 \cdot 10^{-3}$ $^{+7.2\%}_{-5.8\%}$ $^{+1.6\%}_{-1.2\%}$
c.26 <sup>*</sup> $pp \rightarrow W^+W^-\gamma\gamma$ (4f)	p p > w+ w- a a	$5.198 \pm 0.012 \cdot 10^{-4}$ $^{+0.6\%}_{-0.9\%}$ $^{+2.1\%}_{-1.6\%}$	$9.381 \pm 0.032 \cdot 10^{-4}$ $^{+6.7\%}_{-5.3\%}$ $^{+1.4\%}_{-1.1\%}$
c.27 <sup>*</sup> $pp \rightarrow W^{\pm}ZZZ$	p p > wpm z z z	$5.862 \pm 0.010 \cdot 10^{-5}$ $^{+5.1\%}_{-4.7\%}$ $^{+2.4\%}_{-1.8\%}$	$1.240 \pm 0.004 \cdot 10^{-4}$ $^{+9.9\%}_{-8.0\%}$ $^{+1.7\%}_{-1.2\%}$
c.28 <sup>*</sup> $pp \rightarrow W^{\pm}ZZ\gamma$	p p > wpm z z a	$1.148 \pm 0.003 \cdot 10^{-4}$ $^{+3.6\%}_{-3.5\%}$ $^{+2.2\%}_{-1.7\%}$	$2.945 \pm 0.008 \cdot 10^{-4}$ $^{+10.8\%}_{-8.7\%}$ $^{+1.3\%}_{-1.0\%}$
c.29 <sup>*</sup> $pp \rightarrow W^{\pm}Z\gamma\gamma$	pp>wpmzaa	$1.054 \pm 0.004 \cdot 10^{-4}$ $^{+1.7\%}_{-1.9\%}$ $^{+2.1\%}_{-1.7\%}$	$3.033 \pm 0.010 \cdot 10^{-4}$ $^{+10.6\%}_{-8.6\%}$ $^{+1.1\%}_{-0.8\%}$
c.30 <sup>*</sup> $pp \rightarrow W^{\pm} \gamma \gamma \gamma$	p p > wpm a a a	$3.600 \pm 0.013 \cdot 10^{-5}$ $^{+0.4\%}_{-1.0\%}$ $^{+2.0\%}_{-1.6\%}$	$1.246 \pm 0.005 \cdot 10^{-4}$ $^{+9.8\%}_{-8.1\%}$ $^{+0.9\%}_{-0.8\%}$
c.31 <sup>*</sup> $pp \rightarrow ZZZZ$	p p > z z z z	$1.989 \pm 0.002 \cdot 10^{-5}$ $^{+3.8\%}_{-3.6\%}$ $^{+2.2\%}_{-1.7\%}$	$2.629 \pm 0.008 \cdot 10^{-5}$ $^{+3.5\%}_{-3.0\%}$ $^{+2.2\%}_{-1.7\%}$
c.32 <sup>*</sup> $pp \rightarrow ZZZ\gamma$	p p > z z z a	$3.945 \pm 0.007 \cdot 10^{-5}$ $^{+1.9\%}_{-2.1\%}$ $^{+2.1\%}_{-1.6\%}$	$5.224 \pm 0.016 \cdot 10^{-5}$ $^{+3.3\%}_{-2.7\%}$ $^{+2.1\%}_{-1.6\%}$
c.33 <sup>*</sup> $pp \rightarrow ZZ\gamma\gamma$	p p > z z a a	$5.513 \pm 0.017 \cdot 10^{-5}$ $^{+0.0\%}_{-0.3\%}$ $^{+2.1\%}_{-1.6\%}$	$7.518 \pm 0.032 \cdot 10^{-5}$ $^{+3.4\%}_{-2.6\%}$ $^{+2.0\%}_{-1.5\%}$
c.34 <sup>*</sup> $pp \rightarrow Z\gamma\gamma\gamma$	pp>zaaa	$4.790 \pm 0.012 \cdot 10^{-5}$ $^{+2.3\%}_{-3.1\%}$ $^{+2.0\%}_{-1.6\%}$	$7.103 \pm 0.026 \cdot 10^{-5}$ $^{+3.4\%}_{-3.2\%}$ $^{+1.6\%}_{-1.8\%}$
c.35* $pp \rightarrow \gamma \gamma \gamma \gamma$	pp>aaaa	$1.594 \pm 0.004 \cdot 10^{-5}$ $^{+4.7\%}_{-5.7\%}$ $^{+1.9\%}_{-1.7\%}$	$3.389 \pm 0.012 \cdot 10^{-5}$ $^{+7.0\%}_{-6.7\%}$ $^{+1.3\%}_{-1.3\%}$

Process		Syntax	Cross section (pb)				
Heavy quarks and jets			LO 13 TeV	NLO 13 TeV			
d.1 d.2	$pp \rightarrow jj$ $pp \rightarrow jjj$	pp>jj pp>jjj	$\begin{array}{rrrr} 1.162 \pm 0.001 \cdot 10^{6} & {}^{+24.2\%}_{-18.4\%}  {}^{+0.8\%}_{-0.0\%} \\ 8.940 \pm 0.021 \cdot 10^{4} & {}^{+43.8\%}_{-28.4\%}  {}^{+1.2\%}_{-28.4\%} \end{array}$	$\begin{array}{rrrr} 1.580 \pm 0.007 \cdot 10^6 & {}^{+8.4\%}_{-0.0\%}  {}^{+0.7\%}_{-0.0\%} \\ 7.791 \pm 0.037 \cdot 10^4 & {}^{+2.1\%}_{-23.2\%}  {}^{+1.1\%}_{-1.3\%} \end{array}$			
d.3 d.4* d.5* d.6	$pp \rightarrow b\bar{b}$ (4f) $pp \rightarrow b\bar{b}j$ (4f) $pp \rightarrow b\bar{b}jj$ (4f) $pp \rightarrow b\bar{b}b\bar{b}$ (4f)	p p > b b~ p p > b b~ j p p > b b~ j j p p > b b~ b b~	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$			
d.7 d.8 d.9 d.10	$pp \rightarrow t\bar{t}$ $pp \rightarrow t\bar{t}j$ $pp \rightarrow t\bar{t}jj$ $pp \rightarrow t\bar{t}t\bar{t}$	p p > t t~ j p p > t t~ j p p > t t~ j j p p > t t~ t t~	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} 6.741 \pm 0.023 \cdot 10^2 & +9.8\% & +1.8\% \\ -10.9\% & -2.1\% \\ 4.106 \pm 0.015 \cdot 10^2 & +8.1\% & +2.1\% \\ 1.795 \pm 0.006 \cdot 10^2 & +9.3\% & +2.4\% \\ 9.201 \pm 0.028 \cdot 10^{-3} & +30.8\% & +0.4\% \\ -28.6\% & -2.9\% \\ -28.6\% & -5.9\% \end{array}$			
d.11	$pp \rightarrow t\bar{t}b\bar{b}$ (4f)	p p > t t~ b b~	$6.119 \pm 0.004 \cdot 10^{0}  {}^{+62.15}_{-85.7\%}  {}^{+2.95}_{-85.7\%}$	$1.452 \pm 0.005 \cdot 10^{1}  {}^{+ 37.63 }_{- 27.6 \% }  {}^{+ 2.9 \% }_{- 8.6 \% }$			

	Process	Syntax	Cross section (pb)			
	Single-top		LO 13 TeV	NLO 13 TeV		
£.1	$pp \rightarrow tj$ (t-channel)	p p > tt j \$\$ w+ w-	$1.520 \pm 0.001 \cdot 10^2 \xrightarrow{+0.4\%}_{-11.9\%} \xrightarrow{+0.4\%}_{-0.6\%}$	$1.563 \pm 0.005 \cdot 10^2  {}^{+1.65}_{-1.85}  {}^{+0.65}_{-0.85}$		
62	$pp \rightarrow t\gamma j$ (t-channel)	p p > tt a j \$\$ u+ u-	$9.956 \pm 0.014 \cdot 10^{-1}$ $^{+6.05}_{-8.05}$ $^{+0.05}_{-1.05}$	$1.017 \pm 0.003 \cdot 10^{2}$ $^{+1.58}_{-1.26}$ $^{+5.85}_{-0.96}$		
63	$pp \rightarrow tZj$ (t-channel)	p p > tt z j \$\$ w+ w-	$6.967 \pm 0.007 \cdot 10^{-1}$ $^{+8.08}_{-8.06} + 0.091$	$6.993 \pm 0.021 \cdot 10^{-1}$ $^{+1.0%}_{-1.1\%}$ $^{+0.99}_{-1.1\%}$		
£4	$pp \rightarrow tbj$ (t-channel, 4f)	p p > tt bb j \$\$ v+ v-	$1.003 \pm 0.000 \cdot 10^2 + 18.8\% + 0.4\% - 11.8\% - 0.8\%$	$1.319 \pm 0.003 \cdot 10^2 \xrightarrow{+0.8\%}_{-3.2\%} \xrightarrow{+0.4\%}_{-0.8\%}$		
£8*	$pp \rightarrow tbj\gamma$ (t-channel, 4f)	p p > tt bb j a \$\$ w+ w-	$6.293 \pm 0.006 \cdot 10^{-1}$ $^{+16.8\%}_{-13.7\%} \pm 0.9\%$	8.612 ± 0.025 · 10 <sup>-1</sup> +6.28 +0.87		
£6*	$pp \rightarrow tbjZ$ (t-channel, 4f)	p p > tt bb j z \$\$ u+ u-	$3.934 \pm 0.002 \cdot 10^{-1}$ $^{+18.7\%}_{-14.7\%}$ $^{+1.0\%}_{-0.9\%}$	$5.657 \pm 0.014 \cdot 10^{-1}$ $^{+7.2\%}_{-7.9\%}$ $^{+0.09}_{-0.99}$		
£7	$pp \rightarrow tb$ (s-channel, 4f)	pp>u+>t b~, pp>u->t~b	$7.489 \pm 0.007 \cdot 10^{0}$ $^{+3.5\%}_{-4.4\%}$ $^{+1.6\%}_{-1.4\%}$	$1.001 \pm 0.004 \cdot 10^{1}$ $^{+3.75}_{-3.95}$ $^{+1.05}_{-1.05}$		
£8*	$pp \rightarrow tb\gamma$ (s-channel, 4f)	pp>u+>t b~ a, pp>u->t~ b a	$1.490 \pm 0.001 \cdot 10^{-2}$ $+1.95 + 1.95$ -1.85 - 1.85	1.952 ± 0.007 - 10 <sup>-2</sup> + 0.05 + 1.27 -2.36 - 1.43		
£9*	$pp \rightarrow tbZ$ (s-channel, 4f)	p p > u* > 1 b~ x, p p > u- > 1~ b x	$1.072 \pm 0.001 - 10^{-2} + 1.98 + 6.08$ -1.5% - 1.6%	1.539±0.005-10-2 +588 +189		

Process	Syntax	Cross section (pb)			
Heavy quarks+vector bosons		LO 13 TeV	NLO 13 TeV		
e.1 $pp \rightarrow W^{\pm} b\bar{b}$ (4f) e.2 $pp \rightarrow Z b\bar{b}$ (4f)	pp>wpmbb~ pp>zbb~	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		
e.3 $pp \rightarrow \gamma b\bar{b}$ (4f)	p p > a b b~	$1.731 \pm 0.001 \cdot 10^{3}  {}^{+ 51.9 \% }_{- 34.8 \% }  {}^{+ 1.6 \% }_{- 2.1 \% }$	$4.171 \pm 0.015 \cdot 10^{3}  {}^{+ 33.7 \% }_{- 27.1 \% }  {}^{+ 1.4 \% }_{- 1.9 \% }$		
$\begin{array}{ll} \mathrm{e.4^*} & pp \rightarrow W^{\pm}  b \bar{b}  j  (\mathrm{4f}) \\ \mathrm{e.5^*} & pp \rightarrow Z  b \bar{b}  j  (\mathrm{4f}) \\ \mathrm{e.6^*} & pp \rightarrow \gamma  b \bar{b}  j  (\mathrm{4f}) \end{array}$	pp>wpmbb~j pp>zbb~j pp>abb~j	$\begin{array}{rrrr} 1.861 \pm 0.003 \cdot 10^2 & +42.5\% & +0.7\% \\ & -27.7\% & -0.7\% \\ 1.604 \pm 0.001 \cdot 10^2 & +42.4\% & +0.9\% \\ & -27.6\% & -1.1\% \\ 7.812 \pm 0.017 \cdot 10^2 & +51.2\% & +1.0\% \\ & -32.0\% & -1.5\% \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		
$ \begin{array}{ll} {\rm e.7} & pp \mathop{\rightarrow} t\bar{t}W^{\pm} \\ {\rm e.8} & pp \mathop{\rightarrow} t\bar{t}Z \\ {\rm e.9} & pp \mathop{\rightarrow} t\bar{t}\gamma \end{array} $	$\begin{array}{l} p \ p \ > \ t \ t \sim \ wpn \\ p \ p \ > \ t \ t \sim \ z \\ p \ p \ > \ t \ t \sim \ a \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		
$ \begin{array}{ll} \mathrm{e.10}^* & pp \rightarrow t\bar{t}W^{\pm}j \\ \mathrm{e.11}^* & pp \rightarrow t\bar{t}Zj \\ \mathrm{e.12}^* & pp \rightarrow t\bar{t}\gamma j \end{array} $	$\begin{array}{l} p \ p \ > \ t \ t \sim \ wpm \ j \\ p \ p \ > \ t \ t \sim \ z \ j \\ p \ p \ > \ t \ t \sim \ a \ j \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$		
$ \begin{array}{ll} \mathrm{e.13^{*}} & pp \rightarrow t\bar{t}W^{-}W^{+} \ (\mathrm{4f}) \\ \mathrm{e.14^{*}} & pp \rightarrow t\bar{t}W^{\pm}Z \\ \mathrm{e.15^{*}} & pp \rightarrow t\bar{t}W^{\pm}\gamma \\ \mathrm{e.16^{*}} & pp \rightarrow t\bar{t}ZZ \\ \mathrm{e.17^{*}} & pp \rightarrow t\bar{t}Z\gamma \end{array} $	$\begin{array}{l} p \ p \ > \ t \ t \sim \ u + \ u - \\ p \ p \ > \ t \ t \sim \ w p m \ z \\ p \ p \ > \ t \ t \sim \ w p m \ a \\ p \ p \ > \ t \ t \sim \ z \ z \\ p \ p \ > \ t \ t \sim \ z \ a \end{array}$	$\begin{array}{rrrr} 6.675 \pm 0.006 \cdot 10^{-3} & + 30.9\% & + 2.1\% \\ -2404 \pm 0.002 \cdot 10^{-3} & + 26.6\% & + 2.5\% \\ 2.718 \pm 0.003 \cdot 10^{-3} & - 19.6\% & -1.8\% \\ 1.349 \pm 0.014 \cdot 10^{-3} & + 29.3\% & -1.8\% \\ 2.548 \pm 0.003 \cdot 10^{-3} & - 21.9\% & -1.8\% \\ -21.9\% & -1.8\% & -21.9\% & -1.8\% \\ -21.9\% & -1.8\% & -21.9\% & -1.8\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -21.5\% & -21.5\% \\ -21.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ -20.5\% & -1.6\% \\ +20.5\% & -$	$\begin{array}{llllllllllllllllllllllllllllllllllll$		
e.18 <sup>*</sup> $pp \rightarrow t\bar{t}\gamma\gamma$	pp>t t∼ a a	$3.272 \pm 0.006 \cdot 10^{-3}$ +28.4% +1.3% -20.6% -1.1%	$4.402 \pm 0.015 \cdot 10^{-3}$ $^{+7.8\%}_{-9.7\%}$ $^{+1.4\%}_{-1.4\%}$		



D	Pt.	0	die (ab)	P	C	0	then (nh)
Process	Syntax	Citoes set	cuon (po)	Process	Syntax	CTORS SCI	tion (pb)
Single Higgs production		LO 13 TeV	NLO 13 TeV	Higgs pair production		LO 13 TeV	NLO 13 TeV
g.1 $pp \rightarrow H$ (HEFT) g.2 $pp \rightarrow Hj$ (HEFT) g.3 $pp \rightarrow Hjj$ (HEFT) g.4 $pp \rightarrow Hjj$ (HEFT)	pp>h pp>hj pp>hj	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{ll} \mbox{h.1} & pp \rightarrow HH \mbox{ (Loop improved)} \\ \mbox{h.2} & pp \rightarrow HHjj \mbox{ (VBF)} \\ \mbox{h.3} & pp \rightarrow HHW^{\pm} \end{array} $	p p > h h p p > h h j j \$\$ v+ v- z p p > h h vpn	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrr} 2.763 \pm 0.008 \cdot 10^{-2} & +11.4\% + 2.1\% \\ -11.8\% - 2.8\% \\ 6.820 \pm 0.026 \cdot 10^{-4} & +0.8\% + 2.6\% \\ 5.002 \pm 0.014 \cdot 10^{-4} & +1.5\% + 2.0\% \\ -1.2\% - 1.8\% \end{array}$
g.4 pp→Hjj(viir)	pp > n ] ] ## ## #= z	2.557 ± 0.002 · 10 -2.0% -1.4%	2.005 ± 0.000 10" _0.9% _1.5%	h.4 $pp \rightarrow HHW^{\pm}j$	p p > h h wpm j	$1.922 \pm 0.002 \cdot 10^{-4}$ $^{+14.29}_{-11.7\%} \pm 1.39$	$2.218 \pm 0.009 \cdot 10^{-4}$ $^{+2.79}_{-3.3\%}$ $^{+1.89}_{-1.1\%}$
$g_{s} = pp \rightarrow n_{fff} (vnv)$	pp>njjj## u+ u- z	2.824 ± 0.005 · 10 -12.1% -1.0%	a,085 ± 0.010 · 10 · -3.0% -1.1%	h.5' $pp \rightarrow II II W^{+} \gamma$	p p > h h wpm a	$1.952 \pm 0.004 \cdot 10^{-6}$ $^{+8.0\%}_{-3.0\%} + 2.2\%$	$2.347 \pm 0.007 \cdot 10^{-6}$ $^{+2.4\%}_{-2.0\%}$ $^{+2.1\%}_{-1.6\%}$
g.6 $pp \rightarrow HW^{\pm}$	p p > h wpm	$1.195 \pm 0.002 \cdot 10^{0}$ $^{+3.5\%}_{-4.6\%}$ $^{+1.9\%}_{-1.6\%}$	$1.419 \pm 0.005 \cdot 10^{0}$ $^{+2.1\%}_{-2.6\%}$ $^{+1.9\%}_{-1.4\%}$	h.6 $pp \rightarrow IIHZ$	pp>hhz	$2.701 \pm 0.007 \cdot 10^{-4}$ $^{+0.9\%}_{-1.3\%}$ $^{+2.0\%}_{-1.5\%}$	$3.130 \pm 0.008 \cdot 10^{-4}$ $^{+1.6\%}_{-1.2\%}$ $^{+2.0\%}_{-1.5\%}$
g.7 $pp \rightarrow HW^{\pm} j$	p p > h wpn j	$4.018 \pm 0.003 \cdot 10^{-1}$ $^{+10.7\%}_{-9.3\%}$ $^{+0.9\%}_{-0.9\%}$	$4.842 \pm 0.017 \cdot 10^{-1}$ $^{+3.675}_{-2.75}$ $^{+1.976}_{-2.75}$	h.7 $pp \rightarrow HHZj$	pp>hhzj	$1.211 \pm 0.001 \cdot 10^{-4}$ $^{+14.1\%}_{-1.1\%}$ $^{+1.4\%}_{-1.1\%}$	$1.394 \pm 0.006 \cdot 10^{-6}$ $^{+2.7\%}_{-1.0\%}$ $^{+1.5\%}_{-1.1\%}$
g.8" $pp \rightarrow HW^{\pm} jj$	p p > h wpm j j	$1.198 \pm 0.016 \cdot 10^{-1}$ $^{+96.15}_{-19.4\%}$ $^{+0.85}_{-0.6\%}$	$1.574 \pm 0.014 \cdot 10^{-1}$ $^{+5.05}_{-6.5\%}$ $^{+0.95}_{-0.6\%}$	h.8 <sup>*</sup> $pp \rightarrow HHZ\gamma$	pp>hhza	$1.397 \pm 0.003 \cdot 10^{-6} \pm 2.4\% \pm 2.2\%$	$1.604 \pm 0.005 \cdot 10^{-6} \pm 1.7\% \pm 2.3\%$
g.9 $pp \rightarrow HZ$ g.10 $pp \rightarrow HZ j$ g.11* $pp \rightarrow HZ jj$ g.12* $pp \rightarrow HW^+W^-$ (4f)	pp>hz pp>hzj pp>hzj pp>hzjj	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	h.9* $pp \rightarrow HHZZ$ h.10* $pp \rightarrow HHZW^{\pm}$ h.11* $pp \rightarrow HHW^+W^-$ (4f) h.12 $zp \rightarrow HHt\bar{t}$	p p > h h z z p p > h h z upn p p > h h u + u - p p > h h t + u -	$\begin{array}{r} -2.5\% \\ -1.7\% \\ 2.309 \pm 0.005 \cdot 10^{-6} \\ +3.9\% \\ +2.2\% \\ -3.8\% \\ -1.7\% \\ 3.708 \pm 0.013 \cdot 10^{-6} \\ +4.8\% \\ +2.3\% \\ -4.5\% \\ -1.75 \\ -1.75 \\ 7.524 \pm 0.070 \cdot 10^{-6} \\ +3.5\% \\ +2.3\% \\ -3.4\% \\ -1.7\% \\ -3.4\% \\ -1.7\% \\ -1.7\% \\ +30.2\% \\ +1.8\% \end{array}$	$\begin{array}{r} -1.4\% & -1.7\% \\ 2.754 \pm 0.009 \cdot 10^{-6} & +2.3\% & +2.3\% \\ -2.0\% & -1.7\% \\ 4.904 \pm 0.029 \cdot 10^{-6} & +3.7\% & +2.2\% \\ -3.2\% & -1.6\% \\ 9.268 \pm 0.030 \cdot 10^{-6} & +2.3\% & +2.3\% \\ 7.301 \pm 0.024 \cdot 10^{-4} & +1.4\% & +2.2\% \end{array}$
g.13 <sup>*</sup> $pp \rightarrow HW^{\pm}\gamma$	p p > h vpn a	$2.518 \pm 0.006 \cdot 10^{-3} \pm 0.2\% \pm 1.9\%$	$3.309 \pm 0.011 \cdot 10^{-3} \pm 2.7\% \pm 1.7\%$	$h_{13} \longrightarrow HHIi$	nn bhhtt i	$1.844 \pm 0.008 \pm 10^{-5} \pm 0.0\% \pm 1.8\%$	$2.444 \pm 0.000 + 10^{-5} \pm 4.5\% \pm 2.8\%$
g.14* $pp \rightarrow HZW^{\pm}$ g.15* $pp \rightarrow HZZ$	pp>hzwpn pp>hzz	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	h14" $pp \rightarrow HHb\bar{b}$	pp>hhbb~	$\begin{array}{cccccccc} -0.675 & -1.875 \\ 7.849 \pm 0.022 \cdot 10^{-8} & +34.375 \\ -31.975 & -3.775 \end{array}$	$\begin{array}{cccc} -3.1\% & -3.0\% \\ 1.084 \pm 0.012 \cdot 10^{-7} & +7.4\% & +3.1\% \\ -10.8\% & -3.7\% \end{array}$
g.16 $pp \rightarrow Ht\bar{t}$ g.17 $pp \rightarrow Ht\bar{t}$ g.18 $pp \rightarrow Hb\bar{b}$ (4f)	p p > h t t~ p p > h tt j p p > h b b~	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{rrrr} 4.608 \pm 0.016 \cdot 10^{-1} & + 5.73 + 2.03 \\ - 9.06 & - 2.96 \\ 6.328 \pm 0.022 \cdot 10^{-2} & + 5.03 + 1.53 \\ 6.085 \pm 0.026 \cdot 10^{-1} & + 7.36 \\ - 9.85 & - 2.05 \\ \end{array}$				
g.19 $pp \rightarrow H l l j$ g.20* $pp \rightarrow H b \bar{b} j$ (4f)	pp>htt~j pp>hbb~j	$\begin{array}{cccc} 2.674 \pm 0.041 \cdot 10^{-1} & + 5.68 & + 2.68 \\ & - 29.26 & - 2.976 \\ 7.367 \pm 0.002 \cdot 10^{-2} & + 55.68 & + 1.88 \\ & - 29.176 & - 2.176 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$				

Process	Syntax	Cross section (pb)		
Heavy quarks and jets		LO 1 TeV	NLO 1 TeV	
i.1 $e^+e^- \rightarrow jj$ i.2 $e^+e^- \rightarrow jjj$ i.3 $e^+e^- \rightarrow jjjj$	e+ e- > j j e+ e- > j j j e+ e- > j j j j	$\begin{array}{cccc} 6.223 \pm 0.005 \cdot 10^{-1} & +0.0\% \\ & -0.0\% \\ 3.401 \pm 0.002 \cdot 10^{-1} & +9.6\% \\ & -8.6\% \\ 1.047 \pm 0.001 \cdot 10^{-1} & +20.0\% \\ & -15.3\% \end{array}$	$\begin{array}{cccc} 6.389 \pm 0.013 \cdot 10^{-1} & +0.2\% \\ 0.019 \cdot 10^{-1} & +0.2\% \\ 3.166 \pm 0.019 \cdot 10^{-1} & +0.2\% \\ 1.090 \pm 0.006 \cdot 10^{-1} & +0.0\% \\ -2.1\% \\ 0.005 \end{array}$	
${\rm i.4} \qquad e^+e^- \mathop{\rightarrow} jjjjj$	e+ e- > j j j j j	$2.211 \pm 0.006 \cdot 10^{-2}$ $^{+31.4\%}_{-22.0\%}$	$2.771 \pm 0.021 \cdot 10^{-2}  {}^{+ 4.4 \% }_{- 8.6 \% }$	
$\begin{array}{llllllllllllllllllllllllllllllllllll$	<pre>e+ e- &gt; t t~ e+ e- &gt; t t~ j e+ e- &gt; t t~ j j e+ e- &gt; t t~ j j j e+ e- &gt; t t~ t t~ e+ e- &gt; t t~ t t~ j</pre>	$\begin{array}{rrrr} 1.662\pm 0.002\cdot 10^{-1} & +0.0\% \\ -0.0\% \\ 4.813\pm 0.005\cdot 10^{-2} & +9.3\% \\ -7.8\% \\ 8.614\pm 0.009\cdot 10^{-3} & +19.4\% \\ 1.044\pm 0.002\cdot 10^{-3} & +30.5\% \\ 6.456\pm 0.016\cdot 10^{-7} & +19.1\% \\ -14.8\% \\ 2.719\pm 0.005\cdot 10^{-8} & +29.9\% \\ -21.3\% \end{array}$	$\begin{array}{rrrr} 1.745 \pm 0.006 \cdot 10^{-1} & +0.4\% \\ & -0.4\% \\ 5.276 \pm 0.022 \cdot 10^{-2} & +1.3\% \\ 1.094 \pm 0.005 \cdot 10^{-2} & +5.0\% \\ 1.546 \pm 0.010 \cdot 10^{-3} & +10.6\% \\ 1.221 \pm 0.005 \cdot 10^{-6} & +13.2\% \\ 5.338 \pm 0.027 \cdot 10^{-8} & +18.3\% \\ & -15.4\% \end{array}$	
$\begin{array}{lll} {\rm i.11} & e^+e^- \to b\bar{b} \ (4{\rm f}) \\ {\rm i.12} & e^+e^- \to b\bar{b}j \ (4{\rm f}) \\ {\rm i.13}^* & e^+e^- \to b\bar{b}jj \ (4{\rm f}) \\ {\rm i.14}^* & e^+e^- \to b\bar{b}jjj \ (4{\rm f}) \\ {\rm i.15}^* & e^+e^- \to b\bar{b}b\bar{b} \ (4{\rm f}) \\ {\rm i.16}^* & e^+e^- \to b\bar{b}b\bar{b}\bar{b}j \ (4{\rm f}) \end{array}$	e* e- > b b~ e+ e- > b b~ j e* e- > b b~ j j e* e- > b b~ j j e* e- > b b~ b b~ e* e- > b b~ b b~	$\begin{array}{rrrr} 9.198 \pm 0.004 \cdot 10^{-2} & +0.0\% \\ -0.0\% \\ 5.029 \pm 0.003 \cdot 10^{-2} & +9.5\% \\ 1.621 \pm 0.001 \cdot 10^{-2} & +20.0\% \\ 3.641 \pm 0.009 \cdot 10^{-3} & +31.4\% \\ 1.644 \pm 0.003 \cdot 10^{-4} & +19.9\% \\ 7.660 \pm 0.022 \cdot 10^{-5} & +31.3\% \\ -22.0\% \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	
$ \begin{array}{ll} \mathrm{i.17^{*}} & e^+e^- \rightarrow t \overline{t} b \overline{b} \ (\mathrm{4f}) \\ \mathrm{i.18^{*}} & e^+e^- \rightarrow t \overline{t} b \overline{b} j \ (\mathrm{4f}) \end{array} $	e+ e- > t t∼ b b~ e+ e- > t t∼ b b~ j	$\begin{array}{rrrr} 1.819 \pm 0.003\cdot 10^{-4} & {}^{+19.5\%}_{&-15.0\%} \\ 4.045 \pm 0.011\cdot 10^{-5} & {}^{+30.5\%}_{&-21.6\%} \end{array}$	$\begin{array}{rrrr} 2.923 \pm 0.011 \cdot 10^{-4} & +9.2\% \\ -8.9\% \\ 7.049 \pm 0.052 \cdot 10^{-5} & +13.7\% \\ -13.1\% \end{array}$	

Process		Syntax	Cross section (pb)				
Top o	quarks +bosons		LO 1 TeV	NLO 1 TeV			
j.1	$e^+e^- \rightarrow t\bar{t}H$	e+ e- > t t~ h	$2.018 \pm 0.003 \cdot 10^{-3}$	$^{+0.0\%}_{-0.0\%}$ 1.911 ± 0.006 · 10 <sup>-3</sup> $^{+0.4\%}_{-0.5\%}$			
j.2*	$e^+e^- \rightarrow t\bar{t}Hj$	e+ e- > t t~ h j	$2.533 \pm 0.003 \cdot 10^{-4}$	$^{+9.2\%}_{-7.8\%}$ 2.658 ± 0.009 · 10 <sup>-4</sup> $^{+0.5\%}_{-1.5\%}$			
j.3*	$e^+e^- \rightarrow t\bar{t}Hjj$	e+ e- > t t~ h j j	$2.663 \pm 0.004 \cdot 10^{-5}$	$^{+19.3\%}_{-14.9\%}$ 3.278 $\pm$ 0.017 $\cdot$ 10 <sup>-5</sup> $^{+4.0\%}_{-5.7\%}$			
j.4*	$e^+e^- \rightarrow t\bar{t}\gamma$	$e+e- > t t \sim a$	$1.270 \pm 0.002 \cdot 10^{-2}$	$^{+0.0\%}_{-0.0\%}$ 1.335 ± 0.004 · 10 <sup>-2</sup> $^{+0.5\%}_{-0.4\%}$			
j.5*	$e^+e^- \rightarrow t\bar{t}\gamma j$	e+ e- > t t∼ a j	$2.355 \pm 0.002 \cdot 10^{-3}$	$^{+9.3\%}_{-7.9\%}$ 2.617 ± 0.010 · 10 <sup>-3</sup> $^{+1.6\%}_{-2.4\%}$			
j.6*	$e^+e^- \rightarrow t\bar{t}\gamma jj$	e+ e- > t t~ a j j	$3.103 \pm 0.005 \cdot 10^{-4}$	$^{+19.5\%}_{-15.0\%}$ $4.002 \pm 0.021 \cdot 10^{-4}$ $^{+5.4\%}_{-6.6\%}$			
j.7*	$e^+e^- \rightarrow t\bar{t}Z$	e+ e- > t t~ z	$4.642 \pm 0.006 \cdot 10^{-3}$	$^{+0.0\%}_{-0.0\%}$ 4.949 ± 0.014 · 10 <sup>-3</sup> $^{+0.6\%}_{-0.5\%}$			
j.8*	$e^+e^- \rightarrow t\bar{t}Zj$	e+ e- > t t~ z j	$6.059 \pm 0.006 \cdot 10^{-4}$	$^{+9.3\%}_{-7.8\%}$ 6.940 ± 0.028 · 10 <sup>-4</sup> $^{+2.0\%}_{-2.6\%}$			
j.9*	$e^+e^- \rightarrow t\bar{t}Zjj$	e+ e- > t t~ z j j	$6.351 \pm 0.028 \cdot 10^{-5}$	$^{+19.4\%}_{-15.0\%}$ 8.439 $\pm$ 0.051 $\cdot$ 10 <sup>-5</sup> $^{+5.8\%}_{-6.8\%}$			
j.10*	$e^+e^- \to t\bar{t}W^\pm jj$	e+ e- > t t $\sim$ wpm j j	$2.400 \pm 0.004 \cdot 10^{-7}$	$^{+19.3\%}_{-14.9\%}$ 3.723 $\pm$ 0.012 $\cdot$ 10 <sup>-7</sup> $^{+9.6\%}_{-9.1\%}$			
j.11*	$e^+e^- \rightarrow t\bar{t}HZ$	e+ e- > t t∼ h z	$3.600 \pm 0.006\cdot 10^{-5}$	$^{+0.0\%}_{-0.0\%}$ 3.579 ± 0.013 · 10 <sup>-8</sup> $^{+0.1\%}_{-0.0\%}$			
j.12*	$e^+e^- \rightarrow t\bar{t}\gamma Z$	e+ e- > t t~ a z	$2.212\pm 0.003\cdot 10^{-4}$	$^{+0.0\%}_{-0.0\%}$ 2.364 ± 0.006 · 10 <sup>-4</sup> $^{+0.6\%}_{-0.5\%}$			
j.13*	$e^+e^- \rightarrow t\bar{t}\gamma H$	$e + e - > t t \sim a h$	$9.756 \pm 0.016 \cdot 10^{-5}$	$^{+0.0\%}_{-0.0\%}$ 9.423 ± 0.032 · 10 <sup>-5</sup> $^{+0.3\%}_{-0.4\%}$			
j.14*	$e^+e^- \rightarrow t\bar{t}\gamma\gamma$	e+ e- > t t∼ a a	$3.650 \pm 0.008 \cdot 10^{-4}$	$^{+0.0\%}_{-0.0\%}$ 3.833 ± 0.013 · 10 <sup>-4</sup> $^{+0.4\%}_{-0.4\%}$			
j.15*	$e^+e^- \rightarrow t\bar{t}ZZ$	e+ e- > t t∼ z z	$3.788 \pm 0.004 \cdot 10^{-5}$	$^{+0.0\%}_{-0.0\%}$ 4.007 ± 0.013 · 10 <sup>-8</sup> $^{+0.5\%}_{-0.5\%}$			
j.16*	$e^+e^- \rightarrow t\bar{t}HH$	$e + e - > t t \sim h h$	$1.358 \pm 0.001 \cdot 10^{-5}$	$^{+0.0\%}_{-0.0\%}$ 1.206 ± 0.003 · 10 <sup>-5</sup> $^{+0.9\%}_{-1.1\%}$			
j.17*	$e^+e^- \mathop{\rightarrow} t\bar{t}W^+W^-$	e+ e- > t t∼ ¥+ ¥-	$1.372\pm0.003\cdot10^{-4}$	$^{+0.0\%}_{-0.0\%}$ 1.540 ± 0.006 · 10 <sup>-4</sup> $^{+1.0\%}_{-0.9\%}$			























































### Plan







# Loop Induced



#### Why?

- Main production mechanism for Higgs & Higgs associated processes
- Contribution for NNLO computation
- Correction to shape of observables

#### **Difficulties?**

- The phase-space integration is based on the born diagram
- Loop evaluation are extremely slow
- Need Leading Color information for writing Events associated to the loop



## **ME-Reweighting**



•Idea: use one (un)weighted generations and associate additional weights from different hypothesis.

$$W_{new} = \frac{|M_{new}|^2}{|M_{old}|^2} * W_{old}$$



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# g g > ZH







# Loop Induced



#### Why?

- Main production mechanism for Higgs & Higgs associated processes
- Contribution for NNLO computation
- Correction to Shape of observables

#### **Difficulties?**

- •The phase-space integration is based on the born diagram
- Loop evaluation are extremely slow
- Need Leading Color information for writing Events associated to the loop



## **Exact Integration**



#### Difficulties?

- •The phase-space integration is based on the born diagram
- Loop evaluation are extremely slow
- Need Leading Color information for writing Events associated to the loop

#### Solution

- Contract the loop to have tree-level diagrams which drive the integration multichannel
- •Use Monte-Carlo over helicity
- Increase parallelization
- •Compute the loop with the color flow algebra



## **Exact Integration**



#### **Difficulties?**

- •The phase-space integration is based on the born diagram
- Loop evaluation are extremely slow
- Need Leading Color information for writing Events associated to the loop

#### Solution

- Contract the loop to have tree-level Anich drive Legration mess Lannel •Use Mc An PRASUIT hel: WORK Maran Result hel: work or any result warming: remainder the second secon

sompute the loop with the color flow algebra

# First Example: g g> h





# First Example: g g> h
















# Validation



- Comparison of g g > h g between
  - → heft
  - loop induced
  - re-weighting





#### Validation







#### Validation







### Matched/Merged



# Higgs Production up to two loop not considering the VBS production





# Three Higgs



#### Important for the quartic term



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# Three Higgs



•What is the sensitivity in the 4 Higgs coupling:





# 



 Same sign top discovery will be the proof of New Physics but this process exists in the SM



•QED Loop

suppressed by CKM/bottom mass





# p p > h+ h-



#### Model

- 2HDM type II (generate via NLOCT)
- massive b

Loop

 $\sigma_{loop} = 0.00803(1)pb$ 





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#### Status



- 2 to 2 processes: OK on a laptop
- 2 to 3 processes: OK on a small size cluster
- 2 to 4 processes: Specific case

$ m Process  m Single \ boson + jets$		Syntax	Cross section (pb) 13 TeV	
a.1 pp - a.2 pp - a.3 pp -	$ \begin{array}{l} \rightarrow H \\ \rightarrow Hj \\ \rightarrow Hjj \end{array} $	<pre>p p &gt; h [noborn=QCD] p p &gt; h j [noborn=QCD] p p &gt; h j j [noborn=QCD]</pre>	$17.77 \pm 0.060$ $14.82 \pm 0.010$ $8.807 \pm 0.010$	$\begin{array}{rrrr} +31.3\% & +0.7\% \\ -23.1\% & -1.0\% \\ +43.9\% & +0.6\% \\ -28.4\% & -0.9\% \\ +65.3\% & +0.8\% \\ -36.9\% & -1.0\% \end{array}$
a.4 gg - a.5 gg -	$ \begin{array}{l} \rightarrow Zg \\ \rightarrow Zgg \end{array} $	g g > z g [noborn=QCD] g g > z g g [noborn=QCD]	$\begin{array}{c} 51.80 \pm 0.050 \\ 0.0  {}^{0\%}_{0\%}  {}^{0\%}_{0\%} \end{array}$	+46.3% +0.7% -29.4% -1.1%
a.6 gg - a.7 gg -	$ ightarrow \gamma g$ $ ightarrow \gamma g g$	g g > a g [noborn=QCD] g g > a g g [noborn=QCD]	$\begin{array}{cccc} 0.0 & 0\% & 0\% \\ 0\% & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0\% & 0\% & 0\% \end{array}$	

Process	Syntax	Cross section (pb)	
$Double \ bosons + jet$		13 TeV	
b.1 $pp \rightarrow HH$	p p > h h [noborn=QCD]	$1.547 \pm 0.002 \cdot 10^{-2}$ $^{+29.5\%}_{-21.4\%}$ $^{+1.3\%}_{-1.3\%}$	
b.2 $pp \rightarrow HHj$	p p > h h j [noborn=QCD]	$0.0  \begin{array}{c} 0\% & 0\% \\ 0\% & 0\% \end{array}$	
b.3 $pp \rightarrow H\gamma j$	p p > h a j [noborn=QCD]	$0.0  \begin{array}{c} 0\% & 0\% \\ 0\% & 0\% \end{array}$	
b.4 $gg \rightarrow HZ$	g g > h z [noborn=QCD]	$6.180 \pm 0.010 \cdot 10^{-2}  {}^{+28.7\%}_{-20.9\%}  {}^{+1.1\%}_{-1.2\%}$	
b.5 $gg \rightarrow HZg$	g g > h z g [noborn=QCD]	$0.0 {}^{0\%}_{0\%}{}^{0\%}_{0\%}$	
b.6 $gg \rightarrow ZZ$	g g > z z [noborn=QCD]	$1.182 \pm 0.003$ $^{+26.5\%}_{-19.8\%}$ $^{+0.7\%}_{-10\%}$	
b.7 $gg \rightarrow ZZg$	g g > z z g [noborn=QCD]	$0.0  \begin{array}{c} 0\% & 0\% \\ 0\% & 0\% \end{array}$	
b.8 $gg \rightarrow Z\gamma$	g g > z a [noborn=QCD]	$1.211 \pm 0.006 \qquad \begin{array}{c} +29.2\% +0.8\% \\ -21.7\% -1.1\% \end{array}$	
b.9 $gg \rightarrow Z\gamma g$	g g > z a g [noborn=QCD]	$0.0 {}^{0\%}_{0\%}{}^{0\%}_{0\%}$	
b.10 $gg \rightarrow \gamma \gamma$	g g > a a [noborn=QCD]	$5.119 \pm 0.007 \cdot 10^{+2} + 68.8\% + 1.1\% - 42.0\% - 1.5\%$	
b.11 $gg \rightarrow \gamma \gamma g$	gg>aag[noborn=QCD]	$0.0  \begin{array}{c} 0\% & 0\% \\ 0\% & 0\% \end{array} \qquad $	
b.12 $gg \rightarrow W^+W^+$	g g > w+ w- [noborn=QCD]	$3.698 \pm 0.010$ $^{+26.0\%}_{-19.4\%}$ $^{+0.7\%}_{-10.0\%}$	
b.13 $gg \rightarrow W^+W^-g$	g g > w+ w- g [noborn=QCD]	$0.0  \begin{array}{c} 0\% & 0\% \\ 0\% & 0\% \end{array}$	

Process Triple bosons	Syntax	Cross section (pb) 13 TeV
$ \begin{array}{ccc} c.1 & pp \rightarrow HH \\ c.2 & gg \rightarrow HH \\ c.3 & gg \rightarrow HZ \\ c.4 & gg \rightarrow HZ' \\ c.5 & pp \rightarrow H\gamma \\ c.6 & pp \rightarrow HW \end{array} $	$ \begin{array}{llllllllllllllllllllllllllllllllllll$	$ \begin{bmatrix} 0.0 & 0\% & 0\% \\ 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0\% & $
$ \begin{array}{ccc} {\rm c.7} & gg \rightarrow ZZZ\\ {\rm c.8} & gg \rightarrow ZZ\gamma\\ {\rm c.9} & gg \rightarrow Z\gamma\gamma\\ {\rm c.10} & gg \rightarrow ZW \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{bmatrix} 0.0 & 0\% & 0\% \\ 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\ 0.0 & 0\% & 0\% \\$
c.11 $gg \rightarrow \gamma\gamma\gamma$ c.12 $gg \rightarrow \gamma W$	gg > a a [noborn=QCD] $^+W^-$ gg > a w+ w- [noborn=QCD]	$\begin{bmatrix} 0.0 & 0\% & 0\% \\ 0\% & 0\% & 0\% \\ \text{CD} \end{bmatrix}  0.0 & 0\% & 0\% \\ 0\% & 0\% & 0\% \end{bmatrix}$

Process Selected $2 \rightarrow 4$	Syntax	Cross section (pb) 13 TeV
$ \begin{array}{ccc} \text{d.1} & pp \rightarrow Hjjj \\ \text{d.2} & pp \rightarrow HHjj \\ \text{d.3} & gg \rightarrow e^+e^-\mu^+\mu^- \\ \text{d.4} & pp \rightarrow HZ\gamma j \\ \text{d.5} & gg \rightarrow W^+W^-W^+W^- \end{array} $	<pre>p p &gt; h j j j [noborn=QCD] p p &gt; h h j j [noborn=QCD] g g &gt; e+ e- mu+ mu- [noborn=QCD] g g &gt; h z a g [noborn=QCD] g g &gt; w+ w- w+ w- [noborn=QCD]</pre>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$e^+e^-$ processes		$\hat{s} = 500 \text{ GeV}$
e.1 $e^+e^- \rightarrow ggg$ e.2 $e^+e^- \rightarrow HH$ e.3 $e^+e^- \rightarrow HHgg$	e+ e- > g g g [noborn=QED] e+ e- > h h [noborn=QED] e+ e- > h h g g [noborn=QED]	$\begin{array}{cccccccccccccccccccccccccccccccccccc$



### Conclusion





# Demo

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#### Demo Plan



#### Example I: HEFT

- Model Description
- Width Computation
- Decay Chain

#### Example II: MSSM

- Fermion Flow
- Model support
- Systematics

#### Example III: NLO



### **Effective Operator**



• New Physics at (too?) High Energy



#### **Effective Operator**



• New Physics at (too?) High Energy







• New Physics at (too?) High Energy







• New Physics at (too?) High Energy



Additional terms in the Lagrangian  $\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2}\mathcal{L}_6 + \frac{1}{\Lambda^4}\mathcal{L}_8 + \dots$ 





• New Physics at (too?) High Energy



Solution Additional terms in the Lagrangian  $\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$ 

### - Effective Field Theory



$$\mathcal{L} = \mathcal{L}_{SM} + \sum rac{c_i}{\Lambda^2} \mathcal{O}_i$$

- The number of possible Operators are huge
  - 59 Dimension 6 Operators If
     Preserve the SM gauge symmetries
     Preserve B-L accidental symmetries
     We consider only one flavor

### - Effective Field Theory



$$\mathcal{L} = \mathcal{L}_{SM} + \sum rac{c_i}{\Lambda^2} \mathcal{O}_i$$

The number of possible Operators are huge

- 59 Dimension 6 Operators If
   Preserve the SM gauge symmetries
   Preserve B-L accidental symmetries
   We consider only one flavor
- Only One Dimension 5 Operator:  $\mathcal{O} = LHLH$ Give a mass to the neutrino

### - Effective Field Theory



$$\mathcal{L} = \mathcal{L}_{SM} + \sum rac{c_i}{\Lambda^2} \mathcal{O}_i$$

Only few Operators for one process and different effects



 $\mathcal{O}_{WWW} = \operatorname{Tr}[W_{\mu\nu}W^{\nu\rho}W^{\mu}_{\rho}]$  $\mathcal{O}_{W} = (D_{\mu}\Phi)^{\dagger}W^{\mu\nu}(D_{\nu}\Phi)$  $\mathcal{O}_{B} = (D_{\mu}\Phi)^{\dagger}B^{\mu\nu}(D_{\nu}\Phi)$ 

$$\mathcal{O}_{\tilde{W}WW} = \operatorname{Tr}[W_{\mu\nu}W^{\nu\rho}W^{\mu}_{\rho}]$$
$$\mathcal{O}_{\tilde{W}} = (D_{\mu}\Phi)^{\dagger}\tilde{W}^{\mu\nu}(D_{\nu}\Phi)$$



### Demo 1





- import model EWDim6
- •generate p p > w- z
- output
- launch

#### SM + Interference

- •import model EWDim6
- •generate  $p p > w z NP^2 <= 2$
- output
- launch



### 2-body decay







### 2-body decay



2 body decay

$$\Gamma = \frac{1}{2MS} \int d\Phi_2 |\mathcal{M}|^2$$

•By Lorentz Invariance the matrix element is constant over the phase-space.

$$\Gamma = \frac{\sqrt{\lambda(M^2, m_1^2, m_2^2)} |\mathcal{M}|^2}{16\pi S M^3}$$
$$\Lambda(M^2, m_1^2, m_2^2) = \left(M^2 - m_1^2 - m_2^2\right)^2 - 4m_1^2 m_2^2$$



### 2-body decay



2 body decay

$$\Gamma = \frac{1}{2MS} \int d\Phi_2 |\mathcal{M}|^2$$

•By Lorentz Invariance the matrix element is constant over the phase-space.

$$\Gamma = \frac{\sqrt{\lambda(M^2, m_1^2, m_2^2)} |\mathcal{M}|^2}{16\pi S M^3}$$
$$(M^2, m_1^2, m_2^2) = (M^2 - m_1^2 - m_2^2)^2 - 4m_1^2 m_2^2$$

#### Calculable analytically by FeynRules



# N Body Decay



#### 3(and more)-body Decay

- Analytical Formula too complicated
  - Especially in a spectrum independent way
  - Numerical integration
- Need to remove double counting with 2body
- Typically LO computation
  - Remove radiation diagram

Example of code

•Herwig / Bridge / MadWidth







2-body

•Use FeynRules formula (instantaneous)







2-body •Use FeynRules formula (instantaneous) Fast-Estimation of 3-body Only use 2-body decay and **PS** factor



























# MadWidth







# MadWidth























#### Demo 2



- MadWidth
- •Run\_card
















Problem
 Process complicated to have the full process

#### Including off-shell contribution









Problem
 Process complicated to have the full process

Including off-shell contribution

Solution

Only keep on-shell contribution

#### Marrow-Width Approx.





#### Comment

#### **Narrow-Width Approx.**









#### Decay chains

• 
$$p p > t t \sim w+, (t > w+ b, w+ > |+ v|), (t \sim > w- b \sim, w- > j j), (w+ > |+ v|)$$

- Separately generate core process and each decay
   Decays generated with the decaying particle as resulting wavefunction
- Iteratively combine decays and core processes
- Difficulty: Multiple diagrams in decays



# Decay chains



- •Decay chains retain full matrix element for the diagrams compatible with the decay
- Full spin correlations (within and between decays)
- •Full width effects
- •However, no interference with non-resonant diagrams
  - Description only valid close to pole mass
  - ➡ Cutoff at Im ± nFl where n is set in run\_card.



#### **Decay chains**





Results for g g > go go , (go > t1 t~, t~> b~ all all / h+ , (t1 > t n1 , t > b all all / h+)) in the mssm

#### **Available Results**

Links	Events	Tag	Run	Collider	Cross section (pb)	Events
results banner	Parton-level LHE	fermi	test	p p 7000 x 7000 GeV	.33857E-03	10000

#### Main Page

# Thanks to developments in MadEvent, also (very) long decay chains possible to simulate directly in MadGraph!

Mattelaer Olívier





#### Read Event

generate a virtual mass

generate a decay







generate a virtual mass

#### generate a decay

- Finite width
- Spin correlation
- unweighted events







unweighted events







generate a virtual mass



associate a weight to the event

 $|M_{LO}^{P+D}|^2 / |M^{P_{LO}}|^2$ 































Mattelaer Olívíer







Mattelaer Olívíer







Mattelaer Olívíer



#### Demo 3



Decay ChainMadSpin



#### Spin/Color







#### Spin/Color





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#### **Systematics**







#### Demo



Demo
SysCalc





- •NLO corrections have three parts:
  - The Born contribution, i.e. the Leading order.
  - Virtual (or Loop) corrections: a closed loop of particles interfered with the Born amplitudes
  - Real emission corrections: one extra parton compared to the Born process
- •Both Virtual and Real emission have one power of  $\alpha_s$  extra compared to the Born process

$$\sigma^{\rm NLO} = \int_m d\sigma^B + \int_m d\sigma^V + \int_{m+1} d\sigma^R$$











$$\hat{\sigma} = \sigma^{\text{Born}} \left( 1 + \frac{\alpha_s}{2\pi} \sigma^{(1)} + \dots \right)$$





$$\hat{\sigma} = \sigma^{\text{Born}} \left( 1 + \frac{\alpha_s}{2\pi} \sigma^{(1)} + \dots \right)$$



















#### - Fixed Order calculations



#### - Fixed Order calculations





#### Demo



# Demo NLO Fix Order Matched to the shower

#### Summary





- Presentation of MadGraph5
  - Support of BSM
  - Computation of the Width
  - Narrow width Approximation
    - Decay Chain
    - MadSpin
  - Systematics
  - •NLO




## NLO HEFT event generation: MC@NLO method

$$d\sigma^{(\mathbb{H})} = d\phi_{n+1} \left( \mathcal{R} - \mathcal{C}_{MC} \right) ,$$
  
$$d\sigma^{(\mathbb{S})} = d\phi_{n+1} \left[ \left( \mathcal{B} + \mathcal{V} + \mathcal{C}^{int} \right) \frac{d\phi_n}{d\phi_{n+1}} + \left( \mathcal{C}_{MC} - \mathcal{C} \right) \right]$$

- Different weights stored internally: virtual, real and counter terms
- Reweight on an event-by-event basis using the results of the exact loop matrix elements. Schematically:

 $\mathcal{B}, \mathcal{V}, \mathcal{C}^{(int)}, \mathcal{C}_{MC} \times \mathcal{B}_{FT}/\mathcal{B}_{HEFT}$  $\mathcal{R} \times \mathcal{R}_{FT}/\mathcal{R}_{HEFT}$ 

- Fully differential re-weighting
- Matching to parton showers with the MC@NLO method

[1401.7340 and 1408.6542]











