

# FeynRules

<http://europa.fyma.ucl.ac.be/feynrules>

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In collaboration with:

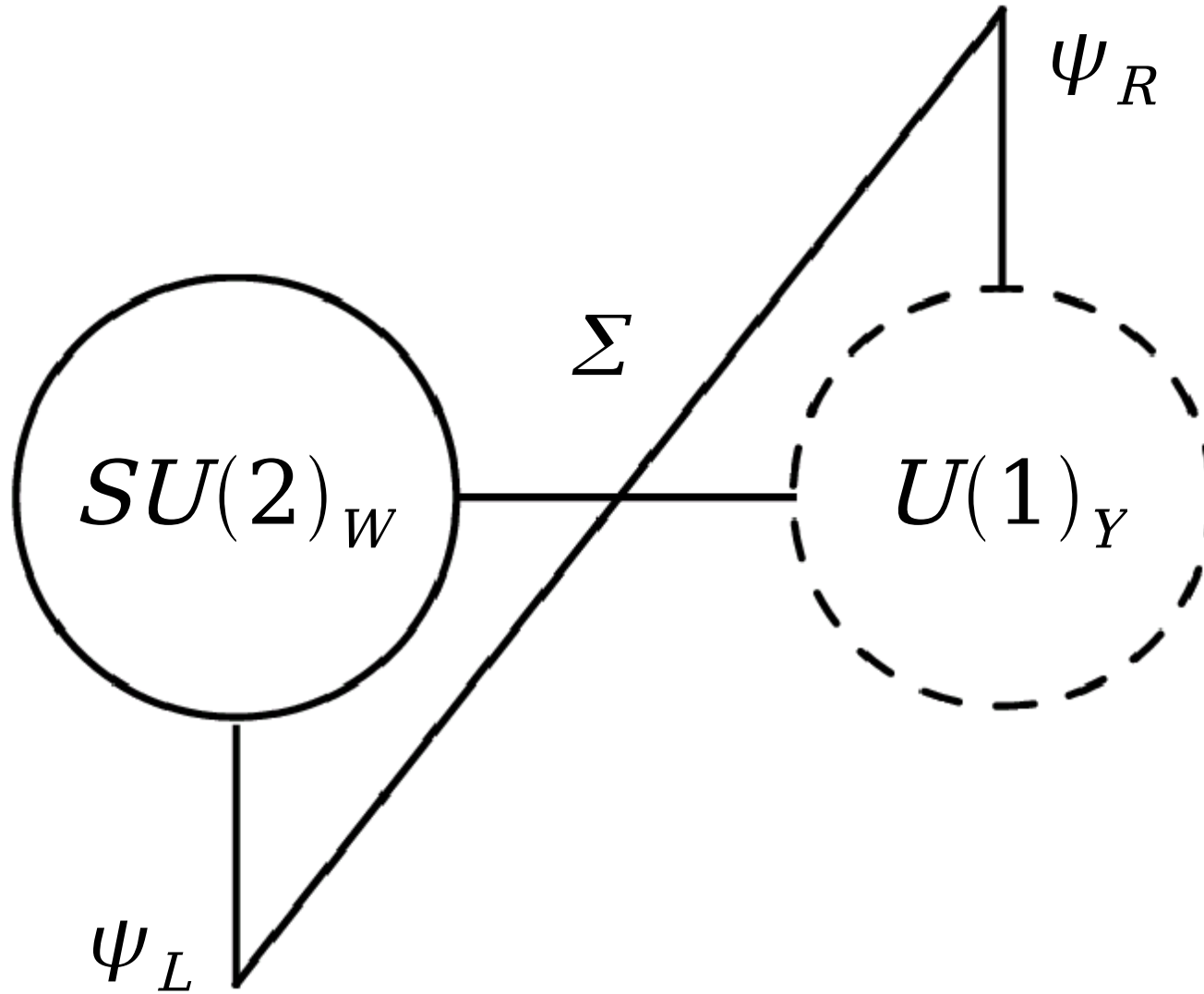
**Claude Duhr**

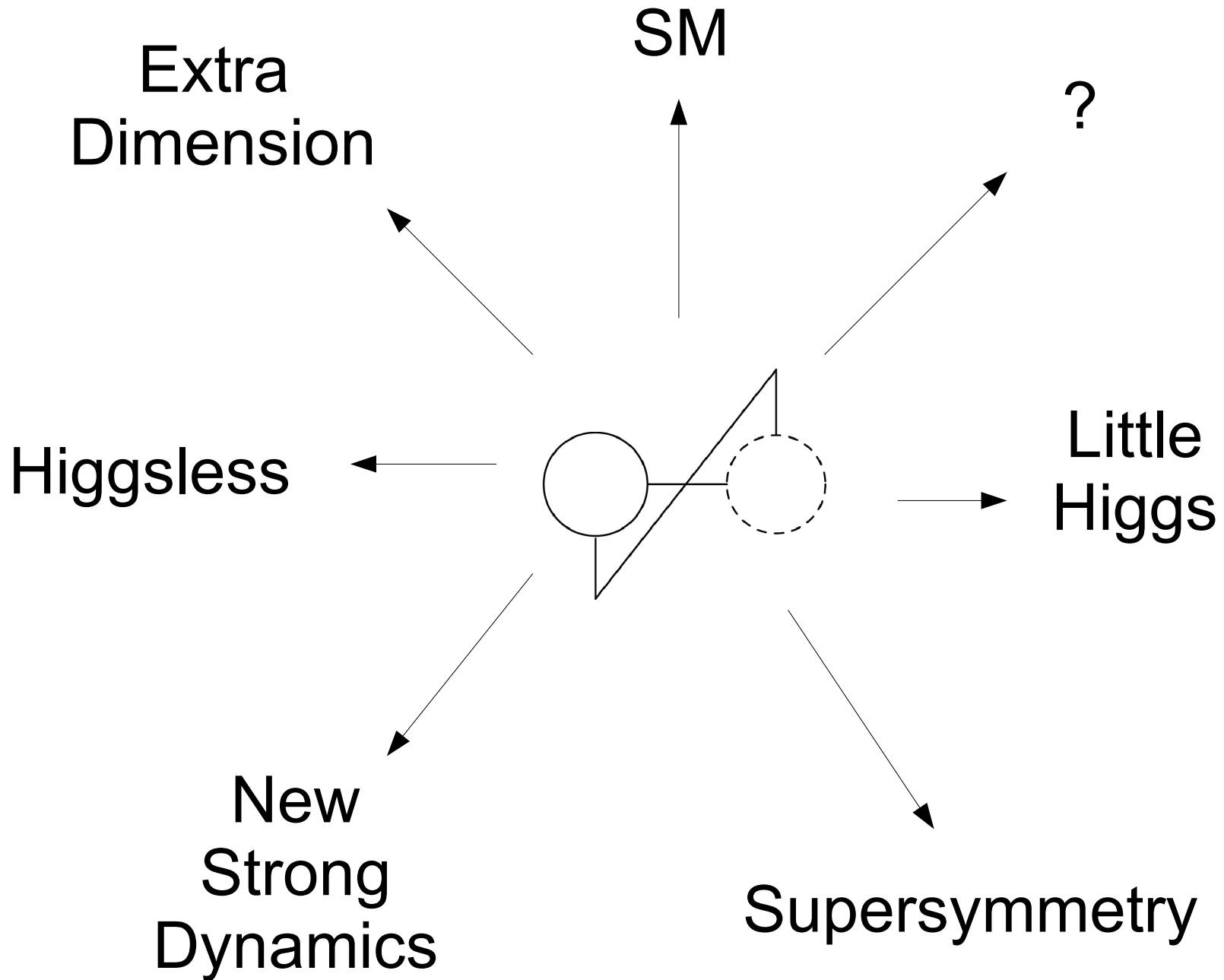
Fabio Maltoni

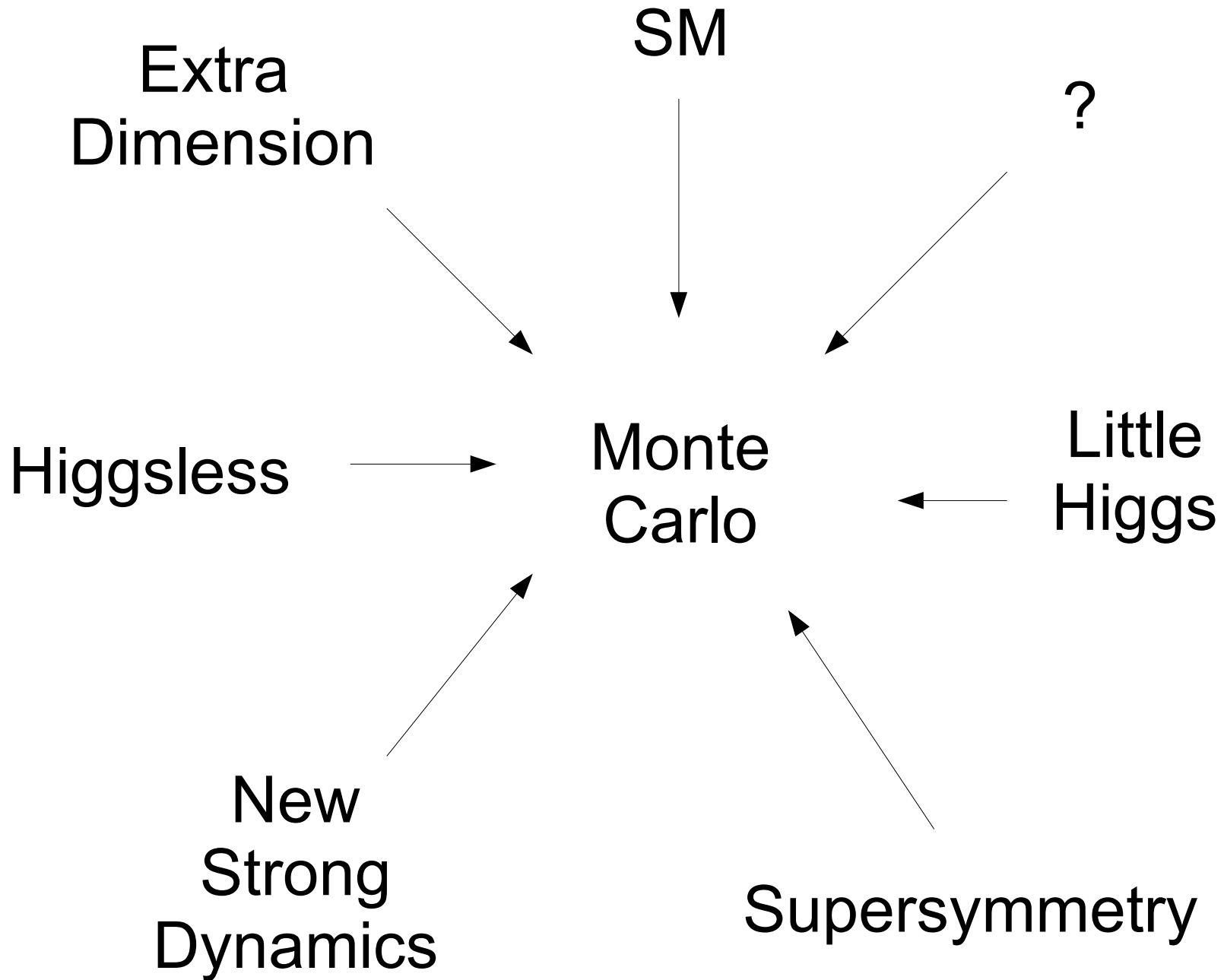
Michell Herquet

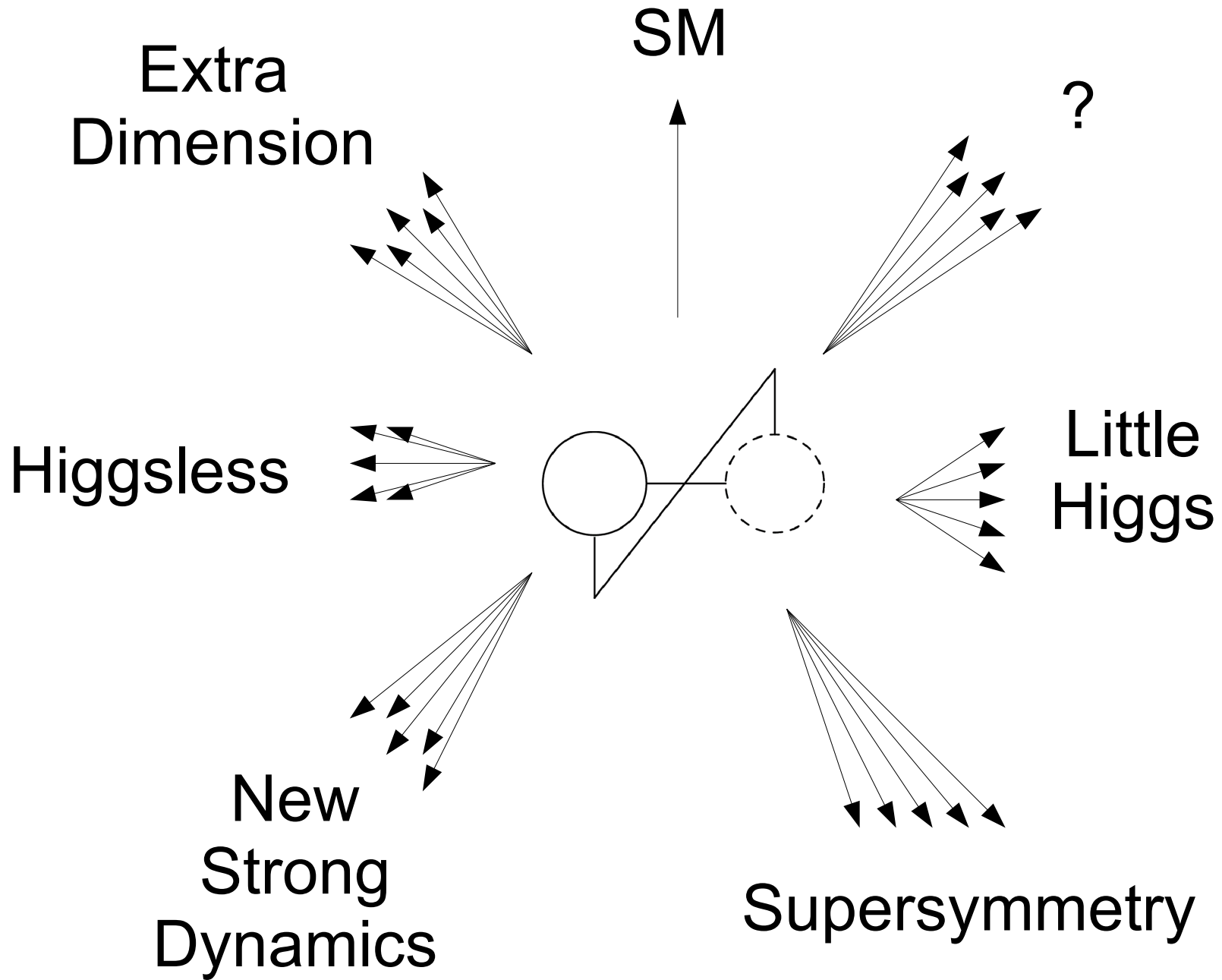
Steffen Schumann

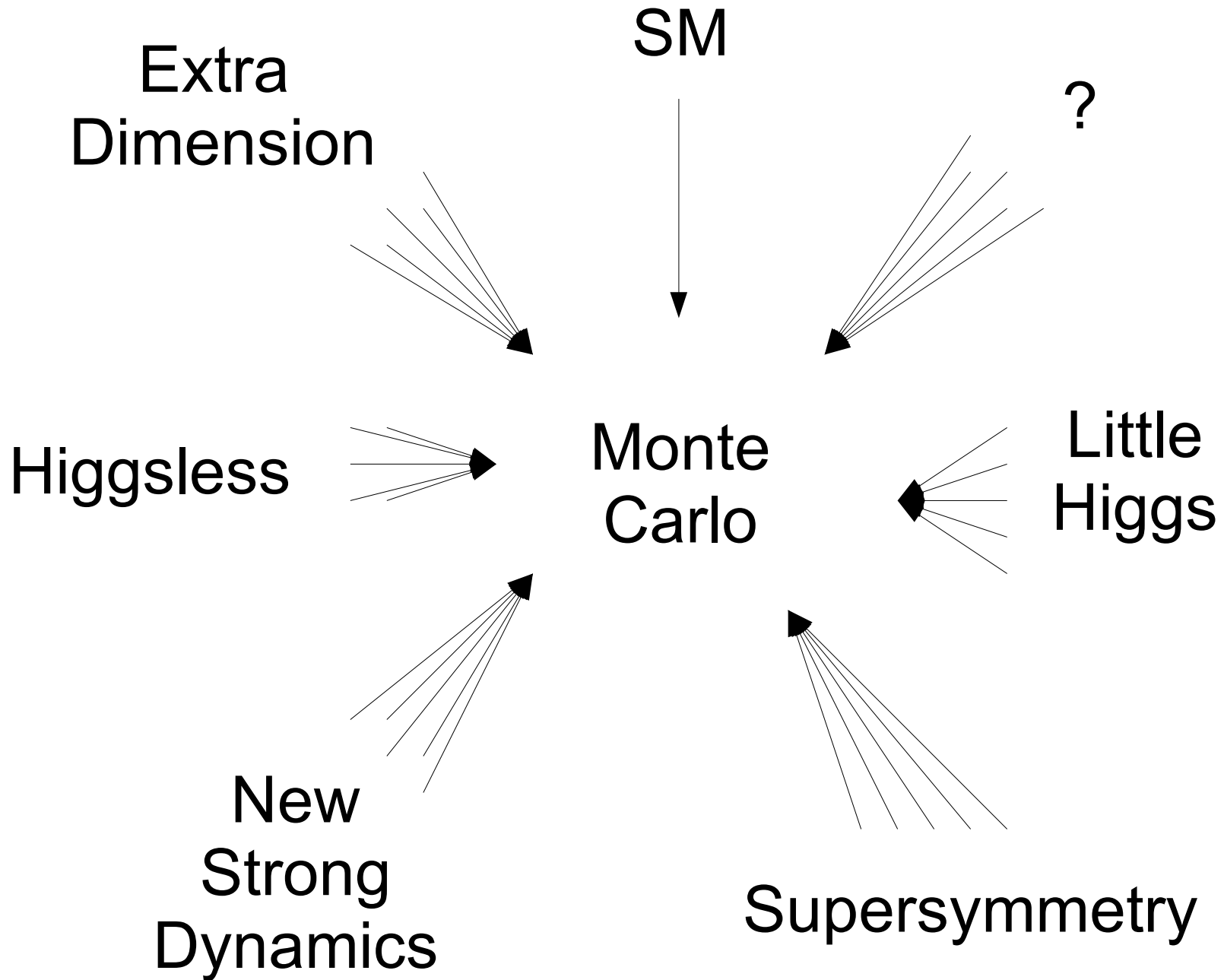
# HSM

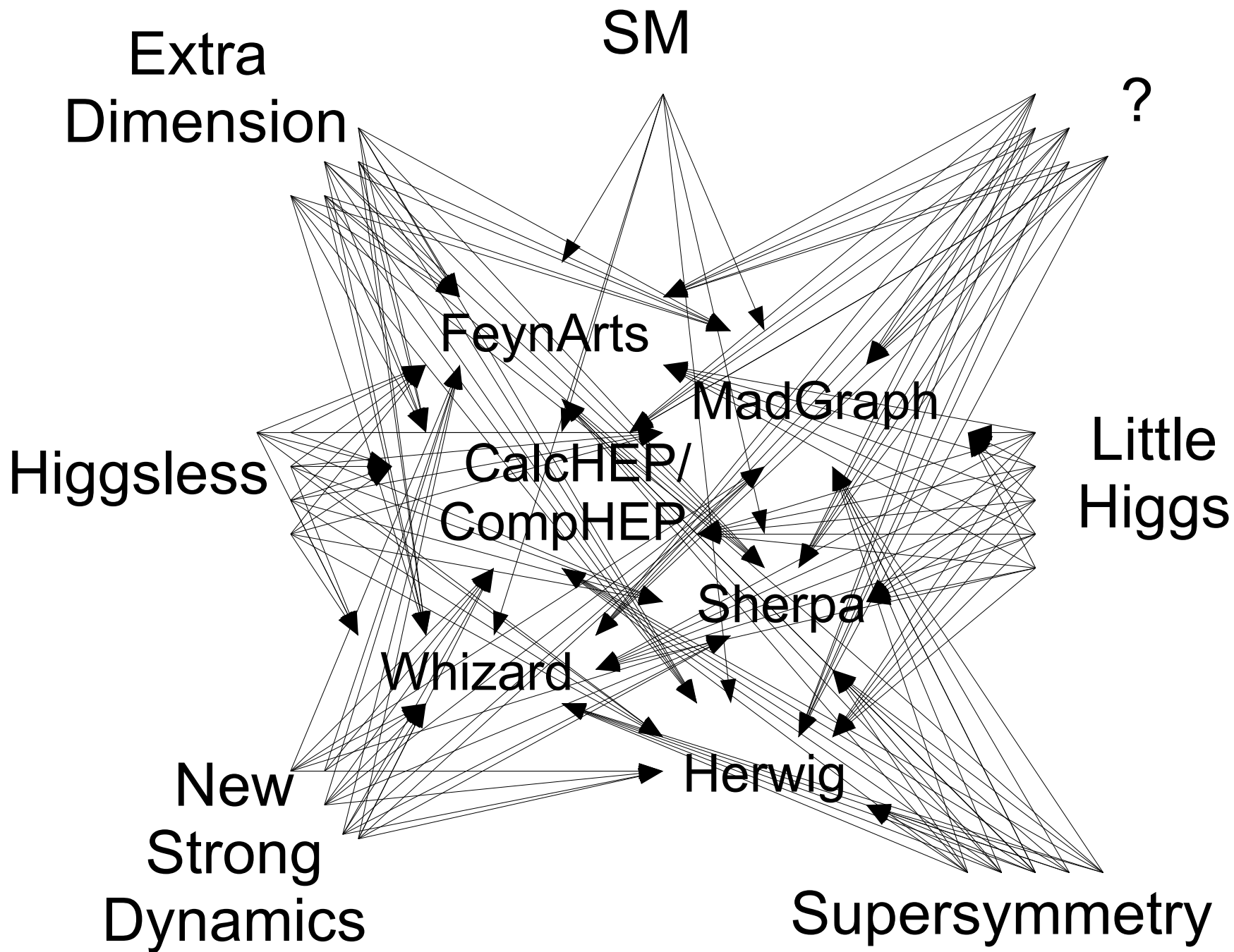


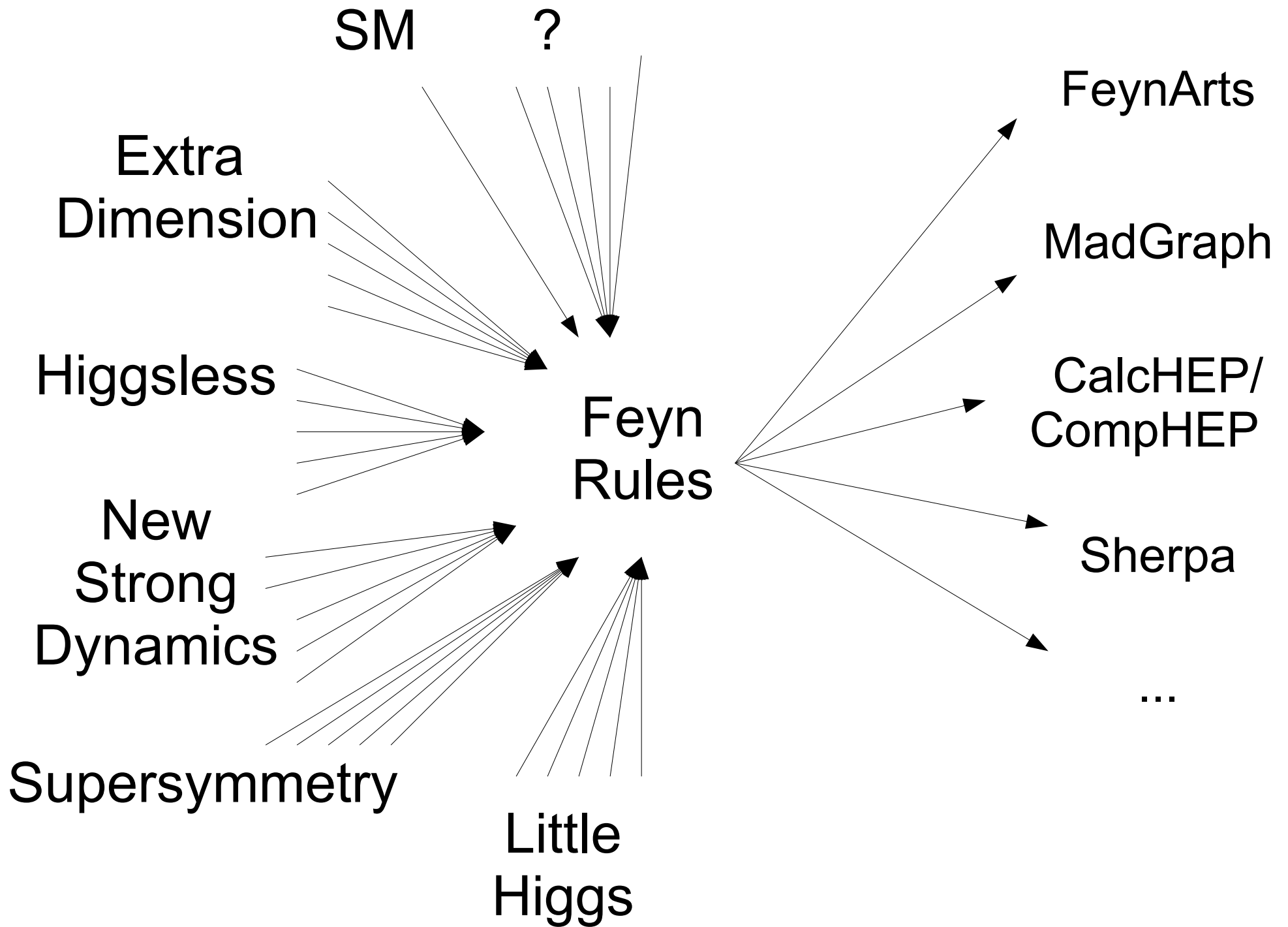




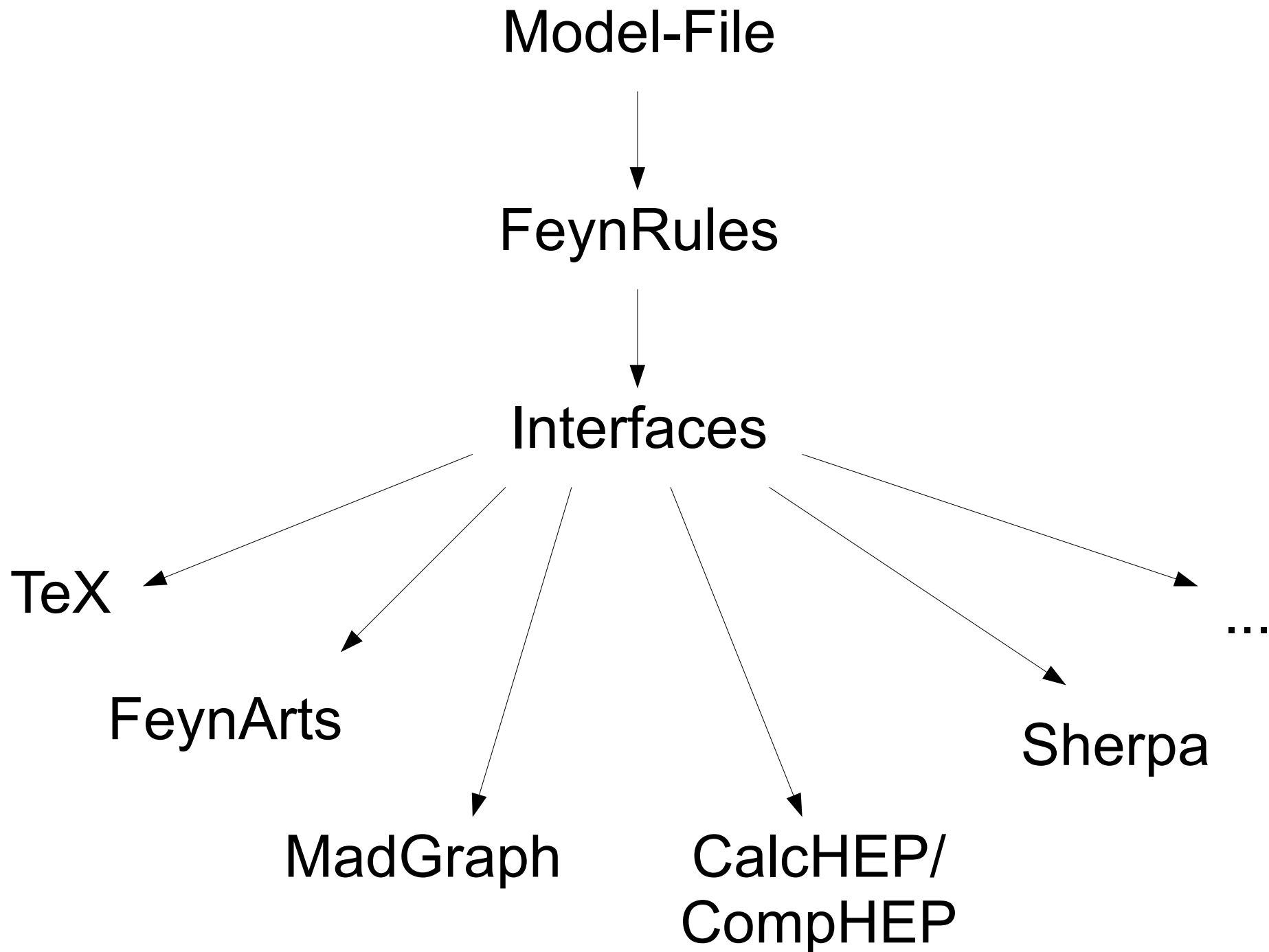












# Model-File

Model and Index information

$M\$GaugeGroups = \{gg1, gg2, gg3, \dots\}$

$M\$Parameters = \{param1, param2, param3, \dots\}$

$M\$ClassesDescription = \{field1, field2, field3, \dots\}$

$L =$  Lagrangian terms

[see appendix for more details](#)

# SM validation

31 key  
processes

Process	CalcHEP Stock	CalcHEP Feynman	CalcHEP Unitary	CompHEP Feynman	MadGraph Stock
gg->gg	116 490.	116 490.	116 490.	116 490.	116 470.
uū->gg	199.95	199.95	199.95	199.94	200.06
t $\bar{t}$ ->gg	64.595	64.595	64.595	64.592	64.564
e <sup>+</sup> e <sup>-</sup> ->μ <sup>+</sup> μ <sup>-</sup>	0.37195	0.37195	0.37195	0.37194	0.3721
e <sup>+</sup> e <sup>-</sup> ->e <sup>+</sup> e <sup>-</sup>	734.15	734.15	734.15	734.16	734.15
e <sup>+</sup> e <sup>-</sup> ->ν <sub>e</sub> $\bar{\nu}$ <sub>e</sub>	49.145	49.145	49.145	49.145	49.149
t $\bar{t}$ ->uū	16.018	16.018	16.018	16.018	16.017
uū->s $\bar{s}$	9.6103	9.6102	9.6103	9.6097	9.5995
u $\bar{d}$ ->c $\bar{s}$	0.23864	0.23864	0.23864	0.23864	0.23861
u $\bar{s}$ ->c $\bar{d}$	0.018947	0.018947	0.018947	0.018947	0.018939
t $\bar{t}$ ->W <sup>+</sup> W <sup>-</sup>	17.265	17.265	17.265	17.265	17.267
t $\bar{t}$ ->ZZ	1.2686	1.2686	1.2686	1.2686	1.2692
t $\bar{t}$ ->Zγ	1.3119	1.3119	1.3119	1.312	1.3134
t $\bar{t}$ ->γγ	0.088486	0.088486	0.088486	0.088485	0.088528
uū->W <sup>+</sup> W <sup>-</sup>	2.0465	2.0465	2.0465	2.0465	2.0467
uū->ZZ	0.21123	0.21123	0.21123	0.21123	0.21139
uū->Zγ	0.33812	0.33812	0.33812	0.33811	0.33791
uū->γγ	0.18322	0.18322	0.18322	0.18323	0.18327
τ <sup>+</sup> τ <sup>-</sup> ->W <sup>+</sup> W <sup>-</sup>	6.1871	6.187	6.187	6.187	6.193
τ <sup>+</sup> τ <sup>-</sup> ->ZZ	0.34765	0.34765	0.34765	0.34765	0.34765
τ <sup>+</sup> τ <sup>-</sup> ->Zγ	2.0057	2.0057	2.0057	2.0057	2.0051
τ <sup>+</sup> τ <sup>-</sup> ->γγ	2.7791	2.7791	2.7791	2.779	2.7783
u $\bar{d}$ ->W <sup>+</sup> W <sup>+</sup> W <sup>-</sup>	0.016192	0.016192	-	0.016175	0.016151
u $\bar{d}$ ->ZZW <sup>+</sup>	0.004209	0.0042089	-	0.0042012	0.0041918
u $\bar{d}$ ->γZW <sup>+</sup>	0.0085385	0.0085385	-	0.0085216	0.0085154
u $\bar{d}$ ->γγW <sup>+</sup>	0.0033698	0.0033698	-	0.00338	0.0033718
ZZ->ZZ	1.9672	1.9672	1.9672	1.9672	1.9663
W <sup>+</sup> W <sup>-</sup> ->ZZ	290.85	290.85	290.85	290.85	290.83
hh->hh	1.94	1.94	1.94	1.94	-
hh->ZZ	65.801	65.801	65.801	65.801	65.912
hh->W <sup>+</sup> W <sup>-</sup>	100.49	100.49	100.49	100.49	100.8

# 3-Site Model

Phys.Rev.D74:075011,2006

Chivukula, Coleppa, Di

Chiara, Simmons, He,

Kurachi, Tanabashi

arXiv:0708.2588

Belyaev, Chivukula,

Christensen, He, Kuang, Qi,

Simmons, Zhang



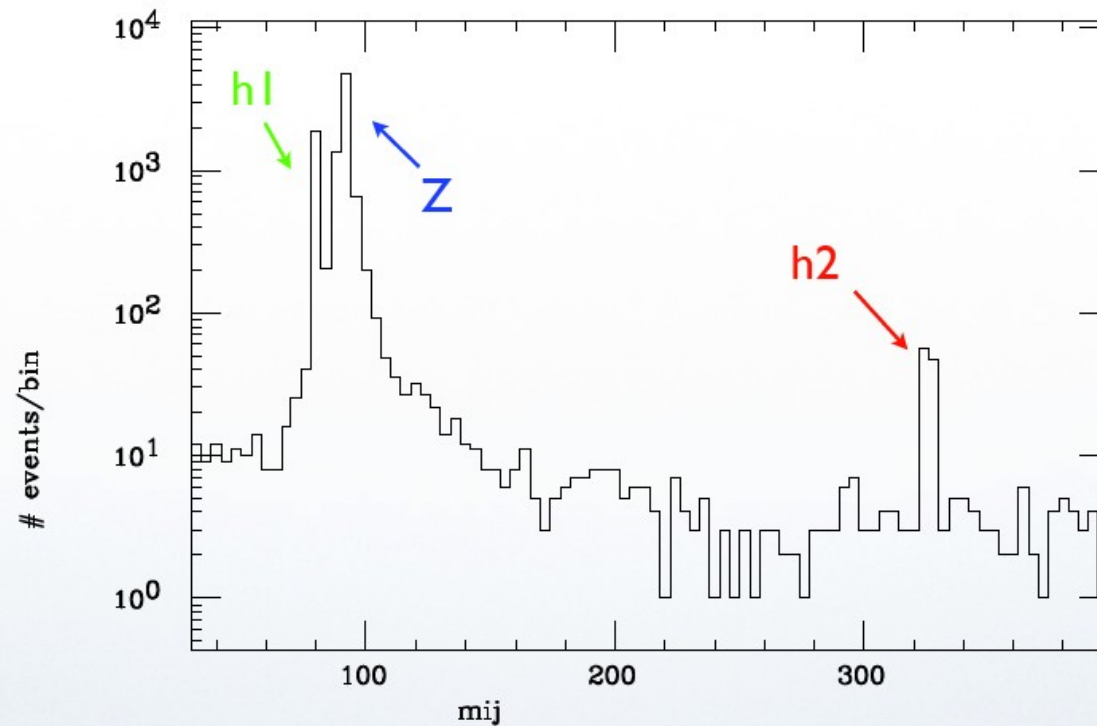
# 3-Site Model Validation

191 key subprocesses

	Lanhep CalcHEP Feynman	Lanhep CalcHEP Unitary	FeynRules CalcHEP Feynman	FeynRules CalcHEP Unitary	FeynRules CompHEP Feynman
$u\bar{u} \rightarrow gg$	170.5	170.5	170.5	170.5	170.49
$u'\bar{u}' \rightarrow gg$	0	0	0	0	0
$t\bar{t} \rightarrow gg$	55.906	55.906	55.906	55.906	55.903
$t'\bar{t}' \rightarrow gg$	0	0	0	0	0
$u\bar{u} \rightarrow \gamma\gamma$	0.15862	0.15862	0.15862	0.15862	0.15862
$u'\bar{u}' \rightarrow \gamma\gamma$	0	0	$3.6538 \times 10^{-37}$	$3.6538 \times 10^{-37}$	$3.6539 \times 10^{-37}$
$t\bar{t} \rightarrow \gamma Z'$	0.00016576	0.00016576	0.00016576	0.00016576	0.00016576
$t'\bar{t}' \rightarrow \gamma Z$	0.033204	0.033204	0.033204	0.033204	0.033204
$t'\bar{t}' \rightarrow \gamma Z'$	0.0049275	0.0049275	0.0049275	0.0049275	0.0049276
$t\bar{t} \rightarrow \gamma Z'$	0.042476	0.042476	0.042476	0.042476	0.042473
$t'\bar{t}' \rightarrow \gamma Z'$	0.012657	0.012657	0.012657	0.012657	0.012657

# Phenomenology with MadGraph

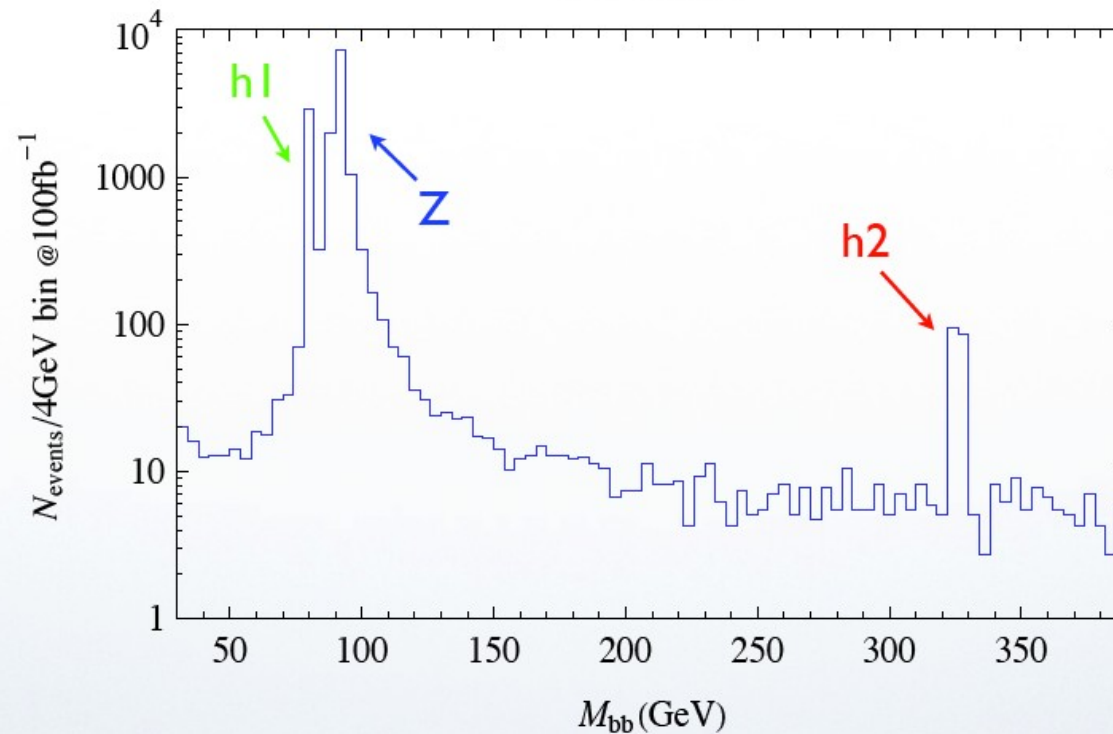
$m(b1,b2)$





# Phenomenology with CalcHep

$$e^+e^- \rightarrow Zb\bar{b}$$





# Summary

- We don't know what new physics we will discover at the LHC.
  - There are many interesting models with many variations.
- There are several great programs for calculating Feynman diagrams:

CalcHEP/CompHEP	MadGraph
FeynArts/FormCalc	Sherpa
...	...

  - Each has its own strengths and weaknesses.
  - Each has its own model-file format.
- There is one tool that writes model-files for each of these.

**FeynRules**

# Appendix

**Model-File**

# Model Information

M\$ModelName = "model name"

```
M$Information = {  
  Authors      -> {"Dr. X", "Dr. Y", ...},  
  Institution  -> {"Pheno State University", ...},  
  emails       -> {x@psu.edu, y@rsu.edu, ...},  
  date         -> "April 12, 2008",  
  references   -> {"Phys.Rev.D177:035001,2008", ...}  
}
```

# Index Declaration

IndexRange[ Index[Generation] ] = Range[3]

IndexRange[ Index[Color] ] = NoUnfold[ Range[3] ]

...

IndexStyle[ Generation, i ]

IndexStyle[ Color, a ]

...

# Gauge Groups

```
M$GaugeGroups = {  
  U1Y == {  
    Abelian          -> True,  
    GaugeBoson      -> B,  
    Charge           -> Y,  
    CouplingConstant -> gp  
  },  
  ...  
}
```

# Parameters

```
M$Parameters = {  
  \[Alpha]S == {  
    ParameterType -> External,  
    ParameterName -> aS,  
    Value         -> 0.118,  
    Description -> "Strong coupling at Z-pole"  
  },  
  ...  
}
```

# Particles

```
M$classesDescription = {  
  ...,  
  F[3] == {  
    ClassMembers      -> {u, c, t},  
    ClassName         -> uq,  
    SelfConjugate     -> False,  
    QuantumNumbers   -> {Q -> 2/3},  
    Indices          -> {Index[Generation], Index[Colour]},  
    FlavorIndex       -> Generation,  
    Mass             -> {Mu, {MU, 0}, {MC, 1.42}, {MT, 174.3}},  
    Width            -> {0, 0, {WT, 1.50833649}},  
    PDG              -> {2, 4, 6},  
    FullName         -> {"u-quark", "c-quark", "t-quark"}  
  },  
  ...  
}
```



# Lagrangian

```
FGlue[mu_,nu_,a_] := Module[{b,c},  
  del[ G[nu , a] , mu]  
  - del[ G[mu, a] , nu]  
  - gs f[a,b,c] G[mu, b] G[nu, c]  
];
```

```
LGlue := -1/4 FGlue[mu,nu,a] FGlue[mu,nu,a];
```

...

# Running FeynRules

# Load Model

```
$FeynRulesPath = "~/physics/FeynRules/FeynRules1.1.5";
```

```
SetDirectory[$FeynRulesPath];
```

```
<< FeynRules`;
```

```
SetDirectory[$FeynRulesPath <> "/Models/SM/"];
```

```
LoadModel["SM.fr"];
```

# Feynman Rules

FeynmanRules[LGauge];

Vertex 1

Particle 1 : Vector , G

Particle 2 : Vector , G

Particle 3 : Vector , G

Vertex:

$g_s f_{a_1, a_2, a_3}$

$$\left( p_1^{\mu_3} \eta_{\mu_1, \mu_2} - p_2^{\mu_3} \eta_{\mu_1, \mu_2} - p_1^{\mu_2} \eta_{\mu_1, \mu_3} + \right. \\ \left. p_3^{\mu_2} \eta_{\mu_1, \mu_3} + p_2^{\mu_1} \eta_{\mu_2, \mu_3} - p_3^{\mu_1} \eta_{\mu_2, \mu_3} \right)$$

# TeX Output

WriteTeXOutput[“VSM”, Output->”SM.tex”]

## 2 Vertices

### 2.1 3-point vertices

- Vertex  $\{G, 1\}$ ,  $\{G, 2\}$ ,  $\{G, 3\}$

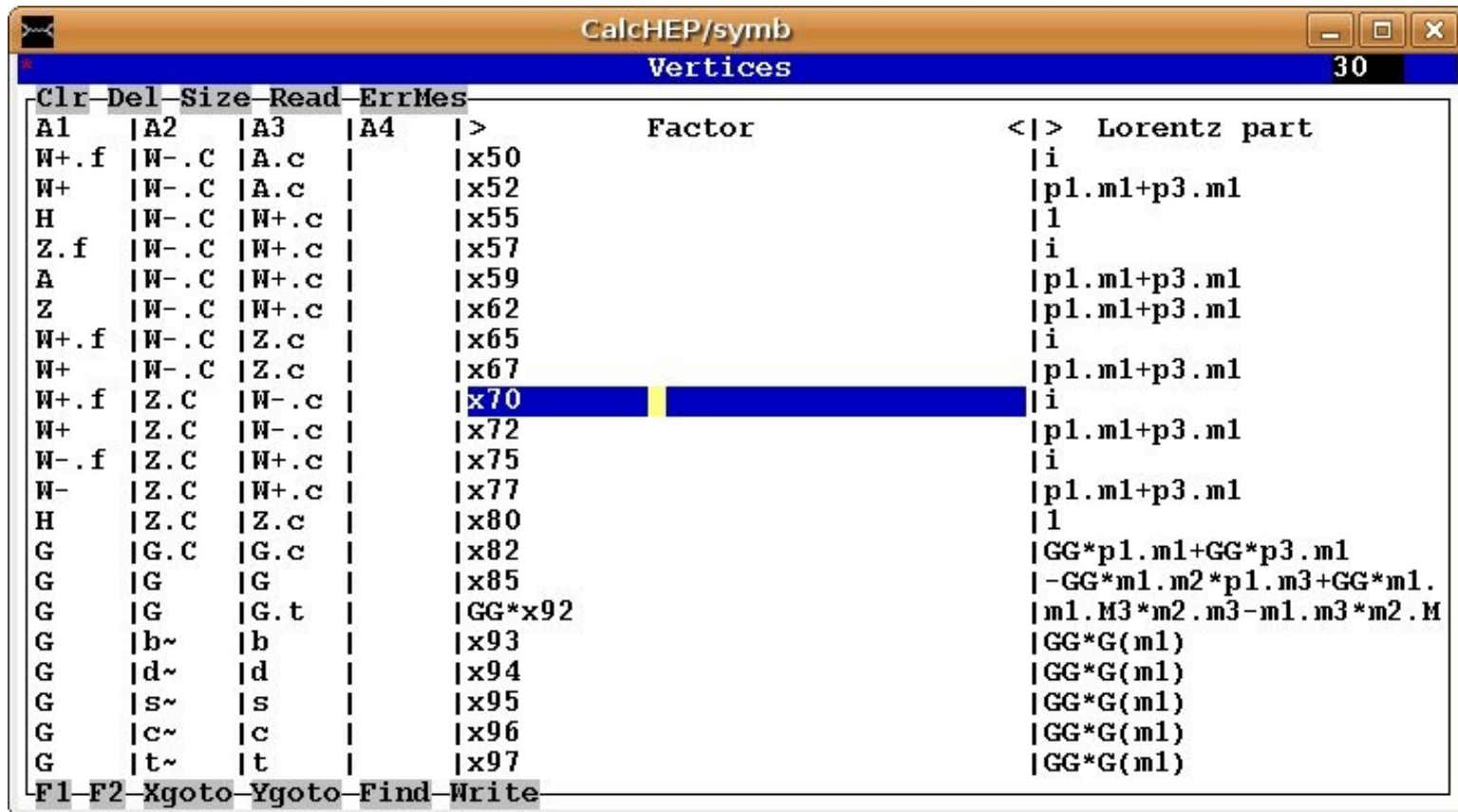
$$g_s f_{a_1, a_2, a_3} (p_1^{\mu_3} \eta_{\mu_1, \mu_2} - p_2^{\mu_3} \eta_{\mu_1, \mu_2} - p_1^{\mu_2} \eta_{\mu_1, \mu_3} + p_3^{\mu_2} \eta_{\mu_1, \mu_3} + p_2^{\mu_1} \eta_{\mu_2, \mu_3} - p_3^{\mu_1} \eta_{\mu_2, \mu_3})$$

- Vertex  $\{A, 1\}$ ,  $\{W^\dagger, 2\}$ ,  $\{W, 3\}$

$$i g_w s_w (p_1^{\mu_3} \eta_{\mu_1, \mu_2} - p_2^{\mu_3} \eta_{\mu_1, \mu_2} - p_1^{\mu_2} \eta_{\mu_1, \mu_3} + p_3^{\mu_2} \eta_{\mu_1, \mu_3} + p_2^{\mu_1} \eta_{\mu_2, \mu_3} - p_3^{\mu_1} \eta_{\mu_2, \mu_3})$$

# CalcHEP Output

WriteCHOutput[LSM]



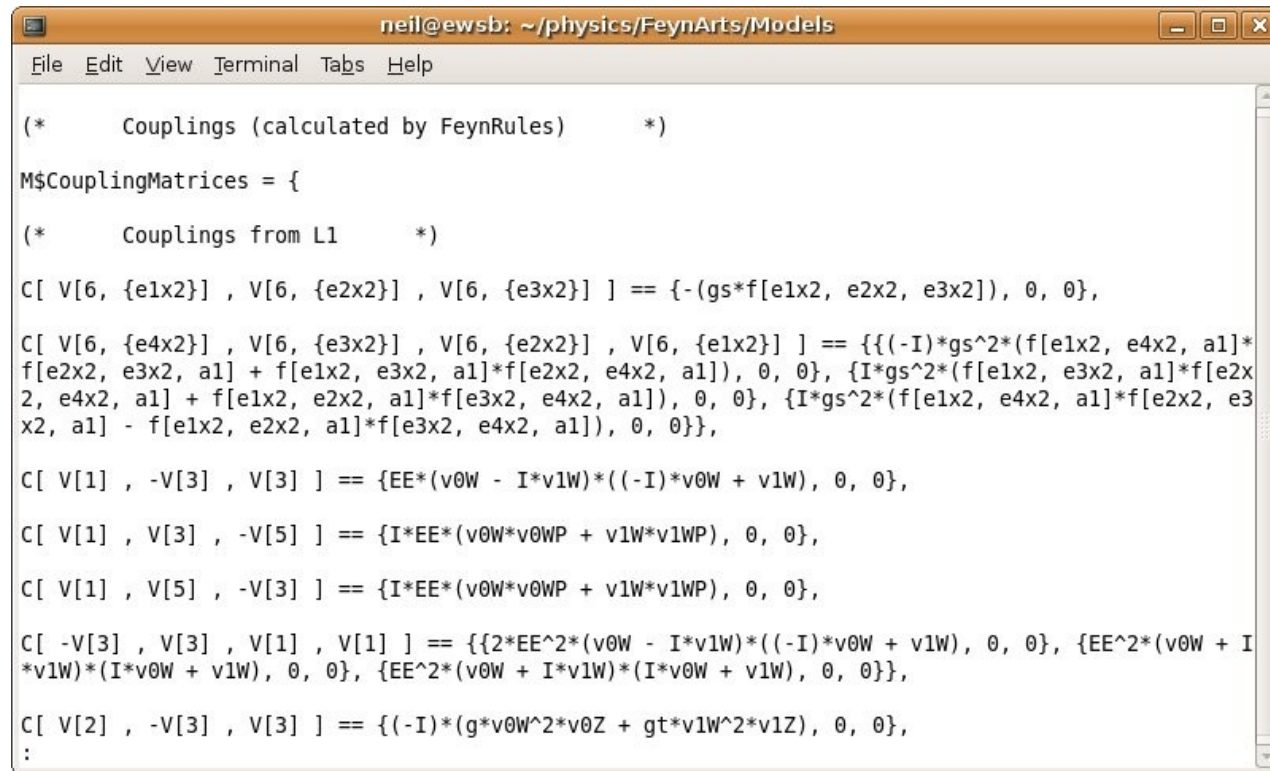
CalcHEP/symb  
Vertices 30

Clr	Del	Size	Read	ErrMes	A1	A2	A3	A4	>	Factor	< >	Lorentz part
					W+.f	W-.C	A.c		x50		i	
					W+	W-.C	A.c		x52		p1.m1+p3.m1	
					H	W-.C	W+.c		x55		1	
					Z.f	W-.C	W+.c		x57		i	
					A	W-.C	W+.c		x59		p1.m1+p3.m1	
					Z	W-.C	W+.c		x62		p1.m1+p3.m1	
					W+.f	W-.C	Z.c		x65		i	
					W+	W-.C	Z.c		x67		p1.m1+p3.m1	
					W+.f	Z.C	W-.c		x70		i	
					W+	Z.C	W-.c		x72		p1.m1+p3.m1	
					W-.f	Z.C	W+.c		x75		i	
					W-	Z.C	W+.c		x77		p1.m1+p3.m1	
					H	Z.C	Z.c		x80		1	
					G	G.C	G.c		x82		GG*p1.m1+GG*p3.m1	
					G	G	G		x85		-GG*m1.m2*p1.m3+GG*m1.	
					G	G	G.t		GG*x92		m1.M3*m2.m3-m1.m3*m2.M	
					G	b~	b		x93		GG*G(m1)	
					G	d~	d		x94		GG*G(m1)	
					G	s~	s		x95		GG*G(m1)	
					G	c~	c		x96		GG*G(m1)	
					G	t~	t		x97		GG*G(m1)	

F1 F2 Xgoto Ygoto Find Write

# FeynArts Output

WriteFeynArtsOutput[LSM]



```
neil@ewsb: ~/physics/FeynArts/Models
File Edit View Terminal Tabs Help

(*      Couplings (calculated by FeynRules)      *)

M$CouplingMatrices = {

(*      Couplings from L1      *)

C[ V[6, {e1x2}] , V[6, {e2x2}] , V[6, {e3x2}] ] == {-(gs*f[e1x2, e2x2, e3x2]), 0, 0},

C[ V[6, {e4x2}] , V[6, {e3x2}] , V[6, {e2x2}] , V[6, {e1x2}] ] == {{(-I)*gs^2*(f[e1x2, e4x2, a1]*
f[e2x2, e3x2, a1] + f[e1x2, e3x2, a1]*f[e2x2, e4x2, a1]), 0, 0}, {I*gs^2*(f[e1x2, e3x2, a1]*f[e2x
2, e4x2, a1] + f[e1x2, e2x2, a1]*f[e3x2, e4x2, a1]), 0, 0}, {I*gs^2*(f[e1x2, e4x2, a1]*f[e2x2, e3
x2, a1] - f[e1x2, e2x2, a1]*f[e3x2, e4x2, a1]), 0, 0}},

C[ V[1] , -V[3] , V[3] ] == {EE*(v0W - I*v1W)*((-I)*v0W + v1W), 0, 0},

C[ V[1] , V[3] , -V[5] ] == {I*EE*(v0W*v0WP + v1W*v1WP), 0, 0},

C[ V[1] , V[5] , -V[3] ] == {I*EE*(v0W*v0WP + v1W*v1WP), 0, 0},

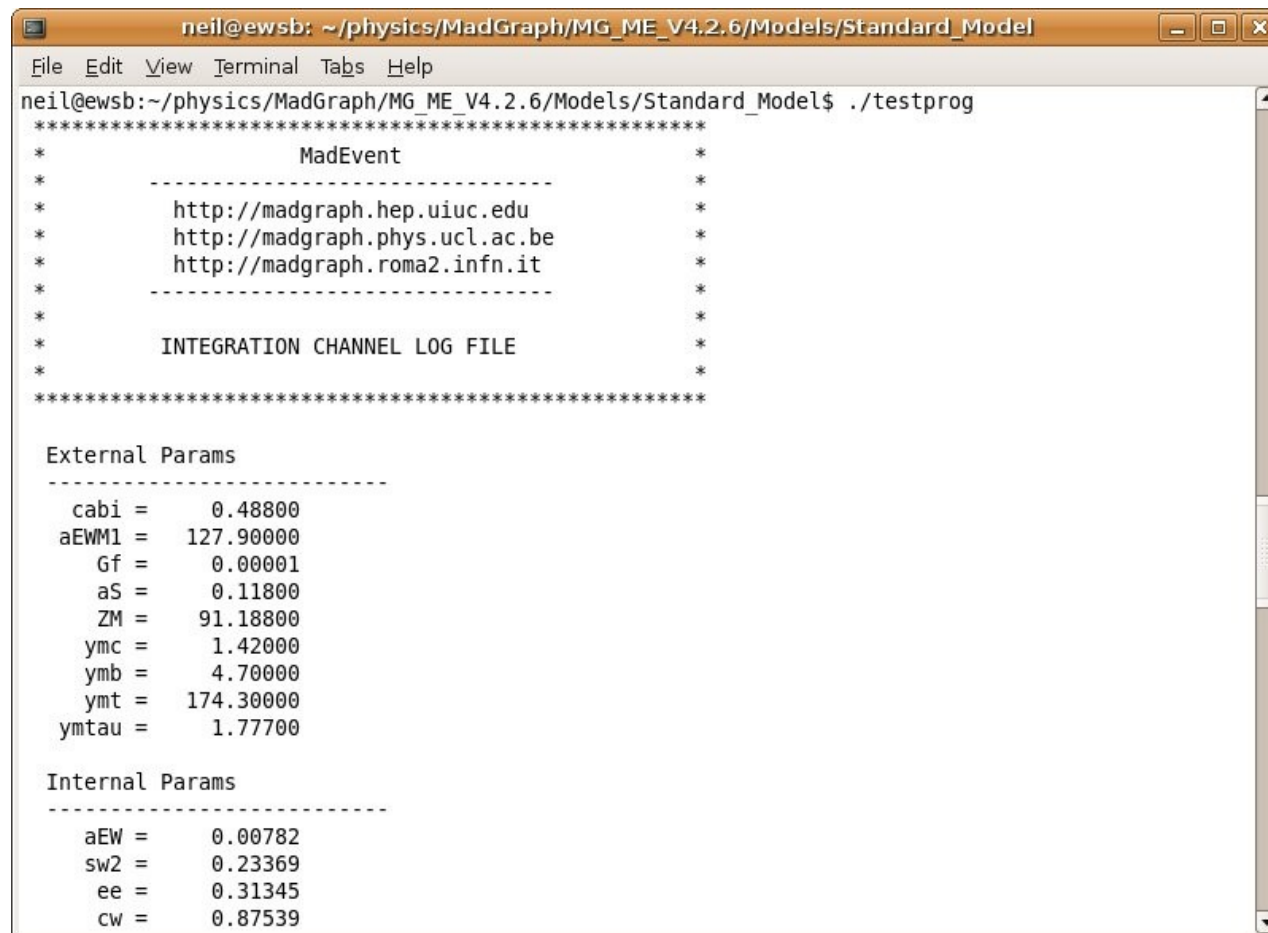
C[ -V[3] , V[3] , V[1] , V[1] ] == {{2*EE^2*(v0W - I*v1W)*((-I)*v0W + v1W), 0, 0}, {EE^2*(v0W + I
*v1W)*(I*v0W + v1W), 0, 0}, {EE^2*(v0W + I*v1W)*(I*v0W + v1W), 0, 0}},

C[ V[2] , -V[3] , V[3] ] == {(-I)*(g*v0W^2*v0Z + gt*v1W^2*v1Z), 0, 0},

:
}
```

# MadGraph Output

WriteMGOutput[LSM]



```
neil@ewsb: ~/physics/MadGraph/MG_ME_V4.2.6/Models/Standard_Model
File Edit View Terminal Tabs Help
neil@ewsb:~/physics/MadGraph/MG_ME_V4.2.6/Models/Standard_Model$ ./testprog
*****
*                               *
*               MadEvent        *
*                               *
*   -----                    *
*   http://madgraph.hep.uiuc.edu *
*   http://madgraph.phys.ucl.ac.be *
*   http://madgraph.roma2.infn.it *
*   -----                    *
*                               *
*   INTEGRATION CHANNEL LOG FILE *
*                               *
*****

External Params
-----
cabi = 0.48800
aEW1 = 127.90000
Gf = 0.00001
aS = 0.11800
ZM = 91.18800
ymc = 1.42000
ymb = 4.70000
ymt = 174.30000
ymtau = 1.77700

Internal Params
-----
aEW = 0.00782
sw2 = 0.23369
ee = 0.31345
cw = 0.87539
```